WORKSHOP CALCULATION & SCIENCE

(NSQF)

1st YEAR

(As per Revised Syllabus July 2022)

Lift & Escalator Mechanic



DIRECTORATE GENERAL OF TRAINING MINISTRY OF SKILL DEVELOPMENT & ENTREPRENEURSHIP GOVERNMENTOF INDIA



NATIONAL INSTRUCTIONAL MEDIA INSTITUTE, CHENNAI

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Workshop Calculation & Science Lift & Escalator Mechanic - 1st Year NSQF As per Revised Syllabus July 2022

Developed & Published by



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FOREWORD

The Government of India has set an ambitious target of imparting skills one out of every four Indians, to help them secure jobs as part of the National Skills Development Policy. Industrial Training Institutes (ITIs) play a vital role in this process especially in terms of providing skilled manpower. Keeping this in mind, and for providing the current industry relevant skill training to Trainees, ITI syllabus has been recently updated with the help of comprising various stakeholder's viz. Industries, Entrepreneurs, Academicians and representatives from ITIs.

The National Instructional Media Institute (NIMI), Chennai, has now come up with instructional material to suit the revised curriculum for **Workshop Calculation & Science - Lift & Escalator Mechanic 1**st **Year** NSQF (Revised 2022) under CTS will help the trainees to get an international equivalency standard where their skill proficiency and competency will be duly recognized across the globe and this will also increase the scope of recognition of prior learning. NSQF trainees will also get the opportunities to promote life long learning and skill development. I have no doubt that with NSQF the trainers and trainees of ITIs, and all stakeholders will derive maximum benefits from these IMPs and that NIMI's effort will go a long way in improving the quality of Vocational training in the country.

The Executive Director & Staff of NIMI and members of Media Development Committee deserve appreciation for their contribution in bringing out this publication.

Jai Hind

Ms. TRISHALJIT SETHI,

Additional Secretary / Director General (Training), Ministry of Skill Development & Entrepreneurship, Government of India.

New Delhi - 110 001

PREFACE

The National Instructional Media Institute(NIMI) was set up at Chennai, by the Directorate General of Training, Ministry of skill Development and Entrepreneurship, Government of India, with the technical assistance from the Govt of the Federal Republic of Germany with the prime objective of developing and disseminating instructional Material for various trades as per prescribed syllabus and Craftsman Training Programme(CTS) under NSQF levels.

The Instructional materials are developed and produced in the form of Instructional Media Packages (IMPs), consisting of Trade Theory, Trade Practical, Test and Assignment Book, Instructor Guide. The above material will enable to achieve overall improvement in the standard of training in ITIs.

A national multi-skill programme called SKILL INDIA, was launched by the Government of India, through a Gazette Notification from the Ministry of Finance (Dept of Economic Affairs), Govt of India, dated 27th December 2013, with a view to create opportunities, space and scope for the development of talents of Indian Youth, and to develop those sectors under Skill Development.

The emphasis is to skill the Youth in such a manner to enable them to get employment and also improve Entrepreneurship by providing training, support and guidance for all occupation that were of traditional types. The training programme would be in the lines of International level, so that youths of our Country can get employed within the Country or Overseas employment. The **National Skill Qualification Framework** (**NSQF**), anchored at the National Skill Development Agency(NSDA), is a Nationally Integrated Education and competency-based framework, to organize all qualifications according to a series of **levels of Knowledge**, **Skill and Aptitude.** Under NSQF the learner can acquire the Certification for Competency needed at any level through formal, non-formal or informal learning.

The **Workshop Calculation & Science -** Lift & Escalator Mechanic 1st Year NSQF (Revised 2022) under CTS is one of the book developed by the core group members as per the NSQF syllabus.

The **Workshop Calculation & Science -** Lift & Escalator Mechanic 1st Year NSQF (Revised 2022) under CTS as per NSQF is the outcome of the collective efforts of experts from Field Institutes of DGT, Champion ITI's for each of the Sectors, and also Media Development Committee (**MDC**) members and Staff of **NIMI**. NIMI wishes that the above material will fulfill to satisfy the long needs of the trainees and instructors and shall help the trainees for their Employability in Vocational Training.

NIMI would like to take this opportunity to convey sincere thanks to all the Members and Media Development Committee (MDC) members.

Chennai - 600 032

EXECUTIVE DIRECTOR

ACKNOWLEDGEMENT

The National Instructional Media Institute (NIMI) sincerely acknowledge with thanks the co-operation and contribution of the following Media Developers to bring this IMP for the course **Workshop Calculation & Science - Lift & Escalator Mechanic 1**st **Year** as per NSQF Revised 2022.

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NIMI records its appreciation of the **Data Entry**, **CAD**, **DTP Operators** for their excellent and devoted services in the process of development of this IMP.

NIMI also acknowledges with thanks, the efforts rendered by all other staff who have contributed for the development of this book.

INTRODUCTION

The material has been divided into independent learning units, each consisting of a summary of the topic and an assignment part. The summary explains in a clear and easily understandable fashion the essence of the mathematical and scientific principles. This must not be treated as a replacment for the instructor's explanatory information to be imparted to the trainees in the classroom, which certainly will be more elaborate. The book should enable the trainees in grasping the essentials from the elaboration made by the instructor and will help them to solve independently the assignments of the respective chapters. It will also help them to solve the various problems, they may come across on the shop floor while doing their practical exercises.

The assignments are presented through 'Graphics' to ensure communications amongst the trainees. It also assists the trainees to determine the right approach to solve the problems. The required relevent data to solve the problems are provided adjacent to the graphics either by means of symbols or by means of words. The description of the symbols indicated in the problems has its reference in the relevant summaries.

At the end of the exercise wherever necessary assignments, problems are included for further practice.

Time allotment:

Duration of 1st Year : 30 Hrs

Time allotment for each title of exercises has been given below. **Workshop Calculation & Science - Lift & Escalator Mechanic** 1st Year NSQF Revised Syllabus 2022.

S.No	Title	Exercise No.	Time in Hrs
1	Unit, Fractions	1.1.01 - 1.1.07	4
2	Square root, Ratio and Proportions, Percentage	1.2.08 - 1.2.14	6
3	Material Science	1.3.15 & 1.3.16	2
4	Mass, Weight, Volume and Density	1.4.17 & 1.4.18	3
5	Speed and Velocity, Work, Power and Energy	1.5.19 & 1.5.20	2
6	Heat & Temperature and Pressure	1.6.21 - 1.6.23	5
7	Mensuration	1.7.24 - 1.7.27	5
8	Trigonometry	1.8.28 - 1.8.30	3
		Total	30 Hrs

LEARNING / ASSESSABLE OUTCOME

On completion of this book you shall be able to

- Demonstrate basic mathematical concept and principles to perform practical operations.
- Understand and explain basic science in the field of study.

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SYLLABUS

1st Year

Workshop Calculation & Science - Lift & Escalator Mechanic Revised syllabus July 2022 under CTS

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	4 Factors, HCF, LCM and Problems	
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	6 Decimal Fractions – Addition, Subtraction, Multiplication & Division	
	7 Solving Problems by using calculator	
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	2 Simple problems using calculator	
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	4 Ratio and Proportion	
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	2 Introduction of iron and cast iron	
IV	Mass, Weight, Volume and Density	3
	1 Mass, volume, density and weight	
	2 Related problems for mass, volume, density and weight	
V	Speed and Velocity, Work, Power and Energy	2
	1 Work, power, energy, HP, IHP, BHP and efficiency	
	2 Potential energy, Kinetic Energy and related problems with assignment	
VI	Heat & Temperature and Pressure	5
	1 Concept of heat and temperature, effects of heat, difference between heat and temperature, boiling point & melting point of different metals and non-metals	

0.11	T :41_	Times in 11
S.No.	Title	Time in Hrs
	2 Scales of temperature, Celsius, Fahrenheit, Kelvin and Conversion between scales of temperature	
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VII	Mensuration	5
	1 Area and perimeter of square, rectangle and parallelogram	
	2 Area and Perimeter of triangles	
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	4 Surface area and Volume of solids - cube, cuboid, cylinder, sphere and hollow cylinder	
VIII	Trigonometry	3
	1 Measurement of angles	
	2 Trigonometrical ratios	
	3 Trigonometrical tables	
	Total	30

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.1.01 Unit, Fractions - Classification of unit system

Necessity

All physical quantities are to be measured in terms of standard quantities.

Unit

A unit is defined as a standard or fixed quantity of one kind used to measure other quantities of the same kind.

Classification

Fundamental units and derived units are the two classifications.

Fundamental units

Units of basic quantities of length, mass and time.

Derived units

Units which are derived from basic units and bear a constant relationship with the fundamental units.E.g. area, volume, pressure, force etc.

Systems of units

- F.P.S system is the British system in which the basic units of length, mass and time are foot, pound and second respectively.
- C.G.S system is the metric system in which the basic units of length, mass and time are centimeter, gram and seconds respectively.
- M.K.S system is another metric system in which the basic units of length, mass and time are metre, kilogram and second respectively.
- S.I. units are referred to as Systems International units which is again of metric and the basic units, their names and symbols are as follows.

Fundamental units and derived units are the two classifications of units.

Length, mass and time are the fundamental units in all the systems (i.e) F.P.S, C.G.S, M.K.S and S.I. systems.

Example

Length: What is the length of copper wire in the roll, if the roll of copper wire weighs 8kg, the dia of wire is 0.9cm and the density is 8.9 gm/cm³?

Solution

mass of copper wire in the roll = 8 kg (or)8000 gramsDia of copper wire in the roll = 0.9 cmDensity of copper wire = 8.9 gm/cm^3

Area of cross section of copper wire

$$=\frac{\pi\,d^2}{4}=\frac{\pi\times(0.9^2)}{4}=0.636cm^2$$

Volume of copper wire

$$= \frac{\text{Mass of copper wire}}{\text{Density of copper wire}} = \frac{8000 \text{ grams}}{8.9 \text{ gm/cm}^3} = 898.88 \text{ cm}^3$$

Length of copper wire

$$= \frac{\text{Volume of copper wire}}{\text{Area of cross section of copper wire}} = \frac{898.88 \text{cm}^3}{0.636 \text{cm}^2}$$
$$= 1413.33 \text{ cm}$$

Length of copper wire =1413cm.

Time: The S.I. unit of time, the second, is another base units of S.I., it is defined as the time interval occupied by a number of cycles of radiation from the calcium atom. The second is the same quantity in the S.I. in the British and in the U.S. systems of units.

S.No.	Basic quantity	Britishun	its		Metric u	nits		Internation	al units
		F.P.S	Symbol	C.G.S	Symbol	M.K.S	Symbol	S.I Units	Symbol
1	Length	Foot	ft	Centimetre	cm	Metre	m	Metre	m
2	Mass	Pound	lb	Gram	g	Kilogram	kg	Kilogram	Kg
3	Time	Second	S	Second	S	Second	s	Second	S
4	Current	Ampere	А	Ampere	А	Ampere	А	Ampere	А
5	Temperature	Fahrenheit	°F	Centigrade	°C	Centigrade	°C	Kelvin	К
6	Light intensity	Candela	Cd	Candela	Cd	Candela	Cd	Candela	Cd

Fundamental units of F.P.S, C.G.S, M.K.S and S.I

Workshop Calculation & Science - Lift & Escalator Mechanic

Exercise 1.1.02

Unit, Fractions - Fundamental and Derived units F.P.S, C.G.S, M.K.S and SI units

S.No	Physical quantity	Britishunits		Metr	Metric units			International units	
		FPS	Symbol	CGS	Symbol	MKS	Symbol	SIUnits	Symbol
~	Area	Squarefoot	ft²	Square centimetre	cm ²	Square metre	m^2	Square metre	m^2
7	Volume	Cubicfoot	ft³	Cubic centimetre	cm ³	Cubic metre	m³	Cubic metre	m³
3	Density	Pound per cubic foot	lb/ft ³	Gram per cubic centimetre	g/cm³	Kilogram per cubic metre	kg/m³	Kilogram per cubic metre	Kg/m³
4	Speed	Foot per second	ft/s	Centimetre per second	cm/sec	Metre per second	m/sec	Metre per second	m/sec
5	Velocity (linear)	Foot per second	ft/s	Centimetre per second	cm/sec	Metre per second	m/sec	Metre per second	m/sec
9	Acceleration	Foot per square	ft/s ²	Centimetre per	cm/sec ²	Metre per square	m/sec ²	Metre per square	m/sec ²
		Secolia		adual e accol la		פברסוומ		SECOLIC	
7	Retardation	Foot per square Second	ft/s²	Centimetre per square second	cm/sec ²	Metre per square second	m/sec²	Metresquaresecond	m/sec ²
8	Angular velocity	Degree per second	Deg/sec	Radian per second	rad/sec	Radian per second	rad/sec	Radian per second	rad/sec
6	Mass	Pound (slug)	qI	Gram	g	Kilogram	kg	Kilogram	kg
10	Weight	Pound	qI	Gram	g	Kilogramweight	kg	Newton	Ν
11	Force	Pounds	lbf	dyne	dyn	Kilogram force	kgf	Newton	$N(kgm/sec^2)$
12	Power	Foot pound per second	ft.lb/sec	Gram.centimetre/sec	g.cm/ sec	kilogram metre per second	kg.m/ sec		-
		Horse power	dų	Erg per second		watt	Μ	watt	W(J/sec)
13	Pressure, Stress	Pound per square inch	lb/in²	Gram per square centimetre	g/cm ²	Kilogram per square metre	kg/m²	Newton per square metre	N/m²
14	Energy, Work	Foot.pound	ft.lb	Gram centimetre	g.cm	Kilogram metre	kg.m	joule	J(Nm)
15	Heat	British thermal unit	BTU	calorie	Cal	joule	ſ	joule	J(Nm)
16	Torque	Pound force foot	lbf.ft	Newton millimetre	N mm	Kilogram metre	kg.m	Newton metre	Nm
17	Temperature	DegreeFahrenheit	Ц °	Degree Centigrade	ပ	Kelvin	¥	Kelvin	×

Derived units of F.P.S. C.G.S. M.K.S and SI system

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.1.03 Unit, Fractions - Measurement units and conversion

Units and abbreviations

Quantity	Units	Abbreviation of unit
Calorificvalue	kilojoules per kilogram	kJ/kg
Specific fuel consumption	kilogram per hour per newton	kg/hr/N
Length	millimetre, metre, kilometre	mm, m, km
Mass	kilogram, gram	kg, g
Time	seconds, minutes, hours	s, min, h
Speed	centimetre per second, metre per second kilometre per hour, miles per hour	cm/s, m/s km/h, mph
Acceleration	metre-per-square second	m/s²
Force	newtons, kilonewtons	N,kN
Moment	newton-metres	Nm
Work	joules	J
Power	horsepower, watts, kilowatts	Hp, W, kW
Pressure	newton per square metre kilonewton per square metre	N/m² kN/m²
Angle	radian	rad
Angularspeed	radians per second radians-per-square second revolutions per minute revolutions per second	rad/s rad/s² Rpm rev/s

Decimal multiples and parts of unit

Decimal power	Value	Prefixes	Symbol	Stands for
1012	10000000000	tera	Т	billion times
10 ⁹	100000000	giga	G	thousand millintimes
10 ⁶	1000000	mega	М	million times
10 ³	1000	kilo	К	thousand times
10 ²	100	hecto	h	hundred times
10 ¹	10	deca	da	ten times
10-1	0.1	deci	d	tenth
10-2	0.01	centi	с	hundredth
10 ⁻³	0.001	milli	m	thousandth
10-6	0.000001	micro	μ	millionth
10 ⁻⁹	0.00000001	nano	n	thousand millionth
10 ⁻¹²	0.00000000001	pico	р	billionth

SI units and the British units:

Quantity	SI unit \rightarrow British unit	British unit \rightarrow SI unit
Length	1 m = 3.281 ft	1 ft = 0.3048 m
	1 km = 0.621 mile	1 mile = 1.609 km
Speed	1 m/s = 3.281 ft/s	1 ft/s = 0.305 m/s
	1 km/h = 0.621 mph	1 mph = 1.61 km/h
Acceleration	1 m/s² = 3.281 ft/s²	1 ft/s² = 0.305 m/s²
Mass	1 kg = 2.205 lb	1 lb = 0.454 kg
Force	1 N = 0.225 lbf	1 lbf = 4.448 N
	1 MN	1 million newtons
Torque	1 Nm = 0.738 lbf ft	1 lbf ft = 1.355 Nm
Pressure	1 N/m² = 0.000145 lbf/in² 1 Pa = 1 N/m²	1 lbf/in ² = 6.896 kN/m ²
	$1 \text{ bar} = 14.5038 \text{ lbf/in}^2$	1 lbf/in ² = 6.895 kN/m ²
Energy, work	1 J = 0.738 ft lbf	1 ft lbf = 1.355 J
0,7	1 J = 0.239 calorie	1 calorie = 4.186 J
	1 kJ = 0.948 BTU	1 BTU = 1.055 kJ
	(1 therm = 100 000 BTU)	
	1 kJ = 0.526 CHU	1 CHU = 1.9 kJ
Power	1 kW = 1.34 hp	1 hp = 0.7457 kW
Fuel consumption	1km/L = 2.82 mile/gallon	1 mpg = 0.354 km/L
Specific fuel	1 kg/kWh = 1.65 lb/bhp h	1 lb/bhp h = 0.606 kg/kWh
consumption	1 litre/kWh=1.575 pt/bhp h	1 pt/bhp h = 0.631 litre/kW
Calorificvalue	1 kJ/kg = 0.43 BTU/lb	1 BTU/lb = 2.326 kJ/kg
	1 kJ/kg = 0.239 CHU/lb	1 CHU/lb = 4.188 kJ/kg

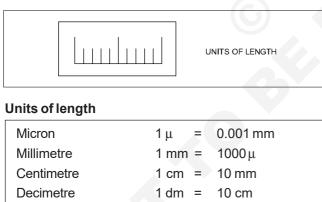
Prefixes for decimal multiples and submultiples

	Use	
1 Megapascal	= 1 MPa	= 1000000 Pa
1 Kilowatt	= 1 kW	= 1000 W
1 Hectolitre	= 1 hL= 1	100 L
Decanewton	= 1 daN	= 10 N
Decimetre	= 1 dm	= 0.1 m
1 Centimetre	= 1 cm	= 0.01 m
1 Millimetre	= 1 mm	= 0.001 m
1 Micrometre	= 1 um	= 0.000001 m

Conversion factors

1 inch	=	25.4 mm
1 mm	=	0.03937 inch
1 metre	=	39.37 inch
1 micron	=	0.00003937"
1 kilometre	=	0.621 miles
1 pound	=	453.6 g
1 kg	=	2.205 lbs
1 metric ton	=	0.98 ton

Units of physical quantities



Units of area

UNITS OF AREA

00 mm ²
00 cm ²
00 dm ²
00 m ²
00 a
00 ha
6.45 cm ²
.093 m ²
.84 m²
0.76 ft ²
0.5 a
2.47 acres
).4047 Hec
tare
10000 sq.
metre

Units of weight



Milligram - force	1 mgf	
Gram-force	1 gf	1000 mgf
Kilogram-force	1 kgf	= 1000 gf
Tonne	1 t	= 1000 kgf
Ounce	1	= 28.35 gf
Pound	1 lbs	= 0.454 kgf
Longton	1	= 1016 kgf
Short ton	1	= 907 kgf

WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1 st Year : Exercise 1.1.03	

Micron	1μ	=	0.001 mm
Millimetre	1 mm	=	1000μ
Centimetre	1 cm	=	10 mm
Decimetre	1 dm	=	10 cm
Metre	1 m	=	10 dm
Kilometre	1 km	=	1000 m
Inch	1"	=	25.4 mm
Foot	1'	=	0.305 m
Yard	1 Yd	=	0.914 m
Nautical mile	1 NM	=	1852 m
Geographical mile	1	=	1855.4 m
	1 NM 1		



UNITS OF VOLUME AND CAPACITY

Units of volume and capacity

Cubic millimetre	1 mm ³	
Cubic centimetre	1 cm ³	= 1000 mm ³
Cubic decimetre	1 dm ³	= 1000 cm ³
Cubic metre	1 m³	= 1000 dm ³
Litre	11	= 1 dm ³
Hectolitre	1 hl	= 100 I
Cubic inch	1 cu. in	= 16.387 cm ³
Cubicfoot	1 cu. ft	= 28317 cm ³
Gallon (British)	1 gal	= 4.54 l
1cubic metre	1 m³	= 1000 litres
1000 Cu.cm	1000 cm	³ = 1 litre
1 cubic foot	1 ft ³	= 6.25 Gallon
1 litre	1lt	= 0.22 Gallon

Work

		WORK
Kilogram-force	1 kgfm	= 9.80665 J
Metre	1 kgfm	= 9.80665 Ws
Joule	1 J	= 1 Nm
Watt-second	1 Ws	= 0.102 kgfm
Kilowatthour	1 kWh	= 3.6 x 10 ⁶ J
		= 859.8456 kcal _{ır}
I.T.Kilocalorie	1 kcal _{ıт}	= 426.kgfm

Power



Circular unit

CIRCULAR OF UNIT Ki Radian Relationship between Radian and Degree 1 Radian = $\frac{180^{\circ}}{\pi}$ 180° = π Radian; 10 1 Degree = $\frac{\pi}{\pi}$ Radian 1.1				Kilogr
Radian M Relationship between Radian and Degree 1 1 Radian = $\frac{180^{\circ}}{\pi}$ 180^{\circ} = π Radian; 1 Degree = $\frac{\pi}{\pi}$ Radian				1 k
Relationship between Radian and DegreeM1 Radian= $\frac{180^{\circ}}{\pi}$ 180^{\circ}= π Radian;1 Degree= $\frac{\pi}{\pi}$ Radian			CIRCULAR OF UNIT	Kild
Relationship between Radian and Degree 1 Radian = $\frac{180^{\circ}}{\pi}$ 180° = π Radian; 1 Degree = $\frac{\pi}{\pi}$ Radian	Radian			
$1 \text{Radian} = \frac{\pi}{\pi}$ $180^{\circ} = \pi \text{Radian};$ $1 \text{Degree} = \frac{\pi}{\pi} \text{Radian}$ 1.7	Relationshi	ip between Radian a	and Degree	Me
$180^{\circ} = \pi \text{Radian};$ $1 \text{Degree} = \frac{\pi}{2} \text{Radian}$	1 Radian			
1 Degree = $\frac{1}{2}$ Radian	180º			10
100	1 Degree	$=\frac{\pi}{180}$ Radian	0	I.T.

Kilogram-force metre/second			
1 kgfm/s	= 9.80665 W		
Kilowatt	1 kW = 1000 W = 1000 J/s		
	= 102 kgfm/s (approx.)		
Metric horse power	1 HP = 75 kgfm/s		
	= 0.736 kW		
1 Calorie	=4.187J		
I.T.Kilocalorie/hour = 1 kcal _{IT/h} = 1.163 W			

Pressure

Pascal	1 Pa	= 1 N/m ²	1 atm	= 101325 Pa
Bar	1 bar = 10N/cm ²	= 100000 Pa-Torr	1 torr	= <u>101325</u> ≈ 133.32 pa
Atmosphere	1 atm	= 1 kgf/cm ²	1 kgf/cm ² =	= 735.6 mm of mercury

TEMPERATURE

Scale	Freezingpoint	Boiling point	TEMPERATURE
Centigrade (°C)	0°C	100°C	
Fahrenheit(°F)	32°F	212°F	
Kelvin (K)	273K	373K	
Reaumur(°R)	0°R	80°R	

 $\frac{{}^{\circ}\mathsf{R}}{80} = \frac{{}^{\circ}\mathsf{C}}{100} = \frac{\mathsf{K}-273}{100} = \frac{{}^{\circ}\mathsf{F}-32}{180}$

	Force	In C.G.S. System : Force (Dyne)	= Mass (gm)XAcceleration (cm/sec ²)
		In F.P.S. System : Force (Poundal)	= Mass (Ib) X Acceleration (ft./sec ²)
		In M.K.S System : Force (Newton)	= Mass (Kg) x Acceleration (mtr./sec ²)
		1 Dyne	= 1 gm x1 cm/sec ²
		1 Poundal	= 1 lb x 1 ft/sec ²
		1 Newton	= 1 kg x 1 mtr/sec ² = 10 ⁵ dynes
		1gm weight	= 981 Dynes
		1 lb weight	= 32 Poundals
		1 kg weight	= 9.81 Newtons
L			

ELECTRICALQUANTITIES

V	Electric potential	V	Volt	V(W/A)	
Е	Electromotive force	V	Volt	V(W/A)	ELECTRICAL QUANTITIES
I	Electric current	А	Ampere	A	
R	Electric resistance	Ω	Ohm	Ω (V/A)	7
е	Specific resistance	Ωm	Ohm metre	Vm/A	
G	Conductance	Ω-1	Siemens	S	

Assignment - Answer the following question.

1	Convert 320 kilometres into miles	b	Ma	ass			
2	Convert 16 tons into kilograms		i	650 g	=		kg
3	Convert 40 inches into centimetres		ii	120 mg	=	<u> </u>	_ 0
4	Convert 8 metres into feet			C C	-		_g
5	Convert 2.5 gallons into litres	С	FC	orce			
6	Convert 5 litres into gallons		i	1.2 N	=	<u> </u>	_kg
7	120°C = °F.		ii	25 kg	=	<u> </u>	_N
8	Expand the abbreviations of the following	d	W	ork, enerç	gy, amou	nt of hea	at
	a N/m²		i	120 KJ	=		_J
	b RPM		ii	300 wh	=		_kwh
9	Convert the following S.I. units as required.	е	Po	ower			
	a Length		i	0.2 kW	=		W
	i 3.4 m = mm		ii	350 W	=		_kW
	ii 10.2 km = mile	f	Сс	onvert as r	equired.		
			i	5 N	=		_KN

Prime Numbers and whole Numbers Factor	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
A factor is a small number which divides exactly into a bigger number.e.g.	$2 \frac{32}{16}$ 2 8
To find the factors of 24, 72, 100 numbers $24 = 2 \times 2 \times 2 \times 3$	$2 \frac{3}{4}$
$72 = 2 \times 2 \times 2 \times 3 \times 3$	
$100 = 2 \times 2 \times 5 \times 5$	Factors of 128 = 2 x 2 x 2 x 2 x 2 x 2 x 2 x 2
The numbers 2,3,5 are called factors.	Select prime numbers from 3 to 29
Definition of a prime factor	3,5,7,11,13,17,19,23,29
Prime factor is a number which divides a prime number into factors.e.g.	 Find the HCF of the following group of numbers HCF of 78, 128, 196
57 = 3 x 19	2 78
The numbers 3 and 19 are prime factors.	3 <u>39</u> 13
They are called as such, since 3 & 19 also belong to prime number category.	78 = 2 x 3 x 13
Definition of H.C.F	2 <u>128</u> 2 64
The Highest Common Factor	2 32
The H.C.F of a given group of numbers is the highest number which will exactly divide all the numbers of that group.e.g.	$\begin{array}{c c} 2 & 16 \\ 2 & 8 \\ 2 & 4 \\ \hline 2 & 2 \end{array}$
To find the H.C.F of the numbers 24, 72, 100 24 = 2 x 2 x 2 x 3	$128 = 2 \times 2$
72 = 2 x 2 x 2 x 3 x 3	2 196
$100 = 2 \times 2 \times 5 \times 5$	2 <u>98</u> 49
The factors common to all the three numbers are	
2 x 2 = 4. So HCF = 4.	196 = 2 x 2 x 49
Definition of L.C.M	HCF = 2
Lowest common multiple	• Find LCM of 84,92,76
The lowest common multiple of a group of numbers is the smallest number that will contain each number of the given group without a remainder.e.g.	LCM = 2 84, 92, 76 2 42, 46, 38 3 21, 23, 19
Factorise the following numbers	7, 23, 19
7,17,20,66,128	LCM = 2 x 2 x 3 x 7 x 23 x 19 = 36708
7,17 - These two belong to Prime numbers. Hence no factor except unity and itself.	• To find out the LCM of 36, 108, 60
2 20 2 10 5	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Factors of $20 = 2 \times 2 \times 5$	1, 3, 5
2 66	LCM of the number
3 <u>33</u> 11	36, 108, 60 = 2 x 2 x 3 x 3 x 3 x 5 = 540
Factors of $66 = 2 \times 3 \times 11$	The necessity of finding LCM and HCF arises in subtraction and addition of fractions.

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.1.05 Unit, Fractions - Fractions - Addition, subtraction, multiplication & division

Description

A minimal quantity that is not a whole number. For e.g. .

 $\frac{1}{5}$ a vulgur fraction consists of a numerator and denominator.

Numerator/Denominator

The number above the line in a vulgar fraction showing how many of the parts indicated by the denominator are taken is the numerator. The total number of parts into which the whole quantity is divided and written below the line in a vulgar fraction is the denominator. e.g.

4 4 12

1,3,7 - numerators

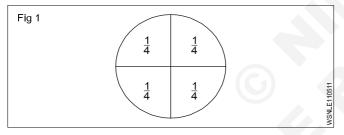
4,12-denominators

Fraction: Concept

Every number can be represented as a fraction.e.g.

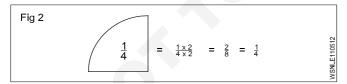
 $1\frac{1}{4} = \frac{5}{4}$, A full number can be represented as an apparent fraction e.g. (Fig.1)

fraction.e.g. (Fig 1)



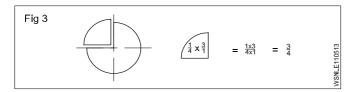
Fraction: Value

The value of a fraction remains the same if the numerator and denominator of the fraction are multiplied or divided by the same number.(Fig 2)



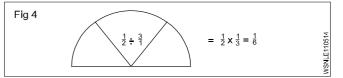
Multiplication

When fractions are to be multiplied, multiply all the numerators to get the numerator of the product and multiply all the denominators to form the denominator of the product. (Fig 3)



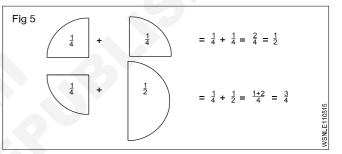
Division

When a fraction is divided by another fraction the dividend is multiplied by the reciprocal of the divisor. (Fig 4)



Addition and Subtraction

The denominators of the fractions should be the same when adding or subtracting the fractions. Unequal denominators must first be formed into a common denominator. It is the lowest common denominator and it is equal to the product of the most common prime numbers of the denominators of the fractions in question. (Fig 5)



Examples

Multiply
$$\frac{3}{4}$$
 by $\frac{2}{3}$,
 $\frac{3}{4} \times \frac{2}{3} = \frac{6}{12} = \frac{1}{2}$
Divide $\frac{3}{2}$ by $\frac{3}{2}$.

$$\frac{3}{8} \div \frac{3}{4} = \frac{3}{8} \times \frac{4}{3} = \frac{3}{2}$$

Add
$$\frac{3}{4}$$
 and $\frac{2}{3}$,

$$\frac{3}{4} + \frac{2}{3} = \frac{9}{12} + \frac{8}{12} = \frac{17}{12} = 1\frac{5}{12}$$

$$sub \frac{7}{16} \text{ from } \frac{17}{32}$$
$$\frac{17}{32} - \frac{7}{16} = \frac{17}{32} - \frac{14}{32} = \frac{(17 - 14)}{32} = \frac{3}{32}$$

Types of fractions

- Proper fractions are less than unity. Improper fractions have their numerators greater than the denominators.
- A mixed number has a full number and a fraction.

Addition of fraction

 $Add\frac{1}{2}+\frac{1}{8}+\frac{5}{12}$

To add these fractions we have to find out L.C.M of denominators 2,8,12.

Find L.C.M of 2,8,12

Step 1 L.C.M

2 2,8,12 2 1,4,6 1,2,3

Factors are 2,2,2,3

Hence L.C.M = 2 x 2 x 2 x 3 = 24 Step 2

 $\frac{1}{2} + \frac{1}{8} + \frac{5}{12} = \frac{12}{24} + \frac{3}{24} + \frac{10}{24}$ $= \frac{12 + 3 + 10}{24} = \frac{25}{24} = 1\frac{1}{24}.$

Subtraction of fraction

subtract $9\frac{15}{32}$ from $17\frac{9}{16}$ or $(17\frac{9}{16}-9\frac{15}{32})$ Step 1: Subtract whole number first 17 - 9 = 8Step 2: L.C.M of 16,32 = 32Since number 16 divides the number 32

Subtracting fractions = $\frac{3}{32}$

Adding with whole number from Step 1

we get $8 + \frac{3}{32} = 8\frac{3}{32}$

Common fractions

Problems with plus and minus sign

Example

solve $3\frac{3}{4} + 6\frac{7}{8} - 4\frac{5}{16} - \frac{9}{32}$

Rule to be followed

- 1 Add all whole numbers
- 2 add all + Numbers
- 3 Add all Numbers
- 4 Find L.C.M of all denominators

Solution

Step 1: Add whole numbers = 3 + 6 - 4 = 5

Step 2: Add fractions =
$$\frac{3}{4} + \frac{7}{8} - \frac{5}{16} - \frac{9}{32}$$

L.C.M of 4,8,16,32 is 32

$$\frac{24 + 28 - 10 - 9}{32}$$
$$= \frac{52 - 19}{32}$$
$$= \frac{33}{32} = 1\frac{1}{32}$$

Step 3: Adding again with the whole number

we get
$$5 + 1\frac{3}{32} = 6\frac{3}{32}$$

Examples

Common fractions

Multiply

	3 hu	, 4	3	4	3	L.	2	3	5	
а	$\frac{3}{8}$ by	7	8	7	14	D				16

Division

a
$$\frac{5}{16} \div \frac{5}{32} = \frac{5}{16} \times \frac{32}{5} = 2$$

b $4\frac{2}{3} \div 3\frac{1}{7} = \frac{14}{3} \div \frac{22}{7} = \frac{14}{3} \times \frac{7}{22} = \frac{49}{33} = 1\frac{16}{33}$

Addition

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8}$$

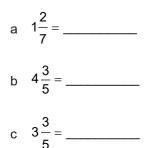
L...C.M = 2,4,8 = 8
$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} = \frac{4+2+1}{8} = \frac{7}{8}$$

Subtraction

$$5\frac{1}{4} - 3\frac{3}{4} = 5 - 3 + \frac{1}{4} - \frac{3}{4}$$
$$= 2 + \frac{1}{4} - \frac{3}{4} = 2\frac{1}{4} - \frac{3}{4}$$
$$= \frac{9}{4} - \frac{3}{4} = \frac{9 - 3}{4}$$
$$= \frac{6}{4} = \frac{3}{2} = 1\frac{1}{2}$$

Assignment

1 Convert the following into improper fractions.



2 Convert the following into mixed numbers.

a
$$\frac{12}{11} =$$

b $\frac{36}{14} =$ _____

c
$$\frac{18}{10} =$$

3 Place the missing numbers.

a
$$\frac{11}{13} = \frac{x}{91}$$

b
$$\frac{3}{5} = \frac{42}{x}$$

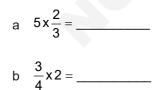
$$c \quad \frac{9}{14} = \frac{x}{98}$$

4 Simplify.

a
$$\frac{45}{60} =$$

$$b \frac{8}{12}$$

5 Multiply.



c
$$\frac{3}{4}x\frac{5}{6} =$$

6 Divide

a
$$\frac{1}{4} \div \frac{3}{4} =$$

b
$$6 \div \frac{3}{4} =$$

- $\begin{array}{c} c & -\frac{1}{4} \cdot \frac{1}{7} = -----$
- 7 Place the missing numbers.

c
$$\frac{7}{8} = \frac{1}{12}$$
 x_____

8 Add the followings:

a
$$\frac{3}{4} + \frac{7}{12} =$$

$$7 + \frac{3}{8} + \frac{3}{4} =$$

9 Subtract

a
$$\frac{4}{5} - \frac{2}{5} =$$

b
$$\frac{5}{6} - \frac{3}{4} =$$

a
$$2\frac{6}{7} - \frac{3}{8} - \frac{1}{3} - 1\frac{1}{16} =$$

b
$$2\frac{2}{7}-\frac{5}{6}+8=$$

11 Express as improper fractions

a
$$5\frac{3}{4}$$

b $3\frac{5}{64}$

. 12

Description

Decimal fraction is a fraction whose denominator is 10 or powers of 10 or multiples of 10 (i.e.) 10, 100, 1000, 10000 etc. Meaning of a decimal number:-

12.3256 means

 $(1 \times 10) + (2 \times 1) + \frac{3}{10} + \frac{2}{100} + \frac{5}{1000} + \frac{6}{10000}$

Representation

The denominator is omitted. A decimal point is placed at different positions of the number corresponding to the magnitude of the denominator

$$Ex.\frac{5}{10} = 0.5, \frac{35}{100} = 0.35 \frac{127}{10000} = 0.0127, \frac{3648}{1000} = 3.648$$

Addition and subtraction

Arrange the decimal fractions in a vertical order, placing the decimal point of each fraction to be added or subtracted, in succession one below the other, so that all the decimal points are arranged in a straight line. Add or subtract as you would do for a whole number and place the decimal point in the answer below the column of decimal points.

Decimal fractions less than 1 are written with a zero before the decimal point. Example: 45/100 = 0.45 (and not simply .45)

Add 0.375 + 3.686

0.375
3.686
4.061

Subtract 18.72 from 22.61

22.61				
18.72				
3.89				

Multiplication

Ignore the decimal points and multiply as whole numbers. Find the total number of digits to the right of the decimal point. Insert the decimal point in the answer such that the number of digits to the right of the decimal point equals to the sum of the digits found to the right of the decimal points in the problem.

Multiply 2.5 by 1.25

= $25 \times 125 = 3125$. The sum of the figures to the right of decimal point is 3. Hence the answer is 3.125.

Division

Move the decimal point of the divisor to the right to make it a full number. Move the decimal point in the dividend to the same number of places, adding zeroes if necessary. Then divide.

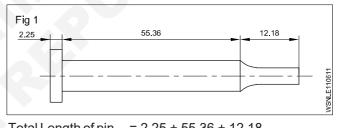
Divide 0.75 by 0.25

$$0.25\overline{\smash{\big)}0.75}$$
$$\frac{0.75}{0.25} \times \frac{100}{100} = \frac{75}{25}$$
$$25\overline{)75} = 3$$

Move the decimal point in the multiplicand to the right to one place if the multiplier is 10, and to two places if the multiplier is 100 and so on. When dividing by 10 move the decimal point one place to the left, and, if it is by 100, move them point by two places and so on.

Example

Allowance allowing 3 mm for cutting off each pin, how many pins can be made from a 900 mm long bar and how much material will be left out?



I otal Length of pin	= 2.25 + 55.36 + 12.18
	= 69.79 mm
Cutting allowance	= 3 mm
Total Length	= length of pin + cutting allowance
	= 69.79 mm + 3 mm
	= 72.79 mm
Length of the bar	= 900 mm
No.of pins to be cut	$=\frac{900}{72.79}=12.394$
	= 12 pins
Left out material	= Total length - length of pin + cutting allowance
	= 900 - 12 x 69.79 + 12 x 3
	= 900 - 837.48 + 36
	= 900 - 873.48
Left out length	= 26.52 mm

Conversion of Decimals into fractions and vice-versa

Convert decimal into fractions

Example

Convert 0.375 to a fraction

Now place 1 under the decimal point followed by as many zeros as there are numbers

$$0.375 = \frac{375}{1000} = \frac{15}{40} = \frac{3}{8}$$
$$0.375 = \frac{3}{8}$$

Convert fraction into decimal

Example

• Convert $\frac{9}{16}$ to a decimal

Proceed to divide $\frac{9}{16}$ in the normal way of division but put zeros (as required) after the number 9 (Numerator)

16	0.5625)90000	
	80	
	100	
	96	
	40	
	32	
	80	
	80	
	0	
0	_	

$$\frac{9}{16} = 0.5625$$

Recurring decimals

While converting from fraction to decimals, some fractions can be divided exactly into a decimal. In some fractions the quotient will not stop. It will continue and keep recurring. These are called recurring decimals.

Examples

convert
$$\frac{1}{3}, \frac{2}{3}, \frac{1}{7}$$

a $\frac{1}{3} = \frac{10000}{3} = 0.3333 - \text{Recurring}$
b $\frac{2}{3} = \frac{20000}{3} = 0.666 - \text{Recurring}$
c $\left(\frac{1}{7} = \frac{10000}{7} = 0.142857142 - \text{Recurring}\right)$

Method of writing approximations in decimals

1.73556= 1.7356Correct to 4 decimal places5.7343= 5.734Correct to 3 decimal places0.9345= 0.94Correct to 2 decimal places

Multiplication and division by 10,100,1000

Multiplying decimals by 10

A decimal fraction can be multiplied by 10,100,1000 and so on by moving the decimal point to the right by as many places as there are zeros in the multiplier.

- 4.645×10 = 46.45 (one place)
- 4.645 x 100 = 464.5 (two places)
- 4.645 x 1000 = 4645 (three places)

Dividing decimals by 10

A decimal fraction can be divided by 10,100,1000 and so on, by moving the decimal point to the left by as many places as required in the divisor by putting zeros

Examples

- $3.732 \div 10 = 0.3732$ (one place)
- 3.732 ÷ 100 = 0.03732 (two places)
- 3.732 ÷ 1000 = 0.003732 (three places)

Examples

 Rewrite the following number as a fraction 453.273

$$= (4 \times 100) + (5 \times 10) + (3 \times 1) + \frac{2}{10} + \frac{7}{100} + \frac{3}{100}$$
$$= 453 \frac{273}{1000}$$

- Write the representation of decimal places in the given number 0.386
 - 3 Ist decimal place

8 - IInd decimal place

6 - Illrd decimal place

- Write approximations in the following decimals to 3 places.
 - a 6.9453 ----> 6.945
 - b 8.7456 ----> 8.746
- Convert fraction to decimal

$$\frac{21}{24} = \frac{7}{8} = 0.875$$

· Convert decimal to fraction

$$0.0625 = \frac{625}{10000} = \frac{5}{80} = \frac{1}{16}$$

Assignment

- 1 Write down the following decimal numbers in the expanded form.
 - a 514.726
 - b 902.524
- 2 Write the following decimal numbers from the expansion.

а	500 + 70 + 5	3	2	9
a	500 + 70 + 5			1000
Ŀ	200 + 9 +	3	5	
b	200 + 9 +		1000)

- 3 Convert the following decimals into fractions in the simplest form.
 - a 0.72
 - b 5.45
 - c 3.64
 - d 2.05
- 4 Convert the following fraction into decimals

а	$\frac{3}{5}$
b	<u>10</u> 4
с	$24 \frac{54}{1000}$
d	12

- $e \frac{8}{25}$
- f $1\frac{3}{25}$
- 5 Addition of decimals
 - a 4.56 + 32.075 + 256.6245 + 15.0358
 - b 462.492 + 725.526 + 309.345 + 626.602
- 6 Subtract the following decimals
 - a 612.5200 9.6479
 - b 573.9246 -215.6000
- 7 Add and subtract the following
 - a 56.725 + 48.258 32.564
 - b 16.45 + 124.56 + 62.7 3.243

- 8 Multiply the following
 - a By 10, 100, 1000
 - i 3.754 x 10
 - ii 8.964 x 100
 - iii 2.3786 x 1000
 - iv 0.005 x 1000
 - b By whole numbers
 - i 8.4 x 7
 - ii 56.72 x 8
 - c By another decimal figure (use calculator)
 - i 15.64 x 7.68
 - ii 2.642 x 1.562
- 9 Divide the following
- 62.5 а 25 64.56 10 0.42 100 48.356 1000 10 Division 16.8 а 1.2 1.54 b 1.1
- 11 Change the fraction into a decimal
 - i $1\frac{5}{8}$ ii $\frac{12}{25}$
- 12 Find the value

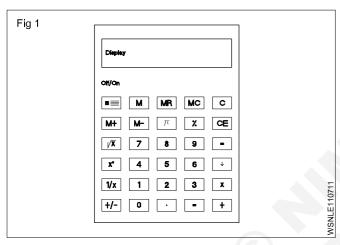
20.5 x 40 ÷ 10.25 + 18.50

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.1.07 Unit, Fractions - Solving problems by using calculator

A pocket calculator allows to spend less time in doing tedious calculations. A simple pocket calculator enables to do the arithmetical calculations of addition, subtraction, multiplication and division, while a scientific type of calculator can be used for scientific and technical calculations also.

No special training is required to use a calculator. But it is suggested that a careful study of the operation manual of the type of the calculator is essential to become familiar with its capabilities. A calculator does not think and do. It is left to the operator to understand the problem, interpret the information and key it into the calculator correctly.

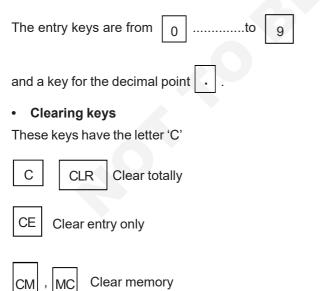
Addition key + _ Subtraction key х Multiplication key **Division key** ÷ Equals key to display the result = **Function keys**



The key board is divided into five clear and easily recognizable areas and the display.

Data entry keys

CM



Pi key π $\int x$ Square root key Percentage key % Sign change key +/-Square key X² 1 Reciprocal key X Memory keys Store the display number Μ



The displayed value is added to the memory

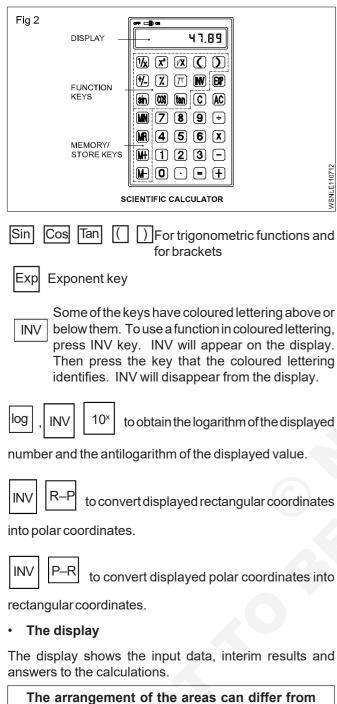
M-The displayed value is subtracted from the memory

MR RCL

The stored value is recalled on to the display

Constructional Details (Fig 1)

Further functional keys included in Scientific calculators are as shown in Fig 2.



one make to another. Keying in of the numbers is done via. an internationally agreed upon set of ten keys in the order that the numbers are written. Rules and Examples:

• Addition: Example 18.2 + 5.7

Sequence	Input	Display
Input of the 1st term of the sum	18.2	18.2
Press + key	+	18.2
Input 2nd term of the sum. the first term goes into the register	5.7	5.7
Press the = key	Ξ	23.9

• Subtraction: Example 128.8 - 92.9

Sequence	Input	Display
Enter the subtrahend	128.8	128.8
Press - key	-	128.8
Enter the minuend. The subtrahend goes into the register	92.9	92.9
Press the = key	Ξ	35.9

• Multiplication: Example 0.47 x 2.47

Sequence	Input	Display			
Enter multiplicand	. 4 7	0.47			
Press x key	X	0.47			
Enter multiplier, multiplicand goes to register	2.47	2.47			
Press = key	=	1.1609			

• Division: Example 18.5/2.5

Sequence	Input	Display
Enter the dividend	18.5	18.5
Press ÷ Key	÷	18.5
Enter the divisor goes to the register Press = key	2.5	2.5 7.4

• Multiplication & Division: Example : 2.5 x 7.2 / 4.8 x 1.25

Sequence	Input	Display
Enter 2.5	2.5	2.5
Press x key	x	2.5
Enter 7.2	7.2	7.2
Press ÷ key	÷	18
Enter Open bracket	(
Enter 4.8	4.8	4.8
Press x key	x	4.8
Enter 1.25	1.25	1.25
Enter Close bracket)	6
Press = key	=	3.0

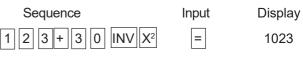
• Store in memory Example (2+6) (4+3)

Sequence	Input	Display
Workout for the first bracket	2	2
DIACKEL	+	2
	6	6
	=	8
Store the first result in	STO, M	8
х	or M+	
Workout for the 2nd bracket	4	4
	+	4
	3	3
	=	7
Press x key	x	7
Recall memory	RCL or MR	8
Press = key	=	56

- Percentage: Example 12% of 1500
- Sequence Input Display 1 5 0 0 Enter 1500 1500 x 1500 Press x key 1 2 Enter 12 12 INV % Press INV % 12 = Press = key 180
 - Square root: Example $\sqrt{2} + \sqrt{3 \times 5}$

Sequence	Input	Display
Enter 2	2	2
Press√a key	\sqrt{a}	1.414
Press + key	+	1.414
Press bracket key	(1.414
Enter 3	3	3
Press √a key	\sqrt{a}	1.732
Press x key	x	1.732
Enter 5	5	5
Press √a key	\sqrt{a}	2.236
Press bracket close key)	3.873
Press = key	=	5.2871969
2 √ + (3 √ x 5) () =	5.2871969
$\sqrt{2} + \sqrt{3 \times 5} = 5.287$		

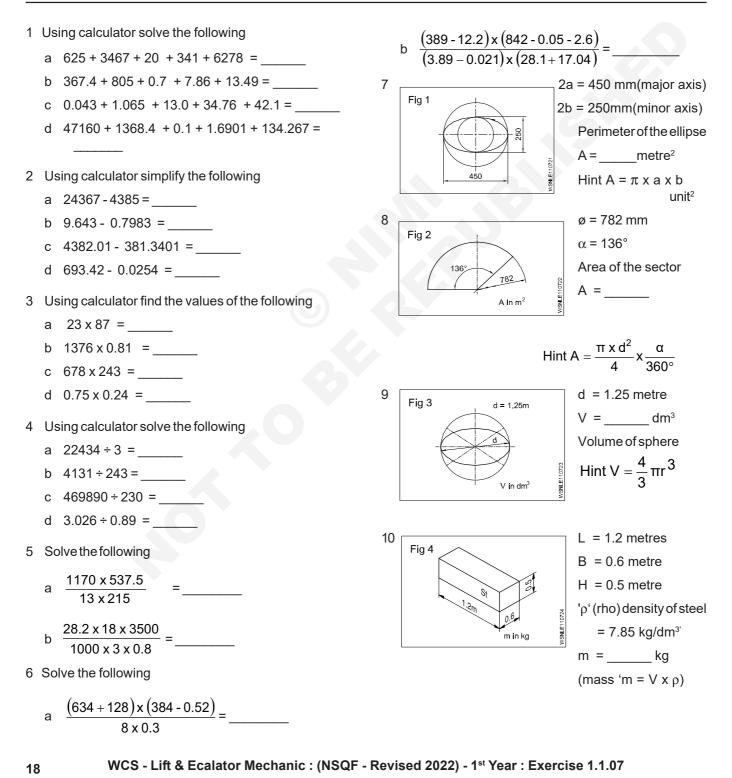
- Common logarithm: Example log 1.23
 Sequence Input Display
 I . 2 3 log = 0.0899051
- **Power:** Example 123 + 30²



- Before starting the calculations be sure to press the 'ON' key and confirm that '0' is shown on the display.
- Do not touch the inside portion of the calculator. Avoid hard knocks and unduly hard pressing of the keys.
- Maintain and use the calculator in between the two extreme temperatures of 0° and 40° C.

Assignment

- Never use volatile fluids such as lacquer, thinner, benzine while cleaning the unit.
- Take special care not to damage the unit by bending or dropping.
- Do not carry the calculator in your hip pocket.



Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.08 Square root, Ratio and Proportions, Percentage - Square and square root

- a basic number
- 2 exponent
- $\sqrt{}$ radial sign indicating the square root.

 $\sqrt{a^2}$ square root of 'a' square

a² radicand

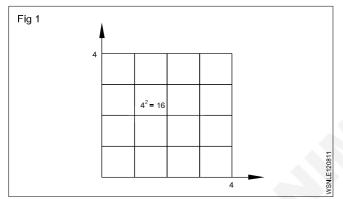
Square number

The square of a number is the number multiplied by itself.

Basic number x basic number = Square number

 $a x a = a^2$

 $4 \times 4 = 4^2 = 16$



Splitting up

A square area can be split up into sub-areas. The largest square of 36 is made up of a large square 16, a small square 4 and two rectangles 8 each.

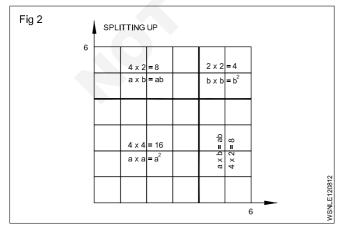
Large square $4 \times 4 = 16$ a^2

Two rectangles $2 \times 4 \times 2 = 16$ 2ab

Small square 2 x 2 = 4 b^2

Sum of sub-areas = $36 = a^2 + 2ab + b^2$

$$\sqrt{36} = \sqrt{a^2 + 2ab + b^2}$$



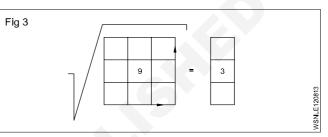
Result: In order to find the square root, we split up the square numbers.

Extracting the square root procedure

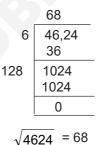
Starting from the decimal point form groups of two figures towards right and left. Indicate by a prime symbol. $\sqrt{4624.00}$

Find the root of the first group, calculate the difference, bring down the next group.

- Multiply the root by 2 and divide the partial radicand.
- Enter the number thus calculated in the divisor for the multiplication.



If there is a remainder, repeat the procedure.

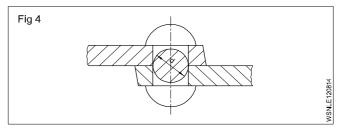


Basic number x basic number = Square

 $\sqrt{\text{Square number}} = \text{basic number}$

Example

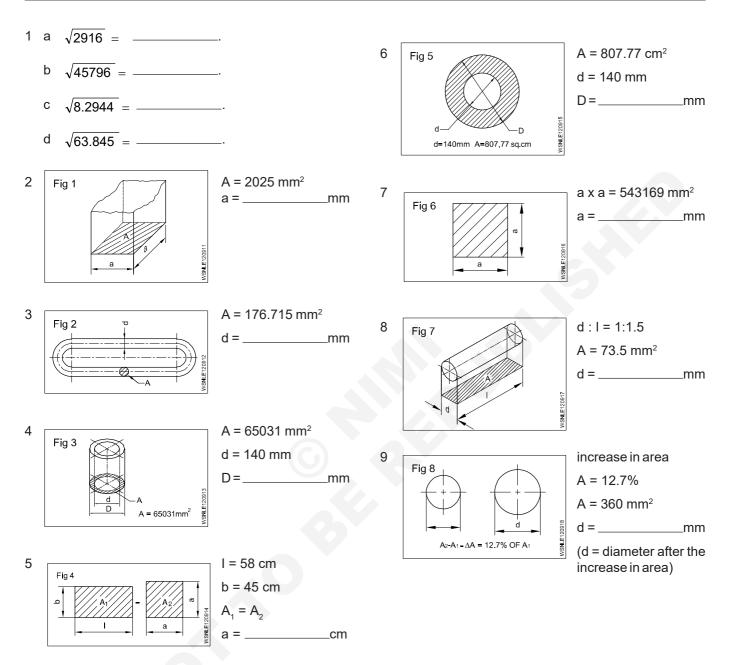
The cross-section of a rivet is 3.46 cm^2 . Calculate the diameter of the hole.



Rivet cross-section is the hole cross-section. To find 'd'.

Given that Area = 3.46 cm^2 Area = $0.785 \text{ x} d^2$ (formula) $3.46 \text{ cm}^2 = d^2 \text{ x} 0.785$ $d^{2} = \frac{3.46 \text{ cm}^{2}}{0.785}$ $d = \sqrt{\frac{3.46}{0.785}} \text{ cm}$ d = 2.1 cm (or) 21 mm

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.09 Square root, Ratio and Proportions, Percentage - Simple problems using calculator

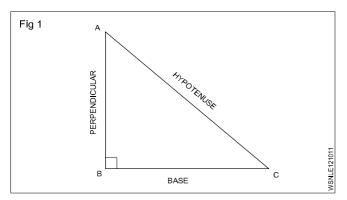


Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.10 Square root, Ratio and Proportions, Percentage - Applications of pythagoras

theorem and related problems

Applications of Pythagoras Theorem

Some of the applications of the Pythagoras theorem are; (Fig 1)



- 1 The Pythagoras theorem is commonly used to find the lengths of sides of a right-angled triangle.
- 2 It is used to find the length of the diagonal of a square.
- 3 Pythagoras theorem is used in trigonometry to find the trigonometric ratios like sin, cos, tan, cosec, sec and cot.
- 4 Pythagoras theorem is used in security cameras for face recognition.
- 5 Architects use the technique of the Pythagoras theorem for engineering and construction fields.
- 6 The Pythagoras theorem is applied in surveying the mountains.
- 7 It is also used in navigation to find the shortest route.
- 8 By using the Pythagoras theorem, we can derive the formula for base, perpendicular and hypotenuse.
- 9 Painters use ladders to paint on high buildings with the help of the Pythagoras theorem.
- 10 Pythagoras theorem is used to calculate the steepness of slopes of hills or mountains.
- 11 The converse of the Pythagoras theorem is used to check whether a triangle is a right triangle or not.

Application of pythagoras theorem in real life

Pythagoras theorem states that

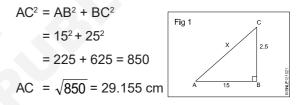
"In a right-angled triangle, the square of the hypotenuse side is equal to the sum of squares of the other two sides".

- 1 The sides of this triangle have been named Perpendicular, Base and Hypotenuse.
- 2 The hypotenuse is the longest side, as it is opposite to the angle 90°.

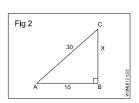
- 3 The sides of a right triangle (say AB, BC and CA) which have positive integer values, when squared, are put into an equation, also called a Pythagorean triplet.
- 4 To calculate the length of staircase required to reach a window
- 5 To find the length of the longest item can be kept in your room.
- 6 To find the steepness of the hills or mountains.
- 7 To find the original height of a tree broken due to heavy rain and lying on itself
- 8 To determine heights and measurements in the construction sites.

Examples

1 What is the side AC if AB = 15 cm, BC = 25 cm.

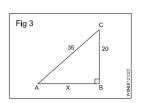


- 2 What is the side BC if AB = 10 cm, AC = 30 cm.
 - $AC^{2} = AB^{2} + BC^{2}$ $30^{2} = 10^{2} + BC^{2}$ $900 = 100 + BC^{2}$ $BC^{2} = 900 - 100 = 800$ BC = 28.284 cm



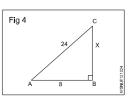
3 What is the side AB if BC = 20 cm, AC = 35 cm.

 $AC^{2} = AB^{2} + BC^{2}$ $35^{2} = AB^{2} + 20^{2}$ 1225 = AB + 400 $AB^{2} = 1225 - 400 = 825$ AB = 28.72 cm

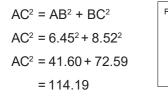


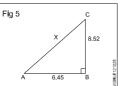
4 What is the value of side BC if AB = 8 cm, AC = 24 cm.

 $AC^{2} = AB^{2} + BC^{2}$ $24^{2} = 8^{2} + BC^{2}$ $576 = 64 + BC^{2}$ $BC^{2} = 576 - 64 = 512$ $BC = \sqrt{572} = 22.63 \text{ cm}$

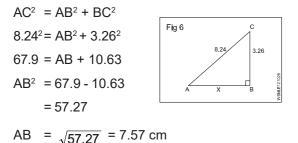


5 What is the value side AC if AB = 6.45 cm, BC = 8.52 cm.

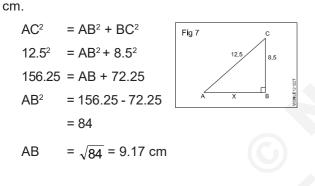




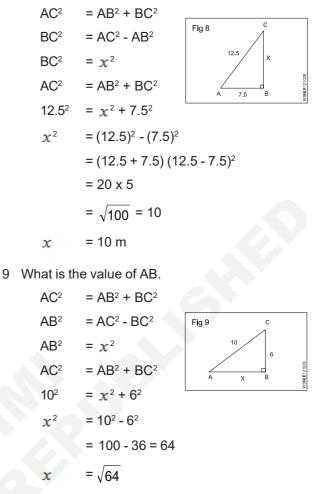
- AC = $\sqrt{114.19}$ = 10.69 cm
- 6 What is the value of side AB if BC = 3.26 cm, AC = 8.24 cm.



7 What is the value of side AB if AC = 12.5 cm, BC = 8.5



8 A ladder of 12.5 metre long is placed with upper end against a wall. The lower end being 7.5 metres from the wall. What height is the upper end above the ground.



Assignment

- 1 What is the value of side AB, in a right angled triangle of side AC = 10 cm and BC = 5 cm.
- 2 What is the value of side AC, in a right angled triangle of side AB = 6.5 cm and BC = 4.5 cm.
- 3 What is the value of side BC, in a right angled triangle of side AC = 14.5 cm and AB = 10.5 cm.
- 4 What is the value of side AC, in a right angled triangle of side AB = 7 cm and BC = 5 cm.

= 8

= 8

AB

5 What is the value of side BC, in a right angled triangle of side AC = 13.25 cm and AB = 8.75 cm.

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.11 Square root, Ratio and Proportions, Percentage - Ratio and proportion

Ratio

Introduction

It is the relation between two quantities of the same kind and is expressed as a fraction.

Expression

a, b two quantities of the same kind. $\frac{a}{b}$ or a:b or a \div b or

a in b is the ratio.

Ratio is always reduced to the lowest terms.

Example

$$7:14 = \frac{7}{14} = \frac{1}{2} = 1:2$$

Proportion

It is the equality between the ratios, a : b is a ratio and c: d is another ratio. Both ratios are equal. Then

a :b :: c : d or
$$\frac{a}{b} = \frac{c}{d}$$

Example

250 : 2000 :: 1 : 8

Proportion fundamentals

- If $\frac{a}{b} = \frac{c}{d}$ then
- ad = bc
- $\cdot \frac{a}{c} = \frac{b}{d}$
- $\cdot \frac{b}{a} = \frac{d}{c}$
- $\frac{a+b}{b} = \frac{c+d}{c}$ and $\frac{a+b}{a} = \frac{c+d}{c}$
- $\frac{a-b}{b} = \frac{c-d}{d}$
- $\frac{a+b}{b+d} = \frac{a}{c} = \frac{c}{d}$

3:4::6:8 or $\frac{3}{4} = \frac{6}{8}$

• 3 x 8 = 6 x 4

$$\overline{6} = \overline{8}$$

$$\frac{4}{3} = \frac{8}{6}$$

$$\frac{3+4}{4} = \frac{6+8}{8}$$

$$\frac{3-4}{4} = \frac{6-8}{8}$$

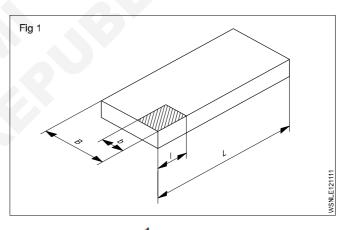
$$\frac{3+6}{4+8} = \frac{9}{12} = \frac{3}{4}$$

3 4

Ratio - relation of two quantities of the same kind. Proportion - equality between two ratios.

Example

• A steel plate of 800 x 1400 mm is to be drawn to a scale of 1:20. What will be the lengths in the Fig 1.

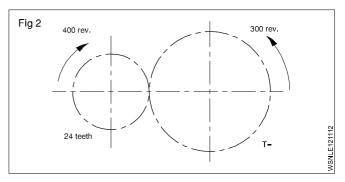


The reduction ratio is $\frac{1}{20}$.

B is reduced from 800 to 800 x $\frac{1}{20}$ = 40 mm.

L is reduced from 1400 x $\frac{1}{20}$ = 70 mm.

 Find the number of teeth of the larger gear in the gear transmission shown in the Fig 2.



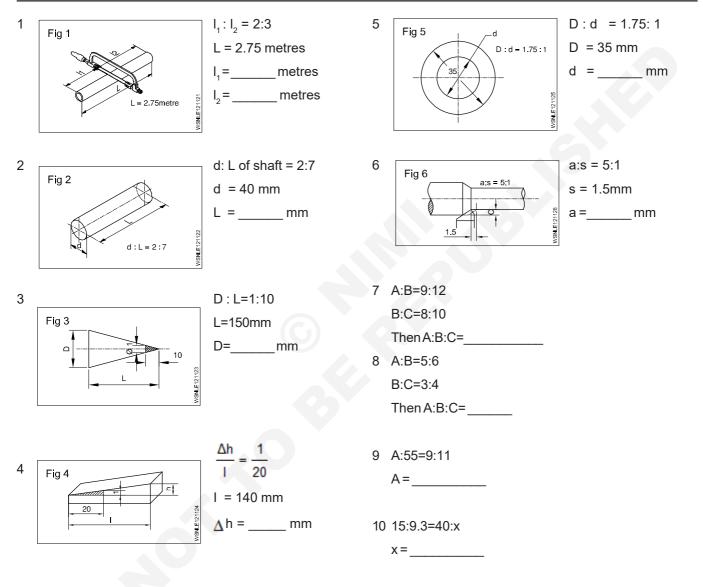
Speed ratio = 400 : 300
Teeth ratio = 24:T

$$\frac{400}{300} = \frac{T}{24}$$

$$\therefore T = \frac{24 \times 400}{300} = 32 \text{ Teeth}$$

Find the ratio of A:B:C If A:B= 2:3 and B:C=4:5 A:B = 2:3 B:C = 4:5 A:B = 8 :12 (Ratio 2:3 multiply by 4) B:C = 12:15 (Ratio 4:5 multiply by 3) ∴ A:B:C = 8:12:15

Assignment



Square root, Ratio and Proportions, Percentage - Ratio and Proportion - Direct and indirect proportions

Proportion

Description

It is the equality between the ratios, a:b is a ratio and c:d is another ratio. Both ratios are equal. Then

a : b::c : d or e.g. 250 : 2000::1 : 8

Rule of three

A three step calculation

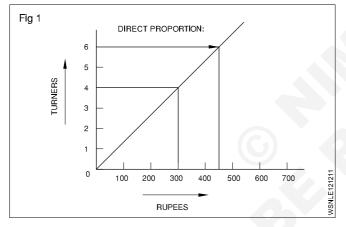
statement

single

multiple.

Direct proportion

The more in one the more in the other - An increase in one denomination produces an increase in the other. (Fig 1)



Examples

1 4 turners earn 300 Rupees. How much will 6 Turners earn?

Statement

4 turners = 300 Rupees

Single

1 Turner = 75 Rupees

Multiple 6 Turners = 6 x 75 = 450 Rupees

2 One vehicle consumes 30 litres of petrol per day how much petrol is used by 6 Vehicles operating under similar condition.

One vehicle uses petrol = 30 litres per day.

Then six vehicles will use = 6 Times as much

= 6 x 30 = 180 litres/day.

3 4 vehicles consumes 120 gallons of petrol per day how much petrol will be used by 12 vehicles operating under the same condition.

4 vehicles use 120 gallons per day

1 Vehicle will use $\frac{120}{4}$ = 30 gallons/day

12 vehicles will use 12 x 30 = 360 gallons/day

Both examples are called simple proportion because only two quantities were used and the day is common for both ratios.

4 If 2 litres of petrol costs Rs 60. Find the cost of 50 litres.

Quantity of Petrol	Cost of Petrol
2 litres	Rs.60
50 litres	x
1 litre petrol	$=\frac{60}{2}$ = Rs.30
50 litres petrol	= 30 x 50 = Rs 1500

5 A 150mm dia gear meshes with 50mm dia gear. If the larger gear has 30 teeth. How many teeth will have the smaller gear have?

Geardia	No. of Teeth	
150 mm	30	
50 mm	x	
$x = \frac{50}{150} \times 30 = 10$ teeth.		

6 A mechanic assembles 7 machines in 2½ days. How long will it take time to assemble 70 machines at the same rate.

Machines Days
7
$$2\frac{1}{2}$$

70 x
 $x = \frac{70 \times 2.5}{7} = 25$ days

Assemble for 70 machines will take 25 days.

7 A roll of wire weighs 1.24 kg from this roll a piece of 3.7cm long is cut and it is found to weigh 2.93 gm. What is the length of the wire in the roll?

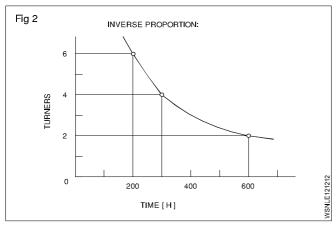
Weight of wire	Length of wire
2.93 gm	3.7 cm
1.24 kg (1240 gm)	x

$$x = \frac{1240}{2.93} \times 3.7 = 1566 \text{ cm}$$

Length of wire = 1566 cm.

Indirect or inverse proportion

The more in one the lesser other - Increase in one quantity will produce a decrease in the other. (Fig 2)



Example

1 4 turners finish a job in 300 hours. How much time will 6 turners take to do the same job?

Solution procedure in three steps:

Statement 4 turners taken = 300 hours

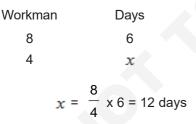
The time will reduce if 6 turners to do the same job. Therefore this is inverse proportion.

Multiple fraction <u>4 Turners</u> x 300 hours

6 Turners = 200 hours

Result - The more the less.

2 8 workman take 6 days to complete a job. How many days it will take for 4 workman to complete the same job?



4 workers complete the work = 12 days.

3 5 men working on a job finished it in 32 days. Find out in how many days 8 men will finish the same job?

Men	Days
5	32
8	x

$$x = \frac{5 \times 32}{8} = 4 \times 5 = 20$$
 days

8 men will complete the job = 20 days.

4 An engine running at 150 rpm drives a shaft by pulley diameter is 55cm and that of the driven shaft pulley is 33 cm. Find the speed of the shaft?

Dia of pulley	Rpm of shaft
55 cm	150
33 cm	x
<i>x</i> =	$\frac{55 \times 150}{33}$ = 250 rpm.

Speed of the 33cm diameter will run 250 rpm.

5 A pulley of 80 cm diameter is rotating at 100 rpm and drives another pulley of 40 cm diameter. Find the rpm of driven pulley. If slip is 2.5% find the rpm?

Dia of pulley	Rpm of pulley
80 cm	100
40 cm	x
40 cm diameter	= 200 rpm.
Slip is 2.5%	= 195 rpm.

Problems involving both

Example

2 turners need 3 days to produce 20 pieces. How long will it take for 6 turners to produce 30 such pieces?

Statement

2 turners, 20 pieces = 3 days

6 turners, 30 pieces = how many days.

First step (Fig 3)

Statement 2 turners for 20 pieces = 3 days 1 turner for 20 pieces = 3 x 2 = 6 days

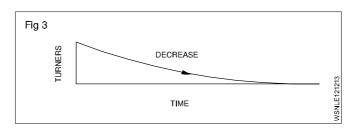
Multiple 6 turners for 20 pieces =
$$\frac{6}{6}$$
 = 1 day

Statement 6 turners for 20 pieces = 1 day

Single 6 turners for 1 piece = $\frac{1}{20}$ days

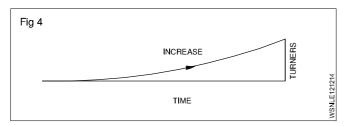
Multiple 6 turners for 30 pieces = $\frac{1}{20} \times 30 = 1.5$ days

Inverse proportion - More the less.



WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.2.12

Second step (Fig 4)



Direct proportion - More the more.

Solve the problem by first writing the statement and proceed to single and then to the multiple according to the type of proportion that is involved.

Introduction

Proportional fundamentals, as applicable to motor vehicle calculations are discussed below.

Simple Proportion

• Proportion

This is an equality between two ratios

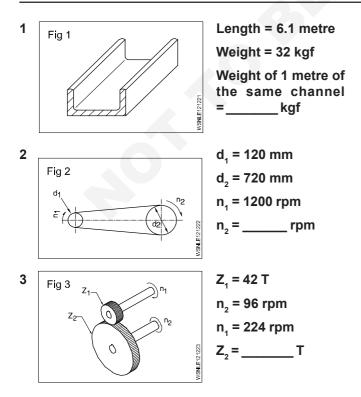
Compound and Inverse proportions

Compound proportions

Example

5 Fitter take 21 days to complete overhauling of 6 vehicles how long 7 Fitters will take to over haul 8 vehicles (Assume time of overhauling each vehicle is constant)

Assignment



In this both direct and indirect proportions are used.

- 1 Fitter will overhauling 1 vehicle in days (shorter time).
- Quantities (No. of days) are taken in last as that is the answer required in this case.

Fitters	Vehicle	Days
5	6	21
7	8	x
$\left(\frac{21\times5}{6\times7}\times8\right) =$	20 days	

Ans: 7 Fitters will overhaul 8 vehicles in 20 days.

Inverse proportion

Some times proportions are taken inversely.

Examples

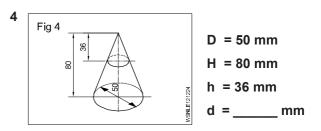
 If one water pump fills the fuel tank in 12 minutes, two pumps will take half the time taken.

The time should not be doubled.

2 pumps will take 30 minutes to fill up a tank how long will 6 similar pumps take this to fill this tank.

Pump	Time
2	30
6	x

Ans: Time taken by 6 pumps =
$$\frac{30 \times 2}{6}$$
 = 10 minutes



- 5 If a mechanic assembles 8 machines in 3 days, how long he will take to assemble 60 machines.
- 6 In an auto shop the grinding wheel makes 1000 rpm and the driven pulley is 200 mm dia. If the driving pulley is 150 mm dia. Find out the rpm of the driving pulley.
- 7 In a gearing of a vehicle the following facts are found.

A 180 mm dia of gear meshes with 60mm dia gear. If the bigger gear makes 60 rpm. What will be the rpm of smaller gear.

8 A vehicular job is completed by 5 mechanics in 4 days. If only 3 mechanics are available, in how many days the work can be completed.

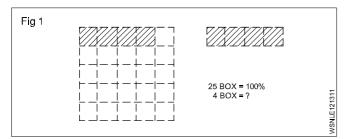
Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.13 Square root, Ratio and Proportions, Percentage - Percentage

Percentage

Percentage is a kind of fraction whose denominator is always 100. The symbol for percent is %, written after the number. e.g. 16%.

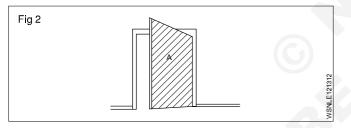
Ex.
$$\frac{16}{100} = 0.16$$

In decimal form, it is 0.16. Percentage calculation also involves rule of three. The statement (the given data), for unit, and then to multiple which is for calculating the answer. (Fig 1)



Example

The amount of total raw sheet metal to make a door was 3.6 metre² and wastage was 0.18 metre². Calculate the % of wastage. (Fig 2)



Solution procedure in three steps.

Statement:

Area of door (A) =3.6 m^2 = 100 %. Wastage = 0.18 m^2

Single:
$$\frac{100}{3.6} \times 1 \text{ m}^2$$

Multiple: for 0.18 m² =
$$\frac{100}{3.6} \times 0.18$$

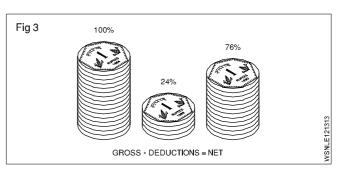
Wastage = 5%.

Analyse the given data and proceed to arrive at the answer through the unit.

Example

A fitter receives a take-home salary of 984.50 rupees.

If the deduction amounts to 24%, what is his total salary? (Fig 3)



Total pay 100%

Deduction 24%

Take home salary 76%

If the take home pay is Rs.76, his salary is 100.

For 1% it is
$$\frac{1}{76}$$

For Rs.984.50, it is $\frac{1}{76}$ x 984.50.

For 100% it is
$$\frac{984.50}{76}$$
 X100 = 1295.39

100% i.e. gross pay = Rs.1295.40.

Example 1

75 litres of oil is taken out from a oil barrel of 200 litres capacity. Find out the percentage taken in this.

Solution

% of oil taken = Oil taken out (litres) / Capacity of Barrel (litres) x 100

$$=\frac{75}{200} \times 100 = 37\frac{1}{2}\%$$

Example 2

A spare part is sold with 15%. Profit to a customer, to a price of Rs.15000/-. Find out the following (a) What is the purchase price (b) What is the profit.

Solution:
$$CP = x$$
,
 $CP = cost price$
 $SP = sale price$

SP=CP+15%of CP

$$15000 = x + \frac{15 x}{100} = \frac{100 x + 15 x}{100}$$

$$x = \frac{1500000}{115} = 13043.47$$

Profit = SP-CP = 15000-13043.47 = 1956.53

Purchase price = Rs.13,043/,Profit = Rs. 1957

Example 3

Out of 80000 cars, which were tested on road, only 16000 cars had no fault. What is the percentage in this acceptance.

$$= \frac{16000}{80000} \times 100 = \frac{100}{5} = 20\%$$

Example 4

The price of a motor cycle dropped to 92% of original price and now sold at Rs.18000/- What was the original price.

Solution

Present price of Motor cycle Rs.18000

This is the value of 92% of original price

Original Price = $18000 \times \frac{100}{92} = \frac{1800000}{92}$ = Rs.19565

Assignment

Example 5

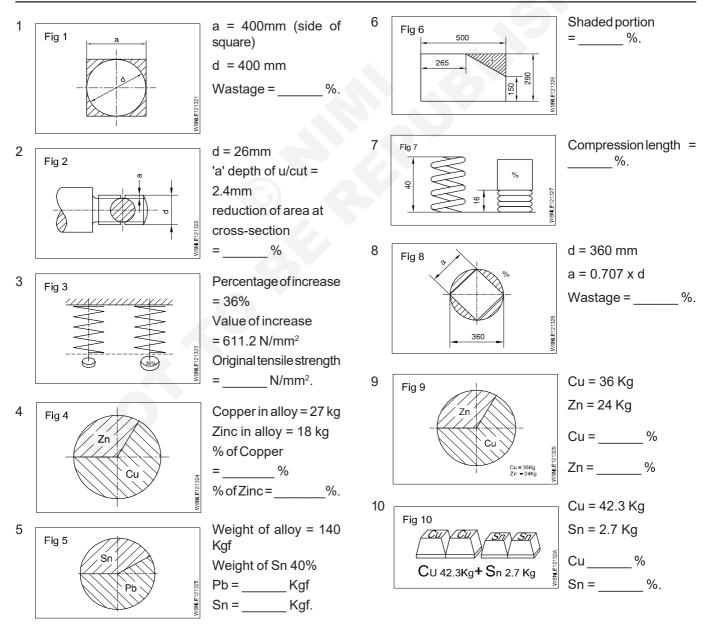
A Motor vehicle uses 100 litres of Petrol per day when travelling at 30 kmph. After top overhauling the consumption falls to 90 litres per day. Calculate percentage of saving.

Solution

Percentage of saving = Decrease in consumption/Original consumption x 100

$$=\frac{10}{100} \times 100$$

= 10% Saving in fuel.



WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.2.13

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.2.14

Square root, Ratio and Proportions, Percentage - Changing percentage to decimal and fraction

Conversion of Fraction into Percentage

1 Convert $\frac{1}{2}$ into percentage.

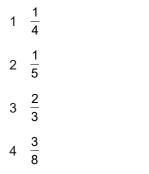
Solution: $\frac{1}{2} \times 100$ = 50%

2 Convert $\frac{1}{11}$ into percentage

Solution:
$$\frac{1}{11} \times 100 = \frac{100}{11}$$

= 9.01%

Convert the following fraction into percentage.



Conversion of Percentage into Fraction

1 Convert 24% into fraction.

Solution: $\frac{24}{100} = \frac{6}{25}$

2 Convert $33\frac{1}{3}$ % into fraction.

Solution:
$$\frac{33\frac{1}{3}}{100} = \frac{\frac{100}{3}}{100} = \frac{100}{3} \times \frac{1}{100}$$
$$= \frac{1}{3}$$

Convert the following percentage into fraction

- 1 15%
- 2 $87\frac{1}{2}\%$
- 3 80%
- 4 12.5%

Conversion of Decimal Fraction into Percentage

1 Convert 0.35 into percentage.

Solution: 0.35 x 100

= 35%

2 Convert 0.375 into percentage.

Solution: 0.375 x 100

= 37.5%

Convert the following Decimal Fraction into Percentage

- 1 0.2
- 2 0.004
- 3 0.875
- 4 0.052

Conversion of Percentage into Decimal fraction

1 Convert 30% into decimal fraction.

Solution:
$$\frac{30}{100} = 0.3$$

2 Convert $33\frac{1}{3}\%$ into decimal fraction.

Solution:
$$\frac{33\frac{1}{3}}{100} = \frac{\frac{100}{3}}{100} = \frac{100}{3} \times \frac{1}{100}$$

$$=\frac{1}{3}=0.333$$

Convert the following percentage into decimal fraction

- 1 15%
- 2 7%
- 3 $12\frac{1}{2}\%$
- 4 90%

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.3.15 Material science - Types of metal, types of ferrous and non ferrous metals

Types of metals

The metals is of two types:

1 Ferrous metal 2 Non-ferrous metal

1 Ferrous metals : The metals that contains major part of iron and contain carbon are called ferrous metals such as pig iron, mild steel, nickel etc., they have iron properties such as rusting, magnetisations etc.

2 Non-ferrous metals : The metals that do not contains iron or carbon and do not have the property of iron are called non-ferrous metals such as copper, aluminum etc.

Ferrous and Non ferrous alloys

Alloying metals and ferrous alloys

An alloy is formed by mixing two or more metals together by melting.

For ferrous metals and alloys, iron is the main constituent metal. Depending on the type and percentage of the alloying metal added, the property of the alloy steel will vary.

Metals commonly used for making alloy steels

Nickel (Ni)

This is a hard metal and is resistant to many types of corrosion rust.

It is used in industrial applications like nickel, cadmium batteries, boilertubes, valves of internal combustion engines, engine spark plugs etc. The melting point of nickel is 1450°C. Nickel can be magnetised. In the manufacture of permanent magnets a special nickel steel alloy is used. Nickel is also used for electroplating. Invar steel contains about 36% nickel. It is tough and corrosion resistant. Precision instruments are made of Invar steel because it has the least coefficient of expansion.

Nickel-steel alloys are available containing nickel from 2% to 50%.

Chromium (Cr)

Chromium, when added to steel, improves the corrosion resistance, toughness and hardenability of steel. Chromium steels are available which may contain chromium up to 30%.

Chromium, nickel, tungsten and molybdenum are alloyed for making automobile components and cutting tools.

Chromium is also used for electroplating components. Cylinder liners are chrome-plated inside so as to have wear resistance properties. Stainless steel contains about 13% chromium. Chromium-nickel steel is used for bearings. Chrome-vanadium steel is used for making hand tools like spanners and wrenches.

Manganese (Mn)

Addition of manganese to steel increases hardness and strength but decreases the cooling rate.

Manganese steel can be used to harden the outer surface for providing a wear resisting surface with a tough core. Manganese steel containing about 14% manganese is used for making agricultural equipment like ploughs and blades.

Silicon (Si)

Addition of silicon for alloying with steel improves resistance to high temperature oxidation.

This also improves elasticity, and resistance against corrosion. Silicon alloyed steels are used in manufacturing springs and certain types of steel, due to its resistance to corrosion. Cast iron contains silicon about 2.5%. It helps in the formation of free graphite which promotes the machinability of cast iron.

Tungsten (W)

The melting temperature of tungsten is 3380° C. This can be drawn into thin wires.

Due to this reason it is used to make filaments of electric lamps.

Tungsten is used as an alloying metal for the production of high speed cutting tools. High speed steel is an alloy of 18% tungsten, 4% chromium and 1% vanadium.

Stellite is an alloy of 30% chromium, 20% tungsten, 1 to 4% carbon and the balance cobalt.

Vanadium (Va)

This improves the toughness of steel. Vanadium steel is used in the manufacture of gears, tools etc. Vanadium helps in providing a fine grain structure in tool steels.

Chrome-vanadium steel contains 0.5% to 1.5% chromium, 0.15% to 0.3% vanadium, 0.13% to 1.10% carbon.

This alloy has high tensile strength, elastic limit and ductility. It is used in the manufacture of springs, gears, shafts and drop forged components.

Vanadium high speed steel contains 0.70% carbon and about 10% vanadium. This is considered as a superior high speed steel.

$\textbf{Cobalt}\left(\text{Co}\right)$

The melting point of cobalt is 1495°C. This can retain magnetic properties and wear- resistance at very high temperatures. Cobalt is used in the manufacture of magnets, ball bearings, cutting tools etc. Cobalt high speed steel (sometimes known as super H.S.S.) contains about 5 to 8% cobalt. This has better hardness and wear resistance properties than the 18% tungsten H.S.S.

Molybdenum (Mo)

The melting point of molybdenum is 2620°C. This gives high resistance against softening when heated. Molybdenum high speed steel contains 6% of molybdenum, 6% tungsten, 4% chromium and 2% vanadium. This high speed steel is very tough and has good cutting ability.

Cadmium (cd)

The melting point of cadmium is 320°C. This is used for coating steel components.

Alloying Metals and Non Ferrous Alloys

Non-ferrous Metals And Alloys

Copper and its alloys

Metals without iron are called non-ferrous metals. Eg. Copper, Aluminium, Zinc, Lead and Tin.

Copper

This is extracted from its ores 'MALACHITE' which contains about 55% copper and 'PYRITES' which contains about 32% copper.

Properties

Reddish in colour. Copper is easily distinguishable because of its colour.

The structure when fractured is granular, but when forged or rolled it is fibrous.

It is very malleable and ductile and can be made into sheets or wires.

It is a good conductor of electricity. Copper is extensively used as electrical cables and parts of electrical apparatus which conduct electric current.

Copper is a good conductor of heat and also highly resistant to corrosion. For this reason it is used for boiler fire boxes, water heating apparatus, water pipes and vessels in brewery and chemical plants. Also used for making soldering iron.

The melting temperature of copper is 1083° C.

The tensile strength of copper can be increased by hammering or rolling.

Copper Alloys

Brass

It is an alloy of copper and zinc. For certain types of brass small quantities of tin or lead are added. The colour of brass depends on the percentage of the alloying elements. The colour is yellow or light yellow, or nearly white. It can be easily machined. Brass is also corrosion-resistant.

Brass is widely used for making motor car radiator core and water taps etc. It is also used in gas welding for hard soldering/brazing. The melting point of brass ranges from 880 to 930°C.

Brasses of different composition are made for various applications.

Bronze

Bronze is basically an alloy of copper and tin. Sometimes zinc is also added for achieving certain special properties. Its colour ranges from red to yellow. The melting point of bronze is about 1005°C. It is harder than brass. It can be easily machined with sharp tools. The chip produced is granular. Special bronze alloys are used as brazing rods.

Bronze of different compositions are available for various applications.

Lead and its alloys

Lead is a very commonly used non-ferrous metal and has a variety of industrial applications.

Lead is produced from its ore 'GALENA'. Lead is a heavy metal that is silvery in colour when molten. It is soft and malleable and has good resistance to corrosion. It is a good insulator against nuclear radiation. Lead is resistant to many acids like sulphuric acid and hydrochloric acid.

It is used in car batteries, in the preparation of solders etc. It is also used in the preparation of paints.

Lead Alloys

Babbitt metal

Babbitt metal is an alloy of lead, tin, copper and antimony. It is a soft, anti-friction alloy, often used as bearings.

An alloy of lead and tin is used as 'soft solder'.

Zinc and its alloys

Zinc is a commonly used metal for coating on steel to prevent corrosion. Examples are steel buckets, galvanized roofing sheets, etc.

Zinc is obtained from the ore-calamine or blende.

Its melting point is 420° C.

It is brittle and softens on heating; it is also corrosionresistant. Due to this reason it is used for battery containers and is coated on roofing sheets etc.

Galvanized iron sheets are coated with zinc.

Tin and tin alloys

Tin

Tin is produced from cassiterite or tinstone. It is silvery white in appearance, and the melting point is 231° C. It is soft and highly corrosion-resistant.

It is mainly used as a coating on steel sheets for the production of food containers. It is also used with other metals, to form alloys.

Example: Tin with copper to form bronze. Tin with lead to form solder. Tin with copper, lead and antimony to form Babbitt metal.

Aluminium

Aluminium is a non-ferrous metal which is extracted from 'BAUXITE'. Aluminium is white or whitish grey in colour. It has a melting point of 660° C. Aluminium has high electrical and thermal conductivity. It is soft and ductile, and has low tensile strength. Aluminium is very widely used in aircraft industry and fabrication work because of its lightness. Its application in the electrical industry is also on the increase. It is also very much in use in household heating appliances.

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.3.16 Material science - Introduction of iron and cast iron

Ferrous Metals

Metals which contain iron as a major content are called ferrous metals. Ferrous metals of different properties are used for various purposes.

Introduction of Iron, Cast Iron, wrought Iron and steel

The ferrous metals and alloys used commonly are:

- Pig-iron
- Cast Iron
- Wrought Iron
- · Steels and Alloy steels

Different processes are used to produce iron and steel.

Pig-iron (Manufacturing process)

Pig-iron is obtained by the chemical reduction of iron ore. This process of reduction of the iron ore to Pig-iron is known as SMELTING.

The main raw materials required for producing Pig-iron are:

- Iron ore
- Coke
- Flux

Iron ore

The chief iron ores used are:

- magnetite
- hematite
- limonite
- carbonite.

These ores contain iron in different proportions and are naturally available.

Coke

Coke is the fuel used to give the necessary heat to carry on the reducing action. The carbon from the coke in the form of carbon monoxide combines with the iron ore to reduce it to iron.

Flux

This is the mineral substance charged into a blast furnace to lower the melting point of the ore, and it combines with the non-metallic portion of the ore to form a molten slag.

Limestone is the most commonly used flux in the blast furnace.

Properties and use of Pig-iron

Pig-iron is, therefore, refined and remelted and used to produce other varieties of iron and steel.

Cast Iron (Manufacturing process)

The pig-iron which is tapped from the blast furnace is the crude form of raw material for the cupola, and should be further refined for making castings. This refining is carried out in the cupola furnace which is a small form of a blast furnace.

Generally cupolas are not worked continuously like blast furnaces but are run only as and when required.

Cast Iron (Types)

Cast iron is an alloy of iron, carbon and silicon. The carbon content ranges from 2 to 4%.

Types of cast iron

The following are the types of cast iron.

- Grey cast iron
- White cast iron
- Malleable cast iron
- Nodular cast iron

Grey cast iron

This is widely used for the casting of machinery parts and can be machined easily.

Machine base, tables, slideways are made of cast iron because it is dimensionally stable after a period of aging.

Because of its graphite content, cast iron provides an excellent bearing and sliding surface.

The melting point is lower than that of steel and as grey cast iron possesses good fluidity, intricate casting can be made.

Grey cast iron is widely used for machine tools because of its ability to reduce vibration and minimize tool chatter.

Grey cast iron, when not alloyed, is quite brittle and has relatively low tensile strength. Due to this reason it is not used for making components subjected to high stress or impact loads.

Grey cast iron is often alloyed with nickel, chromium, vanadium or copper to make it tough.

Grey cast iron is weldable but the base metal needs preheating.

White cast iron

This is very hard and is very difficult to machine, and for this reason, it is used in components which should be abrasion-resistant.

White cast iron is produced by lowering the silicon content and by rapid cooling. When cooled in this manner, it is called chilled cast iron.

White cast iron cannot be welded.

Malleable cast iron

Malleable cast iron has increased ductility, tensile strength and toughness when compared with grey cast iron.

Malleable cast iron is produced from white cast iron by a prolonged heat-treatment process lasting for about 30 hours.

Nodular cast iron

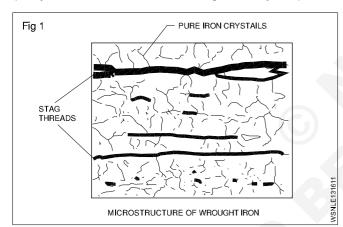
This is very similar to malleable cast iron. But this is produced without any heat treatment. Nodular cast iron is also known as: **Nodular Iron - Ductile Iron - Spheroidal Graphite Iron**

This has good machinability, castability, resistance to wear, low melting point and hardness.

Malleable and nodular castings are used for machine parts where there is a higher tensile stress and moderate impact loading. These castings are less expensive and are an alternative to steel castings.

Wrought Iron (Manufacturing process) (Fig 1)

Wrought iron is the purest form of iron. The analysis of Wrought iron shows as much as 99.9% of iron. (Fig 1) When heated, wrought iron does not melt, but only becomes pasty and in this form it can be forged to any shape.



Modern methods used to produce wrought iron in large quantities are the

- puddling process
- aston or Byers process

Steel

This is pure iron. Carbon content is more. Due to excessive carbon it is harder and tougher. Carbon content is from 0.15 to 1.5%. Besides there are other impurities like sulphur, phosphorous etc. are there which cannot be separated. This is hardened and tempered by heating it to a definite temperature and cooling it in oil or water.

The following methods are adopted for making different types of steel:

- 1 Cementation process 2 Crucible process
- 3 Bessemer process 4 Open hearth process
- 5 Electro thermo process 6 High frequency process.

Types of steel

Main two types of steel are:

- 1 Plain steel
- 2 Alloy steel
- **1 Plain steel**. In this carbon and iron are mixed. According to the percentage of carbon plain steels are classified as:
 - A Low carbon steel
 - B Medium carbon steel
 - C High carbon steel
 - A Low carbon steel: It is also called mild steel. In this. the percentage of carbon is from 0.15%to0.25%. Due to less quantity of carbon is sufficiently soft and tolerates the strain. It can be put in different shapes through forging and rolling. This is not very hard or strong. This cannot be hardened or tempered by ordinary methods. Nuts, bolts, rivets, sheets, wires, T-iron and angle iron etc. are made out of it.
 - B Medium carbon steel: The carbon content is from 0.25% to 0.5%. Due to excess of carbon, it is harder and tougher than mild steel. The tenacity is more. This can be hardened or tempered. Various things are made by forging and rolling. This is used for making high tensile tubes, wires, agricultural implements, connecting rods, cam shafts, spanners, pulleys etc.
 - **C High carbon steel:** It has carbon content from 0.5% to 1.5%. It is very hard and wears least. This can be hardened by heat treatment. This can neither be cast nor rolled. This is very hard and tough. It acquires permanent magnetic properties. This is used for making pointed tools, springs, pumps, files, cutleries, cold chisels press die etc.

2 Alloy Steel

When the steel is mixed with other metals like vinoleum, manganese tungsten etc., it is called an alloy steel. Alloy steel has properties of its ingredients.

Types of Alloy Steel

Two types of alloy steel are:

- A Low alloy steel
- B High alloy steel
- A Low Alloy steel: Besides carbon other metals are in lesser quantity. Its tensile strength is more. The welding can work on it. This can also be hardened and tempered. It is used in manufacturing various parts of an aeroplane and cam shaft etc.
- **B** High Alloy Steel: Besides carbon it has a high percentage of the metals higher than low steel alloy. This is classified into following types:

- a High Speed Steel: It is also called high tungsten alloy steel because it has more quantity of tungsten. According to the quantity of tungsten it is classified into three types:
 - 1 Tungsten 22%, Chromium4%, Vanadium 1%
 - 2 Tungsten 18%, Chromium 4%, Vanadium 1%
 - 3 Tungsten 14%, Chromium 4%, Vanadium 1%

Cutting tools are made out of it because it is very hard but becomes soft at low critical temperature. This temperature is raised out of cutting process of tool, then the cutting tool becomes useless and is unfit for work. But due to high percentage of tungsten it keeps working upto high temperature. It is used for cutting tools, drills, cutters, reamers, hacksaw blades etc.

- b Nickel Steel: In this 0.3% carbon and 0.25 to 0.35% nickel is present. Due to nickel its tensile strength, elastic limit and hardness is increased. It does not catch rust. Its cutting resistance increases 6 times more than plain carbon and steel due to 0.35% nickel present in it. This is used for making rivets, pipes, axle shafting, parts of buses and aeroplanes. If 5% of cobalt is mixed with 30-35% nickel, it becomes invar steel. It is mainly used for making precious instruments.
- **c** Vanadium Steel: It contains 1.5% carbon 12.5% tungsten, 4.5% chromium, 5% vanadium and 5% cobalt. Its elastic limit, tensile strength and ductility is more. It has strength to bear sharp jerks. It is mainly used to manufacture of tools.
- d Manganese Steel: It is also called special high alloy steel. It contains 1.6 to 1.9% of manganese

and 0.4 to 0.5% carbon. It is hard and less wear. It is not affected by magnet. It is used in grinders and rail points etc.

e Stainless Steel: Along with iron it contains 0.2 to 90.6% carbon, 12 to 18% chromium, 8% nickel and 2% molybdenum. It is used for making knives, scissors, utensils, parts of aeroplane, wires, pipes and gears etc.

Properties of stainless steel:

- 1 Higher corrosion resistance
- 2 Higher cryogenic toughness
- 3 Higher work hardening rate
- 4 Higher hot strength
- 5 Higher ductility
- 6 Higher strength and hardness
- 7 More attractive appearance
- 8 Lower maintenance
- f Silicon Steel: It contains 14% of silicon. Its uses are multifarious according to the percentage of silicon. 0.5% to 1% silicon, 0.7 to 0.95% manganese mixture is used for construction work. 2.5 to 4% silicon content mixture is used for manufacturing electric motors, generators, laminations of transformers. In chemical industries 14% silicon content mixture is used.
- **g** Cobalt Steel: High carbon steel contains 5 to 35% cobalt. Toughness and tenacity is high. It has magnetic property therefore used to make permanent magnets.

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.4.17 Mass, Weight, Volume and Density - Mass, volume, density and weight

Mass

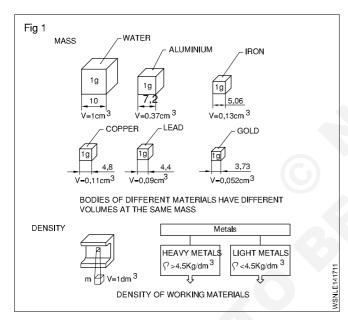
Mass of a body is the quantity of matter contained in a body. The unit of mass in F.P.S system is pound (lb), in C.G.S. system gram (gr) and in M.K.S and S.I systems kilogram(kg). 1ton which is 1000 kg is also used sometimes. The conversion factor is 1000. Three decimal places are shifted during conversion.E.g.1 ton = 1000 kg 1g = 1000 mg.

m - mass of a body

- g acceleration due to gravity in metre/sec² = 9.81 m/ sec²
- V volume of the body
- $\rho\,$ density (pronounced as `rho')

W or FG - weight or weight force

Mass(Fig 1)



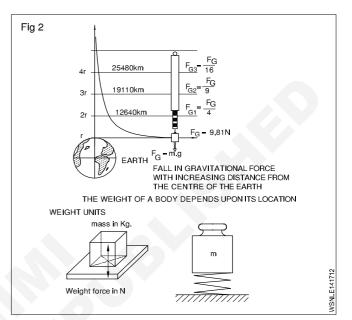
Density

Density is the mass of a body per unit volume. Hence its unit will be gr/cm^3 or kg/dm^3 or ton/m^3 .

Density =
$$\frac{\text{mass}}{\text{volume}} = \frac{\text{m}}{\text{v}} = \rho$$

Weight (Fig 2)

Weight is the force with which a body is attracted by the earth towards its centre. It is the product of the mass of the body and the acceleration due to gravity. The weight of a body depends upon its location.



weight = W or FG = mass x gravitational force = m x g

System	Absolute unit	Derived unit	Conversion
F.P.S. system	1 poundal	1 Lb wt	32.2 poundals (1 lb x 1 ft/sec ² = 1 pound)
C.G.S. system	1 dyne 1 gr x 1 cm/sec²	1 Gr.wt	981 dynes
M.K.S.	Newton	1 kg.wt	1 Newton =
S.I.system	Newton	Newton	1 kg x 1 m/sec ²
1 kg.wt = 9.81 Newton 1 Newton = 10⁵ dynes. (approximately 10N)			

Difference between mass and weight

S. No	Mass	Weight
1	Mass is the quantity of matter in a body (ie) measurement of matter in a body	Weight is measure of amount of force acting on mass due to acceleration due to gravity
2	It does not depend on the position or space	It depends on the position, location and space
3	Mass of an object will not be zero	Weight of an object will be zero if gravity is absent
4	It is measured using by physical balance	It is measured using by spring balance
5	It is a scalar quantity	It is a vector quantity
6	When immersed in water mass does not change	When immersed in water weight will change
7	The unit is in grams and kilogram	The unit is in kilogram weight, a unit of force

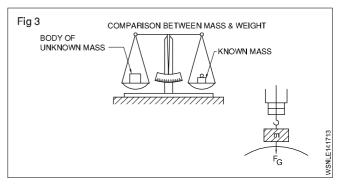
Mass and weight are different quantities. Mass of a body is equal to volume x density. Weight force is equal to mass x acceleration due to gravity.

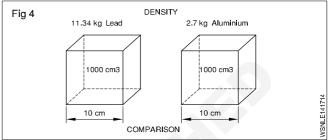
Weight and Density

It is now seen that the mass of a substance is measued by its weight only without any reference to volume. But if equal weights of lead & aluminium, are compared the volume of lead is much smaller than volume of aluminium. So we can now say that lead is more dense than aluminium, i.e In other words the density of lead is greater than aluminium. (Fig 3 & 4)

The relation of mass and volume is called density.

The density expresses the mass of volume E.g. 1 dm 3 of water has the mass of 1kg - thus the density of 1kg/dm 3 (Fig 2)





Unit

The density is measured as below

MKS/SI= Kg/m³, CGS = 1 gm/cm³ FPS = lbs/c ft

	Solids	gm/cc	Liquids	gm/cc
1	Aluminum	2.7	Water	1.00
2	Lead	11.34	Petrol	0.71
3	Cast iron	6.8 to 7.8	Oxygen	1.43
4	Steel	7.75 to 8.05	Diesel Oil	0.83

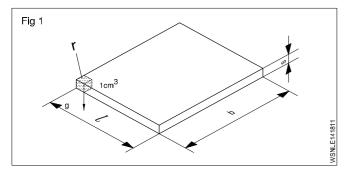
Comparison Between Density And volume

Density	Volume
Mass per unit volume of a substance is called its density	The volume of an object is the amount of space occupied by the object or shape.
Its unit is gm per cu cm; Ibs per cu.ft and kg/cubic meter	Volume = I x b x h
Density = Mass Volume	

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.4.18

Mass, Weight, Volume and Density - Related problems for mass, volume, density and weight

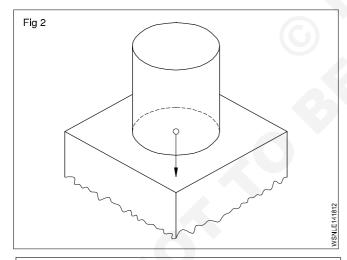
- Calculate the mass in kg of a rectangular steel plate of dimensions 220 x 330 x 15 mm (Fig 1) (density of steel = 7.82 gm/cm³)
 - Mass = Volume x density
 - = 22 x 33 x 1.5cm x 7.82 gm/cm³
 - = 1089 cm³ x 7.82 gm/cm³



2 What is the weight in Newton if a storage container holds 250 litres of water and amount of water exert on the surface which it is standing? (Fig 2)

(1 litre of water = 1 kg of water)

Density of water 1 gm/cm³ or 1 kg/dm³



Acceleration due to gravity is taken as 10 metre/sec² (approximation).

Capacity = 250 litres = 250 dm³ in volume.

Mass of water = volume x density of water

= 250 dm³ x 1 kg/dm³ = 250 kg

Weight extended = mass x acceleration due to gravity

= 250 kg x 10 metre/sec²

= 2500 kg.metre/sec² = 2500 N(... 1 kg.m/sec²=1N)

3 A force of 15 dynes acting on a mass of `m' produces an acceleration of 2.5 cm/sec². Find the mass.

$$\therefore$$
 15 dynes = $\frac{15}{981}$ Gr.wt

Force = m x acceleration produced by the force

- Gr.wt = mass x 2.5 cm/sec²
- gr.cm/sec² = mass x 2.5 cm/sec²

$$\therefore \text{ mass} = \frac{15}{981 \times 2.5} \text{ grams} = \frac{\text{gm.cm/sec}^2}{\text{cm/sec}^2}$$

mass = 0.00612 gram

4 A force of 2 N acts on a mass of 10 kg. Find the acceleration produced by the force on the mass.

Force = $2 N (: 1 N = 1 kg.m/sec^2)$

Force = mass x acceleration

- ... 2 kg.metre/sec² = 10 kg x acceleration produced
- \therefore 2 x 1 kg.metre/sec² = 10 kg x acceleration produced
- ... acceleration produced

 $=\frac{2}{10}$ metre/sec²

= 0.2 metre/sec²

5 Calculate the weight of a body having a mass of 1 kg if the acceleration due to gravity is 9.81 metre/sec²

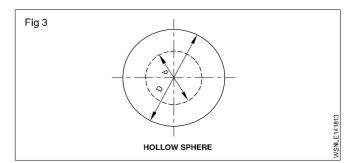
Weight force = mass x acceleration due to gravity = $1 \text{ kg x } 9.81 \text{ metre/sec}^2$

$$(1 \text{ kg.metre/sec}^2 = 1 \text{ N})$$

... 9.81 kg metre/sec² = 9.81 N

In the examples solved the value of `g' is taken as 10 metre/sec², unless specifically mentioned otherwise.

 The outside and inside diametres of a hollow sphere are 150 & 70mm respectively. Calculate its mass if the density of material is 7.5 gm/cm³. (Fig 3)



Mass = Volume x Density

= Volume x 7.5 gm/cm³

D= 150 mm = 15cm R= 7.5 cm

Volume =
$$\frac{4}{3}\pi (R^3 - r^3)$$
unit³
= $\frac{4}{3}\pi (7.5^3 - 3.5^3)$

=1587.5 cm³

Mass = 1587.5 cm³ X 7.5 gm/cm³

= 11906.6 gm=11.9kg say 12kg

6 A car has a mass of 800 kg. Find out its weight force (Take 9.81 m/sec²)

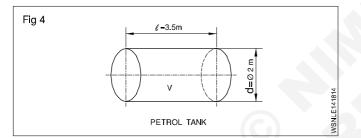
(: 1N = 1kg.m/sec²)

The Wt. force of a car=Mass of car x gravitational acceleration

= 800 x 9.81 N

= 7848 Newtons

7 A cylindrical tank 2m dia x 3.5 m length is filled with petrol. Find the weight of petrol in Tonnes, Assume density of petrol 720 Kg/m³. (Fig 4)



Volume of Tank

$$v = \pi r^2 |(or) \frac{\pi d^2}{4} x |$$
 unit³ = $\frac{\pi x 2^2}{4} x 3.5 m^3$

 $3.14 \times 3.5 \text{ m}^3 = 10.99 \text{ m}^3$ Since 1 m³ = 1000 litres Volume of Tank = 10.99 x 1000 litres Density of petrol = 720 Kg/m³. Weight of Petrol in Kg =10.99x1000 litresx720Kg = 720 x 10990 Kg

Weight of Petrol in Tonnes

(Mastria I Insita)	720X10990	
(Metric Units)	1000	
Weight of Petrol	= 7912.8 Tonnes	

8 If the battery acid specific gravity is 1.3, and this is being filled up into a cylindrical tank. Find out its density.

(Density of water = 1 gm/cm³)

Specific gravity or Relative density

Density of the substance

Density of water at 4°c

Now, density of battery acid

= Specific gravity x Density of water

= 1.3 x 1 gm/cm³

= 1.3 gm/cm³

Example

1 An iron piece weighs 160 kgf in air and 133 kgf when it is fully immersed in water. Find the volume and density of the iron piece.

Weight of the solid in air = 160 kgf Weight of the solid in water = 133 kgf \therefore Loss of weight in water = 27 kgf

By Archimedes principle the loss of weight of a solid in water = volume of water displaced.

- :. Volume of water displaced = 27 cm³
- .:. Volume of the solid= 27 cm³

Density of the iron piece = mass of iron volume of the piece

$$=\frac{160}{160-133}=\frac{160}{27}=5.93$$

Density of the Iron piece = 5.93 gm/cc

2 A piece of wood having 80cc volume, when floated on water remains 60cc volume above water. Find the weight of the water displaced.

Water displaced	= Immersed volume
Immersed volume	= volume of wood - volume of wood above water level
	= 80 - 60 = 20c.c

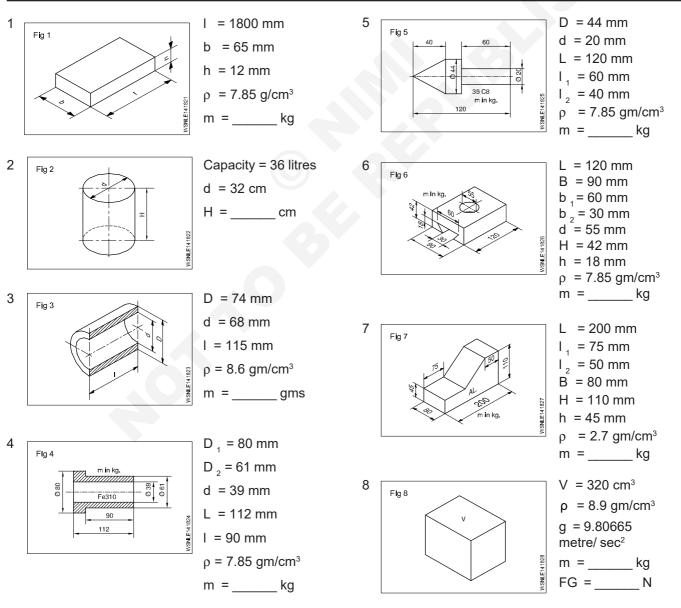
Weight of water displaced = volume x density of water

= 20 x 1 = 20 grams

SI.No	Substance	Density gm/cc
1	Aluminium	2.7
2	CastIron	6.8 - 7.8
3	Copper	8.92
4	Gold	19.32
5	Iron	7.86
6	Lead	11.34
7	Nickel	8.912
8	Silver	10.5
9	Steel	7.75 - 8.05
10	Tin	7.31
11	Zinc	7.14
12	Diamond	3.51

SI.No	Substance	Density gm/cc
13	Bismuth	9.78
14	Brass	8.47
15	Phosphorus Bronze	8.7 - 8.9
16	Ice	0.93
17	Air	0.0013
18	Mercury	13.56
19	Petrol	0.71
20	Diesel	0.83
21	Kerosene	0.78 - 0.81
22	Water	1.0

Assignment



WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.4.18

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.5.19

Speed and Velocity, Work, Power and Energy - Work, power, energy, HP, IHP, BHP and efficiency

Work (Fig 1)

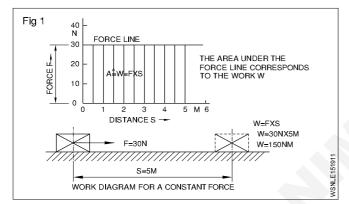
Work is said to be done by a force, when it moves, its point of application through a distance. Applied force 'F' moves a body through a distance's.

Work done 'W' = F x s.

The S.I. unit of work is 1 joule which is the work done by a force of moving the body through a distance of 1 metre.

Therefore joule = 1 N x 1 metre = 1 Nm

Also 1 joule = $1 \text{ Nm} = 10^5 \text{ dynes x } 100 \text{ cm} = 10^7 \text{ dynes cm} = 10^7 \text{ ergs.}$



F - force or weight force in N

 $\ensuremath{\mathsf{s}}$ - distance the body on which force acts is moved in metres

t - time in seconds

v - speed in metre/sec

w - work done by the force in joules

P - Power in Watts

P_{out} - Power output

P_{in} - Power input

Force

A Force is that which changes or tends to change the state of rest or motion of a body.

Force = Mass x Acceleration

F = Ma

Unit

F = M x a

= kg x m/sec²

= 1 Newton (SI unit)

(Newton: If 1 kg of mass accelerates at the rate of 1m/sec² then the force exerted on the mass is 1 newton)

- FPS = 1 pound x 1 Feet/second²
 - = 1 pound
- CGS = 1 gm x 1cm/second²

MKS = 1 kg x 1m/second²

= Newton.

1 Newton = 10⁵ dynes

1kg wt = 9.81N

1 pound = 4.448N,

Newton = 0.225 pound.

Absolute units

In C.G.S. system unit of work = 1 erg = 1 dyne x 1 cm In F.P.S system unit of work = 1 Foot poundal = 1 poundal x 1 foot

In M.K.S. system unit of work = 1 joule = 1 Newton x 1 metre

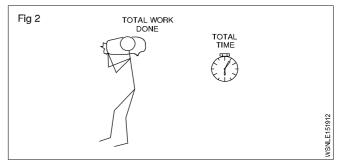
Derived units

C.G.S. system 1 gm Wt x 1 cm = 981 ergs.

F.P.S. system 1 ft lb = 981 foot poundal

M.K.S. system 1 kgf metre = 981 joule.

Power (Fig 2)



It is the work done in unit time.

Power P =
$$\frac{\text{total work done}}{\text{total time}}$$

P = $\frac{\text{Nm}}{\text{sec}}$

The S.I units of power = 1Nm/sec = $\frac{1 \text{ joule}}{\text{sec}}$ which is = 1 watt. power in watts = $\frac{W}{t} = \frac{F.s}{t} = FXV$

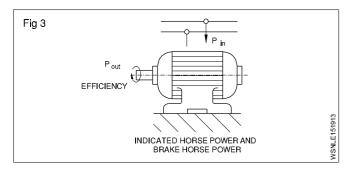
which is equal to 1 Watt. Power in watts = w/t = F.s/t = F x V

In M.K.S. system the unit is 1 kgf meter/sec. One horse power is = 75 kg metre/sec or 4500 kgf metre/min.

1HP (metric) = 735.5 Watts

1HP (British) = 746 Watts = 0.746 KW

Power input is the power given to a machine to do work. Power output is what we get out of the machine. Power output is always less than power input due to friction in the machine. The ratio between power output to power input is efficiency of the machine and it is expressed in percentage. (Fig 3)



efficiency = $\frac{\text{power output}}{\text{power input}} \times 100\%$

Indicated Horse Power and Brake Horse Power

The power actually generated by the engine or generator is the indicated horse power which is indicated on the plate.

The Brake horse power is the power available to do useful work. B.H.P is always less than I.H.P. due to losses to overcome frictional resistance.

: mechanical efficiency = $\frac{B.H.P}{I.H.P} \times 100\%$

Work done by a force = Magnitude of the force x distance moved by the body

Power = Total work done / total time taken

efficiency =
$$\frac{\text{power output}}{\text{power input}} \times 100\%$$

Energy

The energy of a body is its capacity to do work. It is equal to power x time. Hence the unit of energy is the same as the unit of work in all systems.

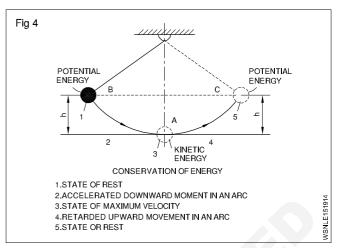
Forms of energy

Mechanical energy, Electrical energy, Atomic energy, Heatenergy, Lightenergy, Chemical energy, sound energy. Energy of one form can be transformed into energy of another form.

Law of conservation of energy

- The energy can neither be created nor destroyed.
- Total energy possessed by a body remains the same.(Fig 4)

Depending upon the position of the body or body in motion, mechanical energy possessed by the body may be potential energy or kinetic energy respectively.



Examples

1 A man weighting 75kg climp 200 metre high hill. Find the Work done by a man?

Formula: Work done (W) = $F \times S$ Given data: F = 75 kg

S = 200m

To find: Work done (W) = ?

Solution: Work done (W) = F x S

= 75 x 200 = 15000

Ans: Work done (w) = 15000 kgm

2 Find the work required to lift a mass of 36.3 Newtons through a height of 3.7 metres?

Formula:Work done (W) = F x SGiven data:F= 36.3 NS= 3.7 mTo find:Work done (W) = ?Solution:Work done (W) = F x S

= 36.3 x 3.7 N.m

= 134.31 Joules

Ans: Work done (W) = 134.31 Joules

3 Calculate the Work done by a man weighing 50kg in carrying a mass of 20kg over his head when he covers a distance of 15metres in vertical direction.

Formula: Work done (W) = F x S Given data: F = 50kg + 20kg = 70kg S = 15 mTo find: Work done (W) = ?

Solution: Work done (W) = F x S

= 70 x 15 = 1050

Ans: Work done (W) = 1050 kg.m

4 A man weighing 60kg lifts a weight of 40kg to the top of building 12 metres height. Find the useful Work done by him and also the efficiency?

Formula: Work done (W) = F x S Given data: Man weight = 60kg Lifts a weight = 40kg = 60 + 40 = 100kg Total weight Distance (S) = 12 m To find: a) Work done (W) = ? b) Efficiency $(\eta) = ?$ Solution: a) Work done (W) = F x S = 100 x 12 = 1200 kg.m b) Efficiency (η) = $\frac{\text{Output}}{\text{Input}} \times 100\%$ $= \frac{40 \times 12}{60 \times 12} \times 100\%$

 $=\frac{480}{720} \times 100\%$

= 66.67%

Ans: a) Work done (W) = 1200 kg.m

b) Efficiency (η) = 66.67%

5 A pump pumps 4000kg of water from 50 metres depth in 40 minutes. Find the Work done by pump in one second?

Work done (W) = $F \times S$ Formula: Given data: F = 4000 ka S = 50 m

To find: Work done per second = ?

Solution:

Work done in 40 minutes,

Work done (W) = $F \times S$

$$=\frac{200000}{40}=5000$$

Work done in 1 second = $\frac{5000}{60}$ = 83.3

Ans: Work done in 1 second (W) = 83.33 kg.m

6 A body of 225 kg is moved by 300 metres in 90 seconds. Find the power required to lift this body?

Formula: Power (P) = $\frac{FxS}{+}$

Given data:

$$F = 225 \text{ kg}$$

$$S = 300\text{m}$$

$$t = 90 \text{ sec}$$
To find: Power

$$(P) = ?$$
Solution: Power

$$(P) = \frac{FxS}{t}$$

$$= \frac{225 \times 300}{90} \text{ kg.m/sec}$$

= 750 kg.m/sec

Ans: Power (P) = 750 kg.m/sec

7 A hydraulic press lifts a load of 5 tonnes in 5 minutes to a height of 5 metres. Calculate the power of the press?

Formula: Power (P) =
$$\frac{FxS}{t}$$

Given data: F = 5 tonnes = 5000 kg
S = 5 metres
t = 5 minutes = 5 x 60 = 300 sec
To find: Power (P) = ?
Solution: Power (P) = $\frac{FxS}{t}$
= $\frac{5000 \times 5}{t}$ = 83.33

300

Ans: Power (P) = 83.33 kg.m/sec

A machine weighing 750N takes 25N material to a 8 height of 10 metres in one minute. calculate the power of machine?

Formula: Power (P) =
$$\frac{FxS}{t}$$

Given data:

Machine weight = 750N
Material weight = 25N
F = 750 + 25 = 775N
S = 10 m
t = 1 min = 60 sec
To find: Power (P)=?
Solution: Power (P)=
$$\frac{FxS}{t}$$

 $=\frac{775 \times 10}{60}$ = 129.17N m/sec

Ans: Power (P) = 129.17N m/sec (or) watts

9 What is the power of pump which takes 15 seconds to lift 90kg of water to a tank situated at a height of 30 metres. (Take g = 10m/sec²)?

Formula: Power (P) = $\frac{FxS}{t}$ Given data: F = 90 kg S = 30 m t = 15 sec To find: Power (P) = ? Solution: Power (P) = $\frac{FxS}{t}$ $= \frac{f \times g \times s}{t}$ $= \frac{90 \times 10 \times 30}{15}$ = 1800 Nm/sec \therefore (1Nm/sec=1 watt) Ans: Power (P) = 1800 watts

10 A hoist lifts a weight of 1000kg through a height of 33 metres in one minute. Find out the horsepower of the hoist?

Formula: Horsepower HP = $\frac{FxS}{t} \times \frac{1}{75}$ F = 1000 kgGiven data: S = 33 m t = 1 minute = 60 secTo find: Horsepower HP = ? **Solution:** Horsepower HP = $\frac{FxS}{t} \times \frac{1}{75}$ (∵ 75 kg.m/sec = 1 HP) $=\frac{1000 \times 33}{60} \times \frac{1}{75}$ = 7.33 H.P. Ans: Horsepower, HP = 7.33 H.P. 11 A pump can raise 900 litres of water per minute to a height of 45 metres. Calculate the H.P of pump? Formula: Horsepower HP = $\frac{FxS}{t} \times \frac{1}{75}$ Given data: F = 900 litres = 900 kg S = 45 m t = 1 minute = 60 sec

To find: Horsepower HP = ?

Solution: Horsepower HP = $\frac{FxS}{t} \times \frac{1}{75}$

(∵ 1 HP = 75 kg.m/sec)

- **Ans:** Horsepower, HP = 9 H.P.
- 12 Find the horsepower of an engine to lift a weight of 2 tonnes to a height of 30 metres in two minutes?

 $=\frac{900 \times 45}{60} \times \frac{1}{75} = 9 \text{ H.P}$

Formula: Horsepowe	$r HP = \frac{FxS}{t} \times \frac{1}{75}$	
Given data:	F = 2 tonnes = 2000 kg	
	S = 30 m	
	t = 2 minutes = 120 sec	
To find: Horsepower	HP = ?	
Solution: Horsepower	$HP = \frac{FxS}{t} \times \frac{1}{75}$	
(<u>·</u> · 1 HP =	= 75 kg.m/sec)	
$=\frac{2000 \times 30}{120} \times \frac{1}{75} = 6.67 \text{ H.P.}$		

Ans: Horsepower, HP = 6.67 H.P.

13 Find out horsepower of a pump required to lift 10000 litres of water in 3 minutes at height of 16 metres. Assume efficiency of pump as 94%?

Formula: Horsepower HP =
$$\frac{FxS}{t} \times \frac{1}{75}$$

$$\eta = \frac{\text{Output}}{\text{Input}} \times 100\%$$

Given data: F = 10000 litres = 10000 kg S = 16 litres

t = 3 minute = 180 sec

To find: Horsepower HP = ?

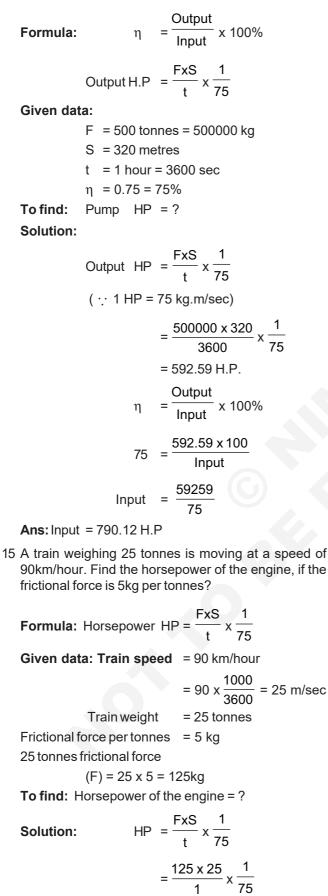
Solution: Horsepower HP = $\frac{FxS}{t} \times \frac{1}{75}$

$$= \frac{10000 \times 16}{180} \times \frac{1}{75}$$
$$= 11.85 \text{ H.P.}$$
$$\eta = \frac{\text{Output}}{\text{Input}} \times 100\%$$
$$94 = \frac{11.85}{\text{Input}} \times 100$$
$$\text{Input} = \frac{11.85 \times 100}{94} = \frac{1185}{94}$$
$$= 12.606 \text{ H.P.}$$

Ans: Input H.P of Pump = 12.606 H.P.

WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.5.19

14 Find the horsepower of a motor which is required to lift 500 tonnes of coal per hour from a mine of 320 metre depth. Efficiency of motor is 0.75?



16 A pump delivers 9000 litres of water per minute to a height of 14 metres. The efficiency of the pump is 78%. The efficiency of electric motor which drives the pump is 92%. Find out the input of the motor?

Formula:

$$\eta = \frac{Output}{Input} \times 100\%$$

$$Output H.P = \frac{FxS}{t} \times \frac{1}{75}$$

$$1 H.P = 0.7355 KW (metric)$$
Given data:

$$F = 9000 \text{ litres} = 9000 \text{ kg}$$

$$S = 14 \text{ metres}$$

$$t = 1 \text{ minute} = 60 \text{ sec}$$
pump $\eta = 75\%$
motor $\eta = 92\%$
To find: Electric motor (KW) = ?
Solution:
Pump Output HP = $\frac{FxS}{t} \times \frac{1}{75}$

$$= \frac{9000 \times 14}{60} \times \frac{1}{75}$$

$$= 28 \text{ H.P.}$$
Input of the pump

$$\eta = \frac{Output}{Input} \times 100\%$$

$$78 = \frac{28}{Input} \times 100$$

$$Input = \frac{28 \times 100}{78} = 35.9 \text{ H.P}$$
Output of the motor = Input of the pump
Output = 35.9 \text{ H.P}
Input of the motor
Motor $\eta = \frac{Output}{Input} \times 100\%$

$$g2 = \frac{35.9}{Input} \times 100$$

$$Input = \frac{35.9 \times 100}{92} = 39.02 \text{ H.P}$$

Ans: HP = 41.67 H.P.

S

45

17 I.H.P of generator is 6 H.P and its efficiency is 90%. Find tis B.H.P.

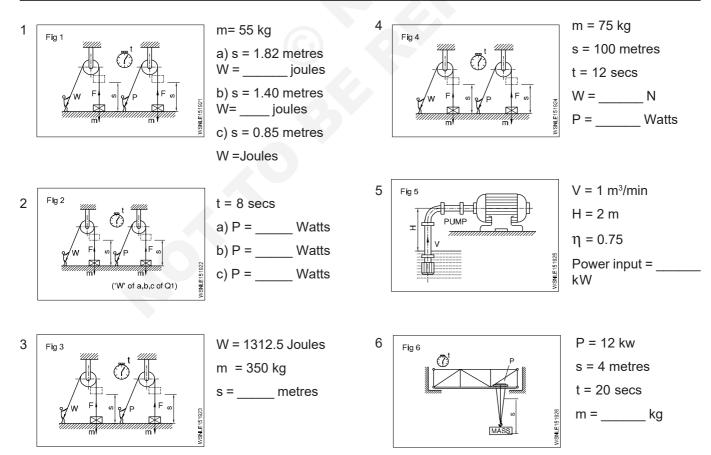
Formula: $\eta = \frac{B.H.P}{I.H.P} \times 100\%$ Given data: I.H.P = 6 H.P $\eta = 90\%$ To find: B.H.P = ? Solution: $\eta = \frac{B.H.P}{I.H.P} \times 100\%$ $g0 = \frac{B.H.P}{6} \times 100\%$ $\frac{90x6}{100} = B.H.P$ B.H.P = 5.4 H.PAns: B.H.P of generator = 5.4 H.P 18 A machine is working on 80% efficiency I.H.P of machine is 50. Calculate the power lost in friction. $\eta = \frac{B.H.P}{I.H.P} \times 100\%$ Given data: Efficiency $\eta = 80\%$ I.H.P = 50 To find: Friction = ? Solution: $\eta = \frac{B.H.P}{I.H.P} \times 100\%$ $80 = \frac{B.H.P}{I.H.P} \times 100\%$ $80 = \frac{B.H.P}{50} \times 100\%$ $\frac{80x50}{100} = B.H.P$ B.H.P = 40 B.H.P = 1.H.P - F.H.P 40 = 50 - F.H.P40 + F.H.P = 50

F.H.P = 50 - 40 = 10

Formula: I.H.P = B.H.P + Frictional loses

Ans: Loss of friction = 10 H.P

Assignment



Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.5.20

Speed and Velocity, Work, Power and Energy - Potential energy, kinetic energy and related problems with assignments

Potential energy

Potential energy is the energy possessed by a body by virtue of its position. A body of mass 'm' kept at a height 'h' from a datum possesses a potential energy of mgh or Wh or Fh; where W or F are the Weight force. When the body is allowed to fall it will be able to do a useful work of Fh.

Example

- Water stored in a Tank
- Coil Spring.

Kinetic energy

It is the energy possessed by a body by virtue of its motion. If a body of mass 'm' starting from rest attains a velocity of 'v' after covering a distance of 's', by the action of an applied force 'F', then work done on the body=F x s But F = m x a. Therefore work done on the body = m x a x s.

But a x s = $\frac{V^2}{2}$ because the body is starting from rest.

Therefore Work done on the body = $\frac{1}{2}$ mv².

Since work done on the body = The energy possessed by the body

Kinetic Energy = $\frac{1}{2}$ mv².

Energy possessed by a body = work done on the body

Potential energy = mgh

Kinetic energy = $\frac{1}{2}$ mv²

If friction is neglected potential energy = Kinetic energy

Example

- Rolling vehicle
- Rotating fly wheel
- Flowing water
- Falling weight

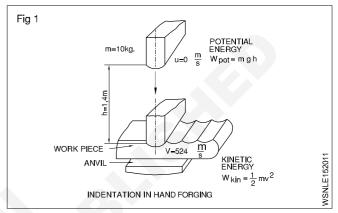
Potential energy

Hammer head drops from height 'h' . m = 10 kg.

 $u = 0 \frac{\text{metre}}{\text{sec}}$ $V^2 = 2 \text{ gs}$ $V^2 = 2 \text{ x } 9.81 \text{ x } 1.4$ $V^2 = 27.468$ V = 5.24 m/sec

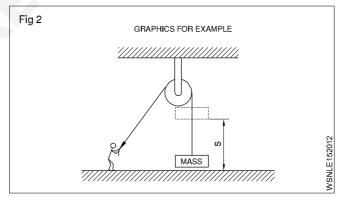
 $P.E = 10 \text{ kg x } 9.81 \text{ metre/sec}^2 \text{ x } 1.4 \text{ metre (Fig 1)}$

K.E =
$$\frac{1}{2}$$
 x 10 kg x 5.24² $\frac{\text{metre}^2}{\text{sec}^2}$



Examples

• A pulley is used to lift a mass with a force of 900 N to a height of 10 metres in 2 minutes. Find the work done by the force and also the power.(Fig 2)



Work done = F x s = 900N x 10 metre

= 9000 Nm = 9000 joules.

Power =
$$\frac{W}{t} = \frac{9000 \text{ joules}}{120 \text{sec}}$$

= $\frac{75 \text{ joules}}{\text{sec}}$
= 75 watts

• Determine the horse power required to drive a lift in raising a load of 2000 kgf at a speed of 2 metre/sec, if the efficiency is 70%.

Useful Work done to raise the lift in 1 sec Force = 2000 kgf Work = F x d

Power =
$$\frac{F \times d}{t} = \frac{2000 \times 2}{1}$$

= 4000 w
Power output = 4000 w
Power input = Power output
= $\frac{4000}{0.7} = 5714$ w

 $\eta = \frac{\text{Output}}{\text{Input}} \times 100\%$

 $HP = \frac{5714}{746} = 7.659 \cong 7.6HP$ Power input = 7.6 HP

A mass of 100 gm is allowed to fall from a height of 10 metres. Determine the amount of Kinetic energy gained by the body. (Take the value of g as 10 metre/ sec²

Since initial velocity is 0 and distance travelled is 10 metres. final velocity $^{2}\,$

 $=V^2 = 2 \times g \times s = 2 \times 10 \times 10 \text{ metre}^2/\text{sec}^2$

$$\therefore \text{K.E} = \frac{1}{2}\text{mv}^2 = \frac{1}{2} \times 100 \text{ gm} \times 200 \text{ metres}^2/\text{sec}^2$$

 $= 10000 \text{ gm metre}^2/\text{sec}^2$

 $=10 \times 10^7$ ergs

= 10 Joules.

K.E. developed by the vehicle at a constant speed

• A motor vehicle of one tonne is travelling at 60 km/hr. Calculate K.E of the vehicle at this speed.

K.E of the vehicle = $\frac{1}{2}$ mv²

Where m = one tonne or 1000 kg

$$v = 60 \text{ km/hr}$$

Solution

Changing v into meter/sec we get,

V = 60× $\frac{1000}{60\times60} = \frac{50}{3}$ m/sec (∴ 1km = 1000m) (∴ 1hour = 3600sec) Now K.E. of vehicle = $\frac{1}{2} \times 1000 \times \frac{50}{3} \times \frac{50}{3}$ 2500

$$= \frac{1000 \times \frac{1000}{18}}{18}$$
$$= \frac{2500000}{18}$$
J

$$=\frac{2500000}{100 \times 18} K.$$
$$=\frac{1250}{9} KJ$$
$$= 138.89 KJ$$

K.E.developed by a vehicle during acceleration

 A motor vehicle of 1200 Kg mass is being accelerated from 36 km to 48 km/hr speed. Calculate the increase in K.E during its acceleration.

Solution

Mass of motor vehicle= 1200 kg

K.E. of the vehicle at 36 km/hr speed

$$= \frac{1}{2} \times 1200 \times 36^{2} J \qquad \text{KE} = \frac{1}{2} \text{ mv}^{2} J$$

v= 36km/hr = 36 x $\frac{1000}{60 \times 60}$ = 10m/sec

K.E of the vehicle at 48 km/hr speed

$$=\frac{1}{2} \times 1200 \times 48^2 J$$
 (\therefore 1kg.m/sec² = 1N)

v= 48 km/hr

$$=48 \text{ x} = \frac{1000}{60 \times 60} = \frac{40}{3} \text{ m/sec}$$

4.0

4000

$$KE = \frac{1}{2} \times 1200 \times 10 \times 10 = 60000 J$$

KE =
$$\frac{1}{2}$$
 x1200 x $\frac{40}{3}$ x $\frac{40}{3}$ = 106666.67 J

Increase in K.E of the vehicle = 106666.67 J - 60000 J= 46666.67 J= 46.666 KJ.

Work done in vehicle operation

The Mechanical Work performed by the motor vehicle for its propulsion on road can generally be classified into two major categories of work done.

- Work done by the IC engine in developing full power under all condition of speed and load.
- Work done by the motor vehicle in performing different operations on road like hill climbing/acceleration/braking/ towing and reversing operation.

Assignment

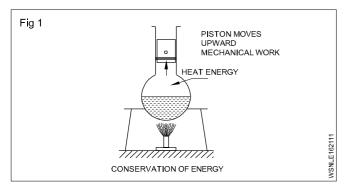
- 1 What is the potential energy in a body of mass 5 kg on top of a pole 20 metre high?
- 2 What is the kinetic energy of a mass of 1 kg moving with velocity if 150 cm/sec?
- 3 The mass of a body is 4 x 10³ kg and it is moving with a velocity 0.1 m/sec. Find out the kinetic energy and mention the unit?
- 4 A bullet of mass 4 grams moves with a speed of 400 m/sec. Calculate the kinetic energy of the bullet and the force required to stop the bullet in 20 cm of distance?
- 5 A bullet of mass 5 grams travel with a speed of 500 m/ sec/ If it penetrates a fixed target which offers a constant resistance of 1000N to the motion of the bullet. Find kinetic energy.
- 6 3 kg of mass is Thrown horizontally and attains the speed of 10 metre per second. Find its kinetic energy.

- 7 The engine of a vehicle 1200 kg moving at 50 km per hour is switched off. calculate the kinetic energy of the vehicle and the distance moved against a resistance of 400 Newton's before coming to stop.
- 8 What is the kinetic energy of mass 3 kg moving with a velocity of 18 km/hour.
- 9 An Iron ball of mass 5 kg is raised to height of 4 metres. If the acceleration due to gravity is 9.8 m/sec2. Calculate the potential energy?
- 10 A total of 4900 joules was expended in lifting a mass of 50 kg. Find the height by which mass was lifted.
- 11 A mass of 5 kg is placed at the height of 30m from the ground. Find the potential energy of the mass in joules.

Heat & Temperature and Pressure - Concept of heat and temperature, effects of heat, difference between heat and temperature, boiling point & melting point of different metals and non-metals

Heat

It is a form of energy. Heat energy can be transformed into other forms of energies. Heat flows from a hotter body to a colder body. (Fig 1)



Units of heat

Calorie: It is the quantity of heat required to raise the temperature of 1 gram of water through 1° C.

BTHU: It is the quantity of heat required to raise 1 lb of water through 1°F. (British thermal unit).

C.H.U; It is the quantity of heat required to raise 1 lb of water through 1°C.

Joule : S.I. Unit (1 Calorie = 4.186 joule)

Effects of heat

- Change in temperature
- Change in size
- Change in state
- Change in structure
- · Change in Physical properties

Specific heat

The quantity of heat required to raise the temperature of one gm of a substance through 1° C is called specific heat. It is denoted by the letter 's'.

Specific heat of water	= 1
Aluminium	= 0.22
Copper	= 0.1
Irc	on = 0.12

Thermal capacity:

It is the amount of heat required to raise the temperature of a substance through 1° C is called the thermal capacity of the substance.

Thermal capacity = ms calories.

Calorific value: The amount of heat released by the complete combustion of unit quantity of the fuel (Mass or volume) is known as calorific value of fuels.

Water equivalent

It is the mass of water which will absorb the same amount of heat as the given substance for the same temperature rise. Water equivalent = Mass of the substance x specific heat of the substance.

Therefore water equivalent = ms

Types of heat

- 1 Sensible heat
- 2 Latent heat
- 1 Sensible heat

Sensible heat is the heat absorbed or given off by a substance without changing its physical state. It is sensible and can be absorbed by the variation of temperature in the thermometers.

2 Latent heat

The heat gained or given by the substance during a change of state (from solid to liquid to gas) is called latent heat or hidden heat. The heat absorbed or given off does not cause any temperature change in the substance.

Types, 1. Latent heat of fusion of solid

2. Latent heat of vaporisation of solid.

1 Latent heat of fusion of solid

The amount of heat required per unit mass of a substance at melting point to convert it from the solid to the liquid state is called latent heat of fusion of solid. Its unit is cal/gram.

Latent heat of fusion of ice

The amount of heat required to convert per unit mass of the ice into water at 0° C temperature is called latent heat of fusion of ice.

Latent heat of fusion of ice(L) = 80 cal/gram

2 Latent heat of vaporisation of liquid

The amount of heat required to vaporise a unit mass of liquid at its boiling point is called latent heat of vaporisation.

Latent heat of vaporisation of water or latent heat of steam

The amount of heat required to convert into steam of a unit mass of water at its boiling point $(100^{\circ}C)$ is called latent heat of vaporisation of water or latent heat of steam.

Latent heat of steam(L) = 540 cal/gram

Temperature

It is the degree of hotness or coldness of a body. The temperature is measured by thermometers.

Difference between heat and temperature

Heat	Temperature
1 It is a form of energy.	This tells the state of heat.
2 Its unit is calorie.	Its unit is degree.
3 Heat is measured by calorimeter.	Temperature is measured by thermometer.
4 By adding quantity of heat of two substances their total heat can be calculated.	By adding two temperatures we cannot find the temperature of the mixture.
5 By heating a substance the quantity of heat is increased regardless of increase in temperature.	Two substances may read the same temperature though they might be having different amount of heat in them.

Melting point

Boiling point

Any substance starts turning into a gas shows the temperature at which it boils this is known as the boiling point. The boiling point of water is 100°C.

The temperature at which any solid melts into liquid or liquid freezing to solid is called the melting point of substance. `The melting point of ice is 0°C.

List of melting point and boiling point of metals and Non -metals

letals and Ion-metals	Melting point °C	Boiling point °C	Metals and Non-metals	Melting point °C
uminium	660.25	2519	Manganese	1246
rgon	-189.19	-185.85	Mercury	-38.72
rsenic	817	614	Molybdenum	2617
arium	729	1897	Nickel	1453
eryllium	1287	2469	Nitrogen	-209.86
romine	-7.1	58.8	Oxygen	-226.65
admium	321.18	767	Phosphorus (white)	44.1
alcium	839	1484	Plutonium	640
arbon (diamond)	3550	4827	Potassium	63.35
arbon (graphite)	3675	4027	Radium	700
hlorine	-100.84	-34.04	Silicon	1410
obalt	1495	2927	Silver	961
opper	1084.6	2562	Sodium	98
iold	1064.58	2856	Sulfur	115.36
elium	-	-268.93	Tin	232.06
ydrogen	-259.98	-252.87	Titanium	1660
dine	113.5	184.3	Tungsten (wolfram)	3422
dium	2443	4428	Uranium	1132
n	1535	2861	Zinc	419.73
ad	327.6	1749		
hium	180.7	1342		
lagnesium	650	1090		

Heat & Temperature and Pressure - Scales of temperature, celsius, fahrenheit, kelvin and conversion between scales of temperature

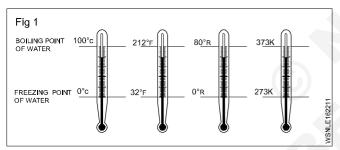
Temperature Scales

Temperature is calibrated between two fixed reference points namely the freezing point of water, and the boiling point of water. These two fixed points on different temperature scales are:

Scale	Freezing point	Boiling point
Centigrade (°C)	0°C	100°C
Fahrenheit (°F)	32°F	212°F
Kelvin (K)	273°K	373°K
Reaumur(°R)	0°R	80°R

Heat is a form of energy. Temperature is the degree of hotness or coldness of a body. The relationship for conversion from one temperature scale to the others is

 $\frac{{}^{\circ}\mathsf{R}}{80} = \frac{{}^{\circ}\mathsf{C}}{100} = \frac{{}^{\circ}\mathsf{K} - 273}{100} = \frac{{}^{\circ}\mathsf{F} - 32}{180}$



1 Convert 0°C into °F

$$\frac{{}^{\circ}F - 32}{180} = \frac{{}^{\circ}C}{100}$$
$${}^{\circ}F - 32 = \frac{{}^{\circ}C}{100} \times 180$$
$${}^{\circ}F - 32 = \frac{0}{100} \times 180$$
$${}^{\circ}F = 0 + 32$$
$$= 32{}^{\circ}F$$
$$0{}^{\circ}C = 32{}^{\circ}F$$

2 Convert -40°C into °F

$$\frac{{}^{\circ}F - 32}{180} = \frac{{}^{\circ}C}{100}$$
$${}^{\circ}F - 32 = \frac{{}^{\circ}C}{100} \times 180$$
$${}^{\circ}F - 32 = \frac{-40}{100} \times 180$$
$$F - 32 = -72$$
$${}^{\circ}F = -72 + 32$$
$$= -40^{\circ}F$$
$$-40^{\circ}C = -40^{\circ}F$$

3 Convert 37ºC into K

$$\frac{{}^{0}C}{100} = \frac{{}^{0}K - 273}{100}$$

$${}^{\circ}K - 273 = C$$

$${}^{\circ}K = C + 273$$

$${}^{\circ}K = 37 + 273$$

$$= 310 K$$

$$37{}^{\circ}C = 310K$$

4 Convert 70°C into Reaumur

$$\frac{{}^{\circ}C}{100} = \frac{{}^{\circ}R}{80}$$
$${}^{\circ}R = \frac{C}{100} \times 80$$
$${}^{\circ}R = \frac{70}{100} \times 80 =$$
$$70{}^{\circ}C = 56{}^{\circ}R$$

56

5 Convert - 25° F into °C

$$\frac{{}^{\circ}C}{100} = \frac{{}^{\circ}F - 32}{180}$$
$$\frac{{}^{\circ}C}{100} = \frac{-25 - 32}{180}$$
$${}^{\circ}C = \frac{-57}{180} \times 100$$
$${}^{\circ}C = \frac{-285}{9} = -31.66$$
$$- 25{}^{\circ}F = -31.7{}^{\circ}C$$

$${}^{\circ}C = \frac{{}^{\circ}F - 32}{180} \times 100$$

$${}^{\circ}C = \frac{98.6 - 32}{180} \times 100$$

$$= \frac{66.6}{180} \times 100$$

$$= \frac{6660}{180} = 37{}^{\circ}C$$
98.6°F = 37°C

Assignment

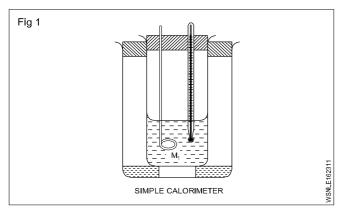
Convert the following 1 $10.5^{\circ}C = \{\circ}F$	13 428°F =°C
$2 40^{\circ}C = {}^{\circ}F$	14 -210ºF =ºC
$3 60^{\circ}C = {}^{\circ}F$	15 88ºF =ºC
$3 80^{\circ}C =$	16 110°F =°C
$4 80^{\circ}C =^{\circ}F$	17 72°F =°C
$5 100^{\circ}C = {}^{\circ}F$	18 50°F =°C
$7 - 80^{\circ}C = _{\circ}F$	19 900°F =°C
7 - 60 C = F 8 200°C = °F	20 72°R =°C
$9 605^{\circ}C = {}^{\circ}F$	21 143ºC =K
$10 \ 1250^{\circ}C = ^{\circ}F$	22 373°K =°C
$10 \ 1230 \ C = \1$ 11 77°F = °C	23 746ºK =ºF
$12 \ 20^{\circ}F ={\circ}C$	24 At what temperature thermometer be dou

24 At what temperature will the reading of a fahrenheit thermometer be double of a centigrade one.

Heat & Temperature and Pressure - Temperature measuring instruments, types of thermometer, pyrometer and transmission of heat - Conduction, convection and radiation

Measuring heat energy

Energy can be released in chemical reactions as light, sound or electrical energy. But it is most often released as heat energy. This allows us to easily measure the amount of heat energy transferred.



The apparatus used to measure the amount of heat by mixer method is called calorimeter. It is nothing but cylindrical shaped vessel and a stirrer made out of mostly copper.

In a calorimeter when the hotter solid/liquid substance are mixed with the cooler solid/liquid substances, heat transfer takes place until both substances reach the same temperature. By the same time calorimeter also reaches the same temperature. By mixing rule,

Loss of heat		Heat absorbed by		
by solid/	=	solid / liquid	+	Heat absorbed by calorimeter
liquid		substance		

Measurement

Temperature is generally measured in degrees Celsius. In this system the freezing point of water is defined as 0°C and the boiling point of water is defined as 100°C. The Kelvin temperature scale begins from absolute 0. i.e. 273°. The temperature intervals are the same.

∴ 273K = 0°C, 20°C = 273K + 20°C = 293K.

Instruments

The instruments used to measure and read temperature takes into account changes in the properties of materials, electrical phenomena incandescence, radiation and melting.

Thermometer

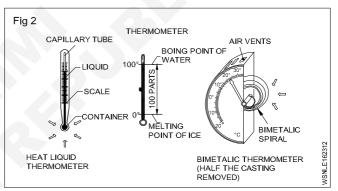
Types of thermometer

- Forehead strips
- Wearable thermometers
- Pacifier thermometers

- Earthermometers (tympanic)
- Forehead thermometers (temporal)
- Digital thermometers
- Mom's hand or lips

They are based on the principle that liquids and solids expand when they are subjected to heat. Mercury and alcohol expand uniformly. When heat is applied the volume of the liquid increases and the liquid rises in the capillary tube integral with the container. Mostly mercury is used in this type of thermometers because of its properties (Shiny and will not adhere to the glass tubes and we can measure up to 300° C.

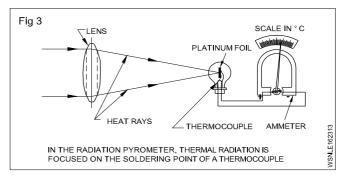
The bimetal thermometer consists of metals with different coefficient of expansion. The bimetal is twisted into a spiral which curls when the temperature rises.

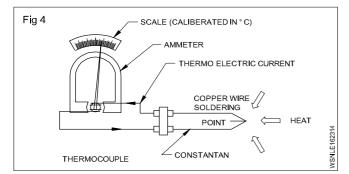


Pyrometer

Thermoelectric pyrometer is based on the principle that the soldering point between the wires of different metals, when heated a contact voltage is generated. The voltage depends upon the temperature difference between the hot measuring point and the cold end of the wire. Thermocouple elements are constructed of copper and Constant (up to 600°C) or of platinum and platinum-rhodium (up to 1600°C)

Radiation pyrometers are used to measure temperatures of red hot metals up to 3000°C. These concentrate thermal rays through an optical lens and focus them on to a thermo element. The scale of the ammeter is calibrated in degrees Celsius or Kelvin.





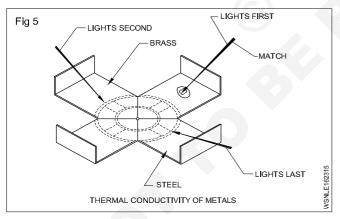
Transmission of Heat

Heat is a form of energy and is capable of doing work. Heat flows from a hot body to a colder body or from a point of high temperature to a point of low temperature. The greater is the temperature difference the more rapidly will be the heat flow. Heat is transmitted in three ways.

- 1 Conduction
- 2 Convection
- 3 Radiation

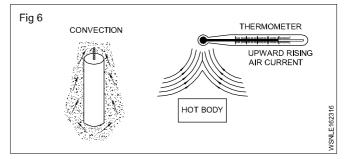
Conduction

Conduction is the name given to the transmission of heat energy by contact. The heat source is in contact with the Conductor. (metal rod). The rod is in contact with a thermometer. Due to Conduction heat is transferred from the heated end to the free end. In general good electrical conductors are also good heat conductors and good electrical insulators are also good heat insulators. A good heat insulator does not necessarily withstand high temperature.



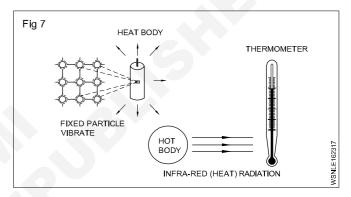
Convection

Convection is the name given to the transmission of heat energy by the up-ward flow. When heated, the fluid (liquid/ gas) becomes less dense and because of its mobility, is displaced upwards, by a similar but colder and more dense fluid. e.g., The domestic hot water system, The cooling system in motor cars.



Radiation

Heat is radiated or transmitted from one object to the other in space without actually being in contact, by means of electro-magnetic waves. These waves are similar to light waves and radio waves. They can be refracted by lenses and reflected by mirrors. This radiation is called infrared. It requires no medium to carry the radiation. (e.g) The heat of the sun travels through the space.



Transmission of heat takes place in three ways Conduction, Convection and Radiation.

Expansion due to heat

When a solid, liquid or gaseous substance is heated, it expands and volume is increased. Similarly when it is cooled, it contracts (shrinks) and volume is decreased.

E.g: small gaps are left in between the lines of railway track to allow for expansion during summer. If this is not done, the rails would expand and bend there by causing derailment of trains.

Except a few substances, all solids, liquids and gases expand. For the same amount of heat given, the expansion of liquids is greater than solid and expansion of gas is more than liquid.

Volume of water is reducing while heating from 0°C to 4°C. After that volume is increasing. The data at 4°C of water will be taken as reference point for any calculations relating with water.

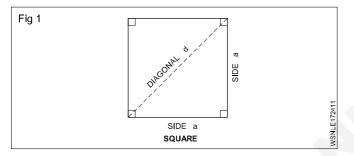
Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.7.24 Mensuration - Area and perimeter of square, rectangle and parallelogram

In Engineering field, an Engineer has to estimate the material, manpower, machinery, etc. required to prepare the geometrical objects. Hence we must be very conversant with all relevant formulae connected with geometrical objects.

Length	- I unit
Breadth or width	ı - b unit
Diagonal	- d unit
Diameter	- d unit

Square

This is also a four sided figure, opposite sides are parallel. All the four sides are equal. Angle between adjustment side are 90°.



 $A = a^2$ (or) unit²

P = 4a unit

$$d = \sqrt{2} a unit$$

a =
$$\frac{d}{\sqrt{2}}$$
 unit where $\sqrt{2}$ = 1.414

Find the area of a brass sheet in the form of a square whose perimeter is 31.2 cm.

∴ a
$$=\frac{31.2}{4} = 7.8 \text{ cm}$$

Area (A) $= a^2$

$$= 7.8 \times 7.8 = 60.84 \text{ cm}^{2}$$

Examples

Find out the circumference, diagonal and area of a 1 square, whose side is 18 cm.

Side of the square (a)=	18 cm	()
Perimeter (P)	=	4a	
	=	4 x 18 = 72 cm	2 nd square
Diagonal (d)	=	$\sqrt{2}$ x a	Side (a)
	=	√2 x 18 = 1.414 x 18	Side (a)
	=	25.45 cm	

Radius	- r unit
Semi perimeter	- S unit
Perimeter	- P unit
Circumference	- C unit
Area	- A unit ²
Total surface are	ea - T.S.A unit²
Lateral surface	area - L.S.A unit²
Volume	- V unit ³

Area(A) =

> 18 x 18 = 324 cm²

Perimeter of square 72 cm =

2 If the diagonal of a square measure 10 cm. Find area of the square.

 a^2

Diagonal of the square (d) = $\sqrt{2}$ a = 10 cm

=

Side (a) =
$$\frac{d}{\sqrt{2}}$$

Area (a²) = $\frac{d}{\sqrt{2}} \times \frac{d}{\sqrt{2}} = \frac{d^2}{2}$
= $\frac{10^2}{2} = \frac{100}{2}$
= 50 cm²
re = 50 cm²

= <u>Perime</u>ter

4

Area of the square

3 The perimeter of one square is 748 cm and that of Another is 336 cm. Find the total area of the two squares.

Side of the square (a)

1stsquare

Side (a)

Area(A)

$$= \frac{\text{Perimeter of } 1^{\text{st} \text{ square}}}{4}$$
$$= \frac{748}{4} = 187 \text{ cm}$$
$$= a^{2}$$
$$= 187 \text{ x } 187$$
$$= 34,969 \text{ cm}^{2}$$

Perimeter of 2nd square 4

$$=\frac{336}{4}=84$$
 cm

Area(A)

= 84 x 84

 $= a^{2}$

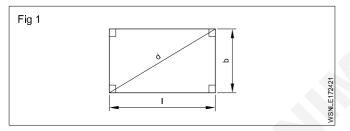
$$= 7,056$$
 cm²

Assignment

- 1 Find the Area, Perimeter and diagonal of a square steel plate whose side measures 28.1 cm.
- 2 Find the area of a square whose diagonal is equal to 8.5 cm.
- 3 Find the area of the square if the side of the square is 28 cm.
- $\label{eq:4} \mbox{ Find its side if the area of the square field is 169 m^2.$
- 5 Find the area of the square if the diagonal of the square is 20 cm.
- 6 Find the perimeter of a square whose diagonal is 144 m.
- 7 Find the area if the perimeter of a square plot is 48 m.

Rectangle

This is a four sided figure. Opposite sides are parallel. Angles between adjacent sides are 90° .



A = Area = length x breadth = l.b.unit²

Diagonal = $\sqrt{I^2 + b^2}$ unit

Examples

1 Find the Area, Perimeter and diagonal of a rectangle whose length and breadth are 144 mm and 60 mm respectively.

Area = A = I x b unit²
= 144 x 60 = 8640 mm²
Perimeter = P = 2 (I + b) unit
= 2(144 + 60)
= 2 x 204 = 408 mm
Diagonal = d =
$$\sqrt{I^2 + b^2}$$
 unit
= $\sqrt{144^2 + 60^2}$
= $\sqrt{20736 + 3600}$
= $\sqrt{24336}$ = 156 mm

2 The perimeter of a rectangle is equal to 42 cm. If its breadth is 9 cm. Find the length of the rectangle.

Perimeter = 42 cm Breath = 9 cm Length = ? Perimeter = P = 2(I + b) 2(I + 9) = 42 $I + 9 = 42 \div 2$ I + 9 = 21 I = 21 - 9I = 12 cm

3 The perimeter of a rectangle is 48 cm and its length is 4 cm more than its width. Find the length and breadth of the rectangle.

Perimeter (P) = 48 cm
Breath (b) = x
Length (l) = x + 4
2(l + b) = Perimeter
2(x + 4 + x) = 48
2(2x + 4) = 48
4x + 8 = 48
4x = 48 - 8
x =
$$\frac{40}{4}$$
 = 10
x = breadth = 10 cm
length = x + 4 = 10 + 4 = 14 cm

4 How many rectangular pieces of 50 cm x 20 cm can be cut out from a sheet of 1000 cm x 500 cm.

Sheet size = 1000 cm x 500 cm

Size of the rectangular piece to be cut = 50 cm x 20 cm

No. of pieces to be cut in lengthwise = $\frac{1000}{50}$ = 20

No. of pieces to be cut in breadthwise = $\frac{500}{20}$ = 25

Total no. of pieces to be cut out $= 20 \times 25$

= 500

5 The perimeter of a rectangle is 320 metre. Its sides are in the ratio of 5:3. Find the area of the rectangle.

Ratio = 5:3 = I : b

Assignment

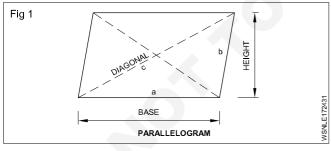
- 1 Find the area of a rectangular plot whose sides are 24 metres and 20 metres respectively. Also find the perimeter of the plot.
- 2 How many rectangular pieces of 5 cm x 4 cm will you get out of 65 cm x 30 cm brass sheet?
- 3 Find its breadth and area if the perimeter of a rectangle is 400 metre and its length is 140 m.
- 4 Find its area, if the opposite sides of a rectangle are 64 cm and 25 cm respectively.

breadth b = 3x2(1 + b)= Perimeter 2(5x + 3x) = 3202(8x)= 320 16x = 320 = $\frac{320}{2}$ = 20 x $I = 5x = 5 \times 20 = 100 \text{ m}$ $b = 3x = 3 \times 20 = 60 m$ (length = 100m, breath = 60m)Area = I x b $= 100 \times 60$ $= 6000 \text{ m}^2$ Area

- 5 What is the width of the rectangle if a rectangle has an area of 224 cm^2 and length 16 cm.
- 6 What is the length of the diagonal of a rectangle with sides 16 cm and 12 cm?
- 7 Find the area of the rectangle if the perimeter of the rectangle is 100 cm and the ratio of its length and breadth is 3:2.

Parallelogram

This is also a four sided figure, opposite side being parallel to each other.



Area of parallelogram = base x height

or =
$$2x\sqrt{s(s-a)(s-b)(s-c)}$$

Where

$$s = \frac{a+b+c}{2}$$

a and b are adjacent sides.

Examples

length I

= 5x

- 1 The base and height of a parallelogram are 7.1 cm and 2.85 cm. Calculate its area.
 - A = base x height units²

2 Find the height of a parallelogram whose area is 20 cm² and base is 10 cm.

$$h = \frac{\text{area}}{\text{base}}$$
$$= \frac{20}{10}$$
$$= 2 \text{ cm}$$

 Two sides of a parallelogram are 12 cm and 8 cm. The diagonal is 10 cm long. Find the area of the parallelogram.

Area A =
$$2x\sqrt{s(s-a)(s-b)(s-c)}$$
 units²
s = $\frac{a+b+c}{2}$
= $\frac{12+8+10}{2}$ Area A
= $\frac{30}{2}$
= 15

A =
$$2 \times \sqrt{15(15-12)(15-8)(15-10)}$$

= $2 \times \sqrt{15 \times 3 \times 7 \times 5}$
= $2 \times \sqrt{1575}$
= 2×39.686
rea A = 79.37 cm^2

Assignment

- 1 Find the area of a parallelogram, if its base and height are 8.1 cm and 30.8 cm respectively.
- 2 Find the area of a parallelogram, if the sides of a field in the shape of parallelogram are 12 m and 17 m and one of the diagonal is 25 m.
- 3 Find the base of a parallelogram whose height is 12 cm and area is 120 cm².
- 4 Find the height of a parallelogram whose base is 40 cm and area is 320 cm².
- 5 Find the area of the land if the sides of a land in the shape of a parallelogram are 24 m and 28 m respectively and one of the diagonal is 30 m.
- 6 What is the perimeter of parallelogram if base is 10 cm and other side is 5 cm?

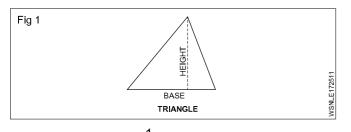
- 7 Find the area of parallelogram if its base and height are 25 cm and 12 cm.
- 8 Find the base of a parallelogram if height is 15 cm and area is 150 cm².
- 9 Find the height of a parallelogram if base is 80 cm and area is 640 cm^2 .
- 10 Find the area of parallelogram if its base and height are 15 cm and 8 cm.
- 11 Calculate the perimeter and area of parallelogram if base, height are 12.7 cm, 5.5 cm and other side is 6.5 cm.
- 12 Find the height of parallelogram if the area is 20 cm² and base is 10 cm.

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.7.25 Mensuration - Area and perimeter of triangles

Triangles

Tri means three. Hence tri- angle means three angled figure. For construction of three angled figure, there should be three sides. Hence triangle means three sided figure. Sum of the three angles of any triangle = 180° .

i Any triangle.

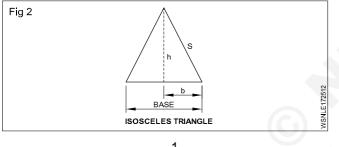


Area of any triangle = $\frac{1}{2}$ x Base x Height unit²



ii Isosceles Triangle

In this triangle two of its sides are equal.



Area of isosceles triangle =
$$\frac{1}{2}$$
 x Base x Height

Where

base = 2.b

s = One of equal sides (or) Slant height

h = Height =
$$\sqrt{s^2 - b^2}$$

Area of isosceles triangle = $\frac{1}{2} \times 2b \times \sqrt{s^2 - b^2}$

$$= b \cdot \sqrt{s^2 - b^2}$$
 unit

(Where b= half of base)

(or) Area of Isosceles triangle = $\frac{1}{4}b\sqrt{4a^2 - b^2}$ unit²

a = Equal sides

iii Equilateral triangle

In this triangle all the three sides are equal. Hence angle between adjacent sides is 60° (Three angles total = 180°)

angle between sides =
$$\frac{180}{3}$$
 = 60°

Fig 3 **VSNLE17251** EQUILATERAL TRIANGLE <u>√</u>3

Area of equilateral triangle =
$$\frac{\sqrt{3}}{4}$$
 x side²

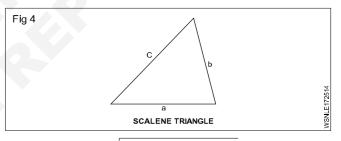
$$=\frac{\sqrt{3}}{4} \times a^2 \text{ unit}^2$$

Where
$$\sqrt{3}$$
 = 1.732
Perimeter P = 3a unit

√3 a uni

iv Scalene triangle

In this triangle the sides are not equal. Angles between the sides, are also not equal. we may also call this triangle as irregular triangle.



Area of triangle = $\sqrt{s(s-a)(s-b)(s-c)}$ unit²

where

F

a,b,c are sides of triangle

s = Semi perimeter =
$$\frac{a+b+c}{2}$$
 unit

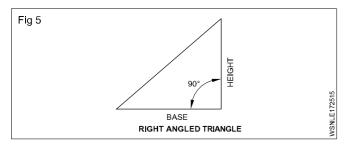
v Right angled triangle

In this triangle, angle between one of two adjacent sides is 90°. Right angle means 90°. That's why right angled triangle means, one of the angles of this triangle is definitely 90°.

Area of right angled triangle

$$= \frac{1}{2} \times \text{Base x Height}$$
$$= \frac{1}{2} \text{bh unit}^{2}$$
Hypotenuse
$$= \sqrt{\text{Base}^{2} + \text{Height}^{2}}$$

60



Where hypotenuse means, the diagonal or largest length of the side of right angled triangle.

Examples

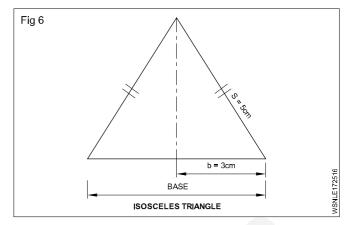
1 Calculate its area if the base and height of a Right angled triangle are 10 cm and 3.5 cm respectively.

Base (b)	= 10 cm
Height (h)	= 3.5 cm
Area (A)	= ?
А	$=\frac{1}{2} x b x h$
	$=\frac{1}{2} \times 10 \times 3.5$
	= 17.5 cm ²

- 2 Calculate the base of a triangle having an area of 15 cm² and height is 3.5 cm.
 - Area (A) = 15 cm² Height (h) = 3.5 cm Base (b) = ? $\frac{1}{2}$ x b x h = A $\frac{1}{2}$ x b x 3.5 = 15 $=\frac{15 \times 2}{2}$ b 3.5 = 8.57 cm
- 3 Calculate the height of a triangle whose area is 60 cm² and base is 10 cm.

Area (A) = 60 cm^2 = 10 cm Base (b) Height (h) = ? 1 2 xbxh = A $\frac{1}{2} \times 10 \times h$ = 60 $=\frac{60 \times 2}{10}$ h height h = 12 cm

4 Find the area of an isosceles triangle whose base is 6 cm long and each of the other two sides 5 cm long.

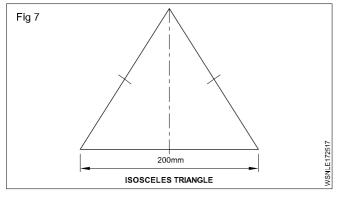


Base (b)	$= 6 \text{ cm} = \frac{6}{2} = 3 \text{ cm}$
Equal sides or slant height 's' Area (A)	= 5 cm = ?
А	$= b x \sqrt{s^2 - b^2}$
	$= 3 \times \sqrt{5^2 - 3^2}$
	$= 3 \times \sqrt{25 - 9}$
	= 3 x \(\sqrt{16}\)
	= 3 x 4
	= 12 cm ²
	or
A	$=\frac{1}{4}b\sqrt{4a^2-b^2}$
	$= \frac{1}{4} \times 6\sqrt{4x5^2 - 6^2}$
	$=\frac{1}{4}\times 6\times 8$
	10 2

= 12 cm²

- 5 Find its height if an isosceles triangle has base of 200 mm and its area is 2000 mm².
 - = 200 mm Base $= 2000 \text{ mm}^2$ Area h = ? xbxh = A $\frac{1}{2}$ x 200 x h= 2000 h = $\frac{2000 \times 2}{200}$ = 20 mm

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6 Find the area of an equilateral triangle whose side is 5 cm.

Area
$$= \frac{\sqrt{3}}{4} a^2 \text{ unit}^2$$

 $= \frac{1.732}{4} \times 5 \times 5$
 $= 10.825 \text{ cm}^2$

7 Calculate its perimeter if one side of an equilateral triangle is 55 mm long.

Side = 55 mm Perimeter (P) = ? P = 3a unit = 3 x 55 = 165 mm

8 Find the area of the triangle having its sides are 9cm, 10cm and 12 cm.

Semi Perimeter = $\frac{a+b+c}{2}$ unit = $\frac{9+10+12}{2} = \frac{31}{2}$

= 15.5 cm

Area A

 $= :\sqrt{s(s-a)(s-b)(s-c)} \text{ unit}^{2}$ $= \sqrt{15.5(15.5-9)(15.5-10)(15.5-12)}$ $= \sqrt{15.5x \ 6.5 \ x \ 5.5 \ x \ 3.5}$ $= \sqrt{1939.4375}$ $= 44.03 \ \text{cm}^{2}$

9 Find the cost of polishing on both sides of a triangular metal plate has sides 60 cm, 50 cm and 20 cm at the rate of Rs.1.35 per 100 cm²

Semi Perimeter =
$$\frac{a+b+c}{2}$$
 unit

$$= \frac{60 + 50 + 20}{2} = \frac{130}{2}$$
$$= 65 \text{ cm}$$
Area A
$$= :\sqrt{s (s - a) (s - b) (s - c)} \text{ unit}^{2}$$
$$= \sqrt{65(65 - 60)(65 - 50)(65 - 20)}$$

 $= \sqrt{65 \times 5 \times 15 \times 45}$

 $= 468.4 \text{ cm}^2$ Area of polish on both sides = 2 x 468.4 = 936.8 cm² Cost of polish per 100 cm² = Rs. 1.35 ∴ Cost of polish is 936.8 cm² = $\frac{936.8}{100} \times 1.35$

- = Rs. 12.65
- 10 Find the area of the right angled triangle with base 20 cm and height 8 cm.

Base b	= 20 cm
Equal sides or slant height	= 8 cm
Area (A)	= ?
Area (A)	$=\frac{1}{2}$ x base x height unit ²
	$=\frac{1}{2} \times 20 \times 8$
	= 80 cm ²

11 Find the area of the right angled triangle if the sides containing the right angle being 10.5 cm and 8.2 cm.

Area (A) $= \frac{1}{2} \times base \times height unit^{2}$ $= \frac{1}{2} \times 10.5 \times 8.2$ $= 43.05 \text{ cm}^{2}$

12 Calculate the perpendicular height of the triangle if the area of the right angled triangle is 19.44 m² and its one of the adjacent side containing the right angle being 5.4 m.

$$\frac{1}{2} x \text{ base x height unit}^2 = \text{Area}$$
$$\frac{1}{2} x 5.4 \text{ x h} = 19.44$$

h =
$$\frac{19.44 \times 2}{5.4}$$

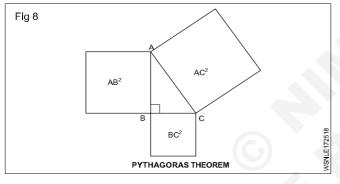
= 7.2 m

13 Calculate the base of a right angled triangle having an area of 12.5 cm². If its height is 2.5 cm.

$$\frac{1}{2} \text{ x base x height unit}^2 = \text{Area}$$
$$\frac{1}{2} \text{ x b x 2.5} = 12.5$$
$$b = \frac{12.5 \times 2}{2.5}$$
$$= 10 \text{ cm}$$

Pythagoras theorem

In a right angled triangle the area of the square drawn with the hypotenuse as the side is equal to the sum of the areas of the squares drawn with the other two sides.



AC = Hypotenuse

AB & BC = Adjacent sides

As per pythagoras theorem,

 $AC^2 = AB^2 + BC^2$

$$\therefore \qquad AC \qquad = \sqrt{AB^2 + BC^2}$$

1 Calculate the hypotenuse of a right angled triangle whose base is 5 cm and height is 12 cm.

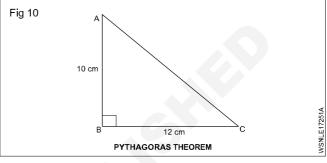
As per pythagoras theorem,

$$AC^{2} = AB^{2} + BC^{2}$$

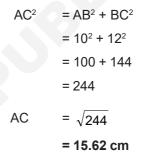
= 12² + 5²
= 144 + 25
= 169
$$AC = \sqrt{169}$$

= 13 cm

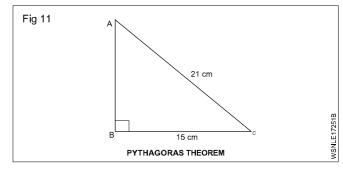
2 What is the length of the hypotenuse of a right angled triangle, when the sides containing the right angles are 10 cm and 12 cm.







3 Find the height of a right angled triangle whose base is 15 cm and hypotenuse is 21 cm.



As per pythagoras theorem,

 $AB^{2} + BC^{2} = AC^{2}$ $AB^{2} + 15^{2} = 21^{2}$ $AB^{2} = 441 - 225$ = 216 $AB = \sqrt{216}$ = 14.7 cm

Mensuration - Area and perimeter of circle, semi-circle, circular ring, sector of circle, hexagon and ellipse

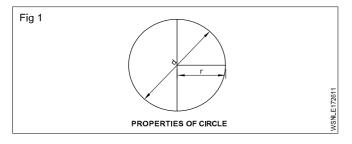
Circle

It is the path of a point which is always equal from its centre is called a circle.

d = diameter of the circle

$$\pi = \frac{22}{7} = 3.14$$

Area of the circle = πr^2



(or)
$$=\frac{\pi}{4} d^2 unit^2$$

Circumference of the circle $2\pi r$ (or) πd unit

Examples

1 Find the area of a circle whose radius is 1.54 m. Also find its circumference.

radius r = 1.54 cm Area A = ? Circumference C = ? $=\pi r^2$ unit² А $=\frac{22}{7} \times 1.4$ = 7.4536 m С = $2\pi r$ unit $= 2 \times \frac{22}{7}$ = 9.68 m 2 Find out the circumference if the a of land is 616 m².

$$A = \pi r^{2} \text{ unit}^{2} \qquad 2r \times \frac{15}{7} = 28$$

$$r^{2} = \frac{616}{\pi} \qquad r = \frac{28x7}{15x2}$$

$$= \frac{616x7}{22} \qquad = 6.53 \text{ cm}$$

 $= \sqrt{196}$ r = 14 m Circumference = $2\pi r$ unit ~ ~

$$= 2 \times \frac{22}{7} \times 14$$

= 88 m

3 Find the side of square into which it can be bent if a wire is in the form of a circle of radius 49 cm.

radius of circle r = 49 cm

side of square = ?

1-

Perimeter of the square = Perimeter of the circle

$$4a = 2\pi r$$

$$4a = 2 \times \frac{22}{7} \times 49$$

$$4a = 308$$

$$a = \frac{308}{4}$$

$$= 77 \text{ cm}$$

Find its radius if the difference between the 4 circumference and diameter of a circle is 28 cm.

Circumference - Diameter = 28 cm

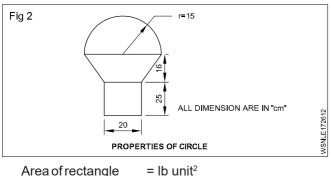
	$2\pi r - d = 28$
.54 x 1.54	$2\pi r - 2r = 28$
m ²	2r (π - 1)= 28
x 1.54	$2r(\frac{22}{7}-1)=28$
area of a circular shape	$2r(\frac{22-7}{7}) = 28$
2	$2r \times \frac{15}{7} = 28$
	$r = \frac{28x7}{15x2}$
	= 6.53 cm

5 What is the side of the largest square cut out from a circle of 50 cm dia.?

Diagonal of a square = Diameter of the circle

$$\sqrt{2}a$$
 = 50
 $a = \frac{50}{\sqrt{2}}$
 $= \frac{50}{1.414}$
= 35.36 cm

6 Calculate the area of the figure given below.



Area of Trapezium =
$$\frac{1}{2} x (a + b) h$$

= $\frac{1}{2} x (30 + 20) 16 \text{ cm}^2$

Semi circle

A semi circle is a sector whose central angle is 180°. Length of arc of semi circle.

Length of arc
$$\ell = 2\pi r \times \frac{180}{360}$$

 $= 2\pi r \times \frac{1}{2} = \pi r$ unit
Area of semi circle $= \frac{\pi r^2}{2}$ Sq. units
Fig 3
Fig 3
Fig 3
Perimeter of a semi circle $= \frac{2\pi r}{2} + 2r$
 $= \pi r + 2r$
 $= r (\pi + 2)$ unit

$$=\frac{1}{2} \times 50 \times 16 \text{ cm}^2$$

= 400 cm²

Area of Semi circle = $\frac{\pi r^2}{2}$ unit²

$$= \pi x 15^2 x \frac{1}{2} \text{ cm}^2$$
$$= 353.57 \text{ cm}^2$$

Total area of the figure = 500 + 400 + 353.57

7 Find the area of remaining steel plate if in a rectangular steel plate 16 cm x 12 cm, there are 6 holes each 4 cm in diameter.

Area of a rectangular plate = length x breadth unit²

$$= 16 \times 12$$
$$= 192 \text{ cm}^2$$
No. of holes = 6
Radius of hole = 2 cm
Area of 6 holes = 6 x πr^2 unit²

 $= 6 \times \frac{22}{7} \times 2 \times 2$ unit²

Area of remaining plate = 192 - 75.43

= 116.57 cm²

Examples

1 Calculate the circumference and area of a semi circle whose radius is 6 cm.

radius r = 6 cm
Area A = ?
Circumference c = ?
A =
$$\frac{\pi r^2}{2}$$
 unit²
 $= \frac{22}{7} \times \frac{1}{2} \times 6^2$
Area (A) = $\frac{22}{7} \times \frac{1}{2} \times 36$
 $= \frac{396}{7} = 56.57$ cm²
Perimeter of a semicircle = $\frac{2\pi r}{2} + 2r = \pi r + 2r$

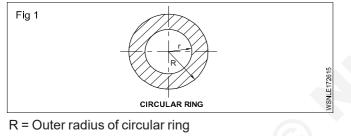
WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.7.26

= r (
$$\pi$$
 + 2) = 6 ($\frac{22}{7}$ + 2)
= 6 $\left(\frac{22+14}{7}\right)$
= 6 x $\frac{36}{7}$
= $\frac{216}{7}$
= 30.86 cm

2 From the figure given below ABCD is a steel plate, a semi circular plate of radius 50 mm has been prepared by gas cutting. Find the waste area.

Plate length AB	= 100 mm
Breadth BC	= 50 mm
Radius	= 50 mm

Circular ring



Area of circular ring =
$$\pi$$
 (R² - r²) unit²
or

 $A = \pi (R + r) (R - r) unit^{2}$

1 Calculate the area of cross section of pipe having outside dia of 17 cm and inside dia of 14 cm.

Given:

Outer dia of pipe = 17 cm

Outer radius of pipe (R) =
$$\frac{17}{2}$$
 = 8.5 cm
Inner dia of pipe = 14 cm

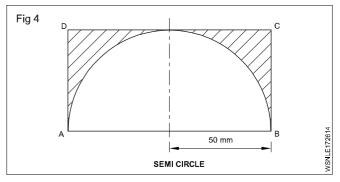
Inner radius of pipe (r) =
$$\frac{14}{2}$$
 = 7 cm

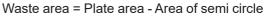
To find:

Area of cross section of pipe = ?

Solution:

Area of cross section of pipe = π (R + r) (R - r) unit² = π (8.5 + 7) (8.5 - 7) = $\frac{22}{7}$ x 15.5 x 1.5 cm² = 73 cm²





$$= lb - \frac{\pi r^2}{2}$$

= 100 x 50 - $\frac{22 x 50 x 50}{7 x 2}$
= 5000 - 3928.57
= 1071 43 mm²

2 Find the distance between the boundaries and the area of the circular ring, if the circumference of two concentric circle are 134 cm and 90 cm.

Given:

Circumference of outer circle = 134 cm

Circumference of inner circle = 90 cm

To find:

Distance between the circles = ?

Area of circular ring = ?

Solution:

Circumference of outer circle = 134 cm $2\pi R$ = 134 cm

$$R = \frac{134}{2\pi} = 21.32 \text{ cm}$$
Circumference of inner circle = 90 cm
 $2\pi r = 90 \text{ cm}$
 $r = \frac{90}{2\pi} = 14.32 \text{ cm}$
Distance between the circle = R - r
 $= 21.32 - 14.32 \text{ cm}$
 $= 7 \text{ cm}$
Area of circular ring = $\pi (R + r) (R - r) \text{ unit}^2$
 $= \pi (21.32 + 14.32) (21.32 - 14.32) \text{ cm}^2$
 $= \frac{22}{7} \times 35.64 \times 7 \text{ cm}^2$

= 784.08 cm²

WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.7.26

3 A wire can be bend in the form of a circle of radius 56 cm. If it is bend in a form of a square, find the side.

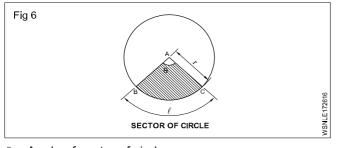
Given:

	Radius of circle	= 56 cm	
To find:			
	Side of square	= ?	

Solution:

Radius of circle = 56 cm

Sector of Circle



 θ = Angle of sector of circle

I = Arc length

r = radius

Length of Arc
$$\ell = \frac{0}{360^{\circ}} \times 2\pi r$$
 unit

Perimeter P = 2r + ℓ unit

Area = $\frac{\theta}{360^{\circ}} \times \pi r^2$ unit² (or) A = $\frac{\ell r}{2}$ unit²

1 Find the perimeter and area of a sector of circle of radius 7 cm and its angle is 120°.

Given:

Angle of sector of circle $= 120^{\circ}$ Radius = 7 cm

To find:

Perimeter = ? , Area = ?

Solution:

Length of arc $(\ell) = \frac{1}{360^{\circ}} \times 2\pi r$ unit

$$=\frac{120}{360} \times 2 \times \frac{22}{7} \times 7 \text{ cm}$$

Perimeter =
$$2r + \ell$$
 unit

$$= 2 \times 7 + 14.67 \text{ cm}$$

Area

Area =
$$\frac{120^{\circ}}{360^{\circ}} \times \frac{22}{7} \times 7^2 \text{ cm}^2 = 51.33 \text{ cm}^2$$

= 360° x πr^2 unit²

Circumference of circle = $2\pi r$ unit = $2\pi x$ 56 cm

Side of square
$$= x \text{ cm}$$

Wire can be bend from the form of round to square

$$a = \frac{352}{4} = 88 \text{ cm}$$

2 Find the radius of the circle if the angle is 60° and the area of a sector of a circle is 144 cm²,

Given:

Area of sector of circle (A) = 144 cm²

Angle of sector of circle $\theta = 60^{\circ}$

To find:

Radius of circle = ?

Solution:

Area (A) = $\frac{\theta}{360^{\circ}} \times \pi r^2$ unit² 144 = $\frac{60^{\circ}}{360^{\circ}} \times \frac{22}{7} \times r^2$ cm² r² = 274.91 cm² r = $\sqrt{274.91}$ = 16.58 cm

3 Find the area of the sector whose angle is 105°, and the perimeter of sector of circle is 18.6 cm.

Given:

Perimeter of a sector of a circle = 18.6 cm

Angle of sector of circle = 105°

To find:

Area = ?

Solution:

Length of Arc
$$(\ell) = \frac{\theta}{360^{\circ}} \times 2\pi r$$
 unit

$$\ell = \frac{103}{360^{\circ}} \times 2 \times \frac{22}{7} \times r$$
= 1.83r
Perimeter (P) = ℓ + 2r unit
18.6 = 1.83r + 2r
3.83r = 18.6 cm
r = $\frac{18.6}{3.83}$ = 4.86 cm

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Area A =
$$\frac{\theta}{360^{\circ}} \times \pi r^2$$
 unit²
= $\frac{105^{\circ}}{360^{\circ}} \times \frac{22}{7} \times (4.86) \text{ cm}^2$
= 21.65 cm²

4 Find the area, if the radius is 12.4 cm and the perimeter of a sector of a circle is 64.8 cm.

Given:

Perimeter P = 64.8 cm = 12.4 cm Radius r

To find:

Solution:

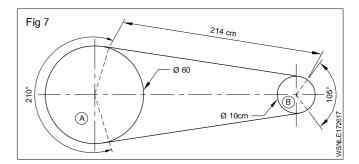
l

Area A

= P - 2r unit
= 64.8 - 2 (12.4) cm
= 64.8 - 24.8 = 40 cm
=
$$\ell r$$
 unit² =

 $= \ell + 2r$ unit

5 Find out the length of the belt, if the arrangement of a belt is shown in the figure below.



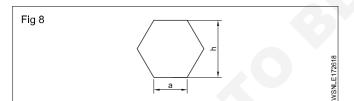
Solution:

Length
$$\ell_{A} = \frac{\theta}{360^{\circ}} \times 2\pi r$$
 unit
$$= \frac{210^{\circ}}{360^{\circ}} \times 2 \times \frac{22}{7} \times 30 = 110$$

Length $\ell_{B} = \frac{\theta}{360^{\circ}} \times 2\pi r$ unit

$$= \frac{105^{\circ}}{360^{\circ}} \times 2 \times \frac{22}{7} \times 5 = 91.7 \text{ cm}$$
$$= \ell_{A} + \ell_{B} + 2 \times 214 \text{ cm}$$
$$= 110 + 9.17 + 428 \text{ cm}$$
$$= 547.17 \text{ cm}$$

Hexagon



2

= 248 cm²

Side = a unit

Perimeter P = 6a unit

Area A =
$$6 \times \frac{\sqrt{3}}{4} \times a^2$$
 units² (Area of 6 equilateral triangle)

DAF (Distance Across Flats) = $\sqrt{3} \times a$ unit

DAC (Distance Across Corners) = 2 x a unit

1 Find out the perimeter, area, DAF and DAC of a regular hexagon whose side is 2cm.

(DAF - Distance Across Flats)

(DAC - Distance Across Corners)

Given: Side of hexagon (a) = 2cm

To Find: P = ?, A = ?, DAF = ?, DAC = ? Solution: = 6a unit

Perimeter of hexagon (P)

= 6a unit = 6 x 2 cm = 12 cm

cm

Area of hexagon A

=
$$6 \times \frac{\sqrt{3}}{4} \times a^2$$
 unit²

$$= 6 \times \frac{1.732}{4} \times 2^2$$

DAF (Distance Across $=\sqrt{3} \times a$ unit Flats)

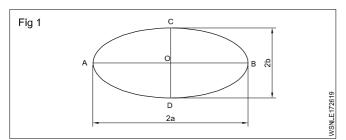
$$= \sqrt{3 \times 2} = 1.732 \times 2$$

= 3.464 cm

DAC (Distance Across Corners) = $2 \times a$ unit

= 2 x 2 = 4 cm

Ellipse



Major axis AB = 2a

```
Half of Major axis OB = a,
```

Minor axis CD = 2b

Half of Minor axis OC = b

Area of ellipse A = π x a x b unit²

Perimeter of ellipse P = $2\pi \sqrt{\frac{(a^2 + b^2)}{2}}$ unit

1 Find its area and perimeter, if the major and minor axis of an ellipse are 12 cm and 8 cm respectively.

Solution:

Major axis 2a = 12 cm
a =
$$\frac{12}{2}$$
 = 6 cm

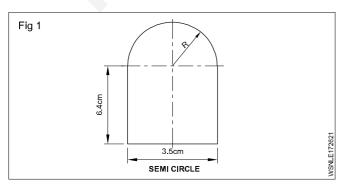
Assignment

Circle

- 1 Find the circumference and area of a circle whose radius is 10 metre.
- 2 Find its diameter if the area of a circle is 330 cm².
- 3 Find its area if the circumference of a circle is 50 cm.
- 4 Find out the area and circumference of a circle of diameter is 50 cm.
- 5 Find its area if the circumference of a circle is 44 cm.

Semi circle

- 1 Calculate the circumference and area of semi circle whose radius is 14 cm.
- 2 Find area of the given figure.



Minor axis 2b = 8 cm
b =
$$\frac{8}{2} = 4$$
 cm
Area A = π x a x b unit²
= $\frac{22}{7}$ x 6 x 4 cm²
= 75.43 cm²
eter (P) = $2\pi \sqrt{\frac{(a^2 + b^2)}{2}}$ unit
= $2 \times \frac{22}{7} \sqrt{\frac{(6^2 + 4^2)}{2}}$ unit
= $2 \times \frac{22}{7} \sqrt{\frac{36 + 16}{2}}$ unit
= $2 \times \frac{22}{7} \times \sqrt{26}$
= $2 \times \frac{22}{7} \times 5.1 = 32.06$ cm

Circular ring

Perimete

- 1 Find out area of a ring washer, whose inner radius and outer radius are 13 cm and 15 cm respectively.
- 2 Find the area of a ring portion of a washer whose outer dis is 30 m and inner dis is 20 m. Also calculate the difference between the circumference of circles.

Sector of circle

- 1 Find the perimeter and area of a sector of a circle of radius 5cm and its angle is 96°.
- 2 Find the radius of the circle if the angle is 90° and the area of sector of a circle is 196 cm^2 .

Hexagon

- 1 Find out the Area, perimeter, DAF, and DAC of hexagon of side 4cm.
- 2 Find the area of cross section of a regular hexagon rod whose side is 7.5 cm.

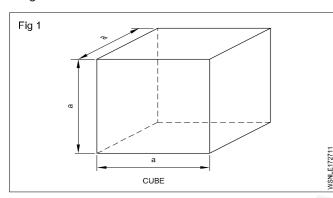
Ellipse

- 1 Find the area of the biggest ellipse that can be inscribed in a rectangle of length 18 cm and breadth 12 cm. Also calculate its perimeter.
- 2 How much fencing will be required to enclose an elliptical plot of ground the axes of the ellipse being 200 and 170 meter respectively.

Cube

All sides of cube are same i.e length,breadth and height have same value. It is bounded by six equal square faces.

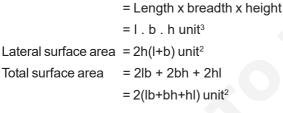
Volume of cube = side x side x side = a^3 unit³ Lateral surface area = $4a^2$ unit² Total surface area = 6 x side x side = $6a^2$ unit² $\sqrt{3} = 1.732$ Diagonal d = $\sqrt{3}a$

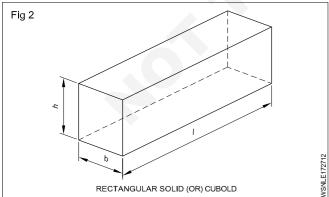


Rectangular solid (or) cuboid

Rectangular soild is bounded by six rectangular surfaces and opposite surfaces are equal and parallel to each other.

Volume of rectangular solid



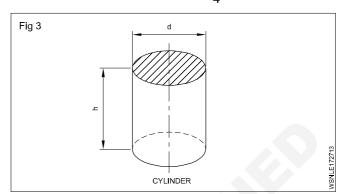


I = Iength, b = breadth and h = height

Cylinder

This is a prism whose top and bottom surfaces are equal and circular.

Volume of cylinder = $\pi r^2 h$ or $\frac{\pi}{4} d^2 h$



Curved area of cylinder = 2π rh unit²

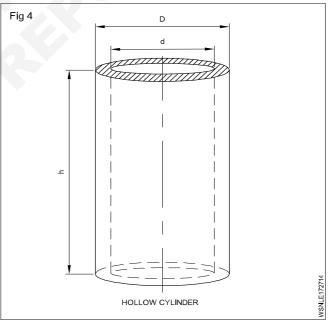
Total surface area of cylinder = $2\pi r(h+r)$ unit²

r = Radius of base , d = Diameter of base

h = Height of cylinder

Hollow cylinder

Hollow means empty space. In hollow cylinder there is an empty place. Water pipe is an example of hollow cylinder.



Volume of hollow cylinder = π (R² - r²) h (or) = π (R + r) (R - r) h (or)

$$= \frac{\pi}{4} (D^2 - d^2) h unit^3$$
$$= \frac{\pi}{4} (D + d)(D - d) h$$

Total surface area of hollow cylinder =

Inner + outer curved area + area of top and bottom circular part

$$\therefore$$
 TSA : 2π Rh + 2π rh + 2π (R² - r²)

R = outer radius

r = inner radius

D = outer diameter

d = inner diameter

h = height of cylinder

Mean dia = $\frac{D-d}{2}$

If thickness given then:

Volume of hollow cylinder = π x mean dia x thickness x height

Finding out volumes of solids

The space occupied by a body is known its volume. The volume of a body indicates the capacity to hold substance in it.

The general form of Lateral surface area Total surface area and Volume is :

Lateral surface area = perimeter of the base x height

Total surface area = LSA + 2 (base area)

Volume = Area of base x height

Important and commonly used solids are described below one after another:

Cube

1 Find the diagonal, lateral surface area,, total surface area and volume of a cube of side 4.5 cm.

	side a	= 4.5 cm
	diagonal d	$=\sqrt{3}$ a unit
		= 1.732 x 4.5
		= 7.794 cm
	L.S.A	= 4a ² unit ²
		= 4 x 4.5 x 4.5
		= 81 cm ²
	T.S.A	= 6a² unit
		= 6 x 4.5 x 4.5
		= 121.5 cm ²
	V	= a ³ unit ³
		= 4.5 x 4.5 x 4.5
		= 91.125 cc.
2	Calculate volume of	a cube where side is 9 cm
	-	- 0

= 9 cm а V = ? $= a^{3}$ V

- 3 Find out side of the cube if a cube has volume of 3375cm³.
 - = 3375 cm³ V = ? а a³ = 3375 = ³√3375 а $=\sqrt{3x3x3x5x5x5}$ $= 3 \times 5$ = 15 cm
- 4 Find the side of a cube, if its surface area is 216 cm²

Surface area = T.S.A = 216 cm² 6a² = 216

а

$$a^{2} = \frac{216}{6}$$
$$= 36$$
$$a = \sqrt{36}$$
$$= 6 \text{ cm}$$

5 Find the side of the square tank, if its height is 2 metre and has the capacity to hold 50,000 litre of water.

Height of square shape tank	: (h) =	2 m
Capacity	=	50,000 litre
1000 litre	=	1 m³
50,000 Litre	=	50000 1000
	=	50 m ³
Capacity of tank	: =	50 m ³
a² x h	=	50
a² x 2	=	50
a²	=	$\frac{50}{2}$ = 25 m ²
а	=	√25 = 5 m

Side of the square tank = 5 m

Rectangular Solid (or) Cuboid

1 Find its volume and T.S.A if a tank is 20 m long, 15 m broad and 12 m high.

Ι	= 20m
b	= 15 m
h	= 12 m
V	= ?
T.S.A	= ?

Volume v = Ibh unit³

= 20 x 15 x 12

= 3600 m³

- T.S.A = 2(lb + bh + hl) unit²
 - $= 2((20 \times 15) + (15 \times 12) + (20 \times 12))$
 - = 2 (300 + 180 + 240)
 - = 1440 m²
- 2 Find out its height if the cross section is 260 mm length and 180 mm wide rectangular and the capacity of a fuel tank is 10500 cm³.

I = 260mm = 26 cm

- b = 180 mm =18 cm
- v = 10500 cm³
- h = ?
- I.b.h = volume

$$h = \frac{10500}{26 \times 10}$$

3 How many litres of water it can store if a water tank has the following dimensions length = 1 metre, width = 0.8 metre and height = 1.2 metre?

Volume = $I x b x h unit^3$

- = 1 x 0.8 x 1.2 = 0.96 m³ [1 m³ = 1000 litres]
 - = 0.96 x 1000

= 960 litres of water can store in the tank.

4 Find its volume if the base of a prism is a rectangle having 5m length, 4m breadth and the height of the prism is 15m.

The base of prism is rectangle

- Area of base = length x breadth
 - = 5 x 4
 - = 20 square m

Volume of prism = Area of base x Height

Cylinder

1 Find the volume and total surface are of a cylinder having 9cm diameter and 15 cm height.

diameter	= 9 cm
radius r	= 4.5 cm
height h	= 15 cm
Volume V	= ?

T.S.A = ?
V =
$$\pi r^2 h \text{ unit}^3$$

= $\frac{22}{7} \times 4.5 \times 4.5 \times 1$
= 954.4 cm³
T.S.A = $2\pi r(h+r) \text{ unit}^2$
= $2 \times \frac{22}{7} \times 4.5 (15 + 22)$

$$= 2 \times \frac{22}{7} \times 4.5 \times 19.5$$

= 551.4 cm²

5

4.5)

2 Calculate the radius if the curved surface area of a cylindrical roller is 48π cm² and the roller is 10 cm long

C.S.A	$= 48\pi \text{ cm}^2$
length	= 10 cm
radius	= ?
2πrh	= 48π
$2 \times \pi \times r \times 10$	= 48π
г	$=\frac{48 \times \pi}{2 \times \pi \times 10}$

= 2.4 cm

3 Find its radius if the volume of a cylinder is 5544 cm³ and its height is 16 cm.

$\pi r^2 h$	= v
3.14 x r ² x 16	= 5544
r ²	$=\frac{5544}{3.14 \times 16}$
r ²	$=\frac{5544}{50.24}$ = 110.35
r	= √110.35 = 10.5 cm

4 Find the diameter of the tank if the volume of a circular tank is 68.46 m³, its height is 2 m.

= 68.46
$=\frac{68.46}{3.14x2}$
= 10.9
$= \sqrt{10.9}$
= 3.3 m
= 2r
= 2 x 3.3
= 6.6 m

5 A cylindrical vessel is to be made of 3 metre long and 1.9994 metre diameter. Calculate its total surface area, if it is in a closed form on one end.

h = 3m d = 1.9994 m r = 0.9997 m T.S.A = C.S.A + Base area = $2\pi rh + \pi r^2$ = $(2 \times \frac{22}{7} \times 0.9997 \times 3) + (\frac{22}{7} \times 0.99997^2)$ = 18.85 + 3.14 = **21.99 m**²

6 How many litres of water a cylinder of radius 75 cm and height 100 cm can hold.

V

radius 17.5 cm.

$$= \pi r^{2} h \text{ unit}^{3}$$

$$= 3.142 \text{ x } 75 \text{ x } 75 \text{ x } 100$$

$$= 1767375 \text{ cm}^{3}$$

$$= \frac{1767375}{1000} [1000 \text{ cc} = 1 \text{ litre}]$$

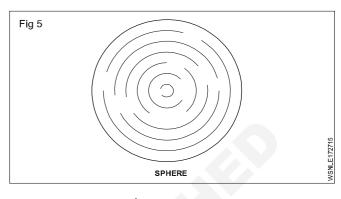
$$= 1767.375 \text{ litres.}$$

Gas contain in 17678.57 cm³ = 17678.57 x 120

Volume of oxygen = 2121428 cc.

Sphere

Sphere is a solid circular body.



Volume of sphere =
$$\frac{4}{3}\pi r^3$$
 or

$$\frac{\pi}{6}$$
d³ unit³

Total surface area of sphere = $4\pi r^2$ unit²

Where r = Radius of sphere

d = Diametre of sphere

Radius = $\frac{1}{2}$ of diameter

1 Find the volume and surface area of a sphere of 3 cm radius.

$$V = \frac{4}{3}\pi r^{3} \text{ unit}^{3}$$
$$= \frac{4 \times 22 \times 3 \times 3 \times 3}{3 \times 7}$$
$$= 113.1 \text{ cm}^{3}$$
$$= 4\pi r^{2} \text{ unit}^{2}$$
$$= 4 \times \frac{22}{7} \times 3 \times 3$$
$$= 113.1 \text{ cm}^{2}$$

2 Find the diameter of sphere having volume of 15625 cc.

$$\frac{4}{3}\pi r^{3} = \text{Volume}$$
$$\frac{4}{3} \times \frac{22}{7} \times r^{3} = 15625$$
$$r^{3} = \frac{15625 \times 3 \times 7}{4 \times 22}$$

Volume of cylinder = Volume of rectangular box

7 Calculate the height of cylindrical tin if a closed rectangular box 40 cm long, 30 cm wide and 25 cm

deep has the same volume as that of cylinder tin of

= l x h x h

$$\frac{22}{7} \times 17.5 \times 17.5 \times h = 40 \times 30 \times 25$$

 $\pi r^2 h$

h

$$= \frac{40 \times 30 \times 25 \times 7}{22 \times 17.5 \times 17.5}$$
$$= \frac{210000}{6737.5}$$
$$= 31.17 \text{ cm}$$

8 An oxygen cylinder is 15 cm in diameter and 100 cm in length. It is filled with gas under pressure so that every cm³ of the cylinder contains 120 cm³ of gas. How much cc of oxygen does this hold?

Volume of cylinder = πr^2 h unit³

$$= \frac{22}{7} \times 7.5 \times 7.5 \times 100$$
$$= 17678.57 \text{ cm}^3$$

Gas contain in 1 cm³ = 120 cm³ of gas

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$$= \frac{328125}{88}$$

$$= 3728.69$$

$$r = \sqrt[3]{3728.69}$$

$$= 15.51 \text{ cm}$$
diameter
$$= 2 \text{ x radius}$$

$$= 2 \text{ x 15.51}$$

$$= 31.02 \text{ cm}$$

3 How many spherical balls of 1 cm radius can be made from a sphere of 32 cm diameter.

No. of balls x volume of small sphere = Volume of bigger sphere

$$N \times \frac{4}{3} \times \pi r^{3} = \frac{4}{3} \pi r^{3}$$

$$N \times \frac{4}{3} \times \not r \times 1^{3} = \frac{4}{3} \times \not r \times r^{3}$$

$$N = 16 \times 16 \times 16$$

= 4096 balls

4 Three brass balls of diameters 3 cm, 4 cm and 5 cm are melted and make into one solid ball, if there is no wastage. Find the diameter of the solid ball.

Assignment

Cube

- 1 Find the diagonal, lateral surface area, total surface area and volume of cube, whose side is 15 cm.
- 2 Find the volume of 10 cubes where each side is 5 cm.
- 3 Find its volume if a solid cube has each of its sides 60 mm long.
- 4 What is its side if the total surface area of a cube is 384 m^2 .

Cuboid

- 1 Find the volume of the tank in m³, if the length is 60 m, breadth 40 m and height 20 m.
- 2 Find the volume of a C.I. casting of a rectangular block having 25 cm x 20 cm x 8 cm size.
- 3 Calculate the total surface area of a box whose length, width and height are 120 cm, 50 cm and 60 cm respectively.
- 4 Find the volume of the sheet if a brass sheet is of 25 cm square and 0.4 cm thick.

$$\begin{array}{rl} 1^{\rm st} \, {\rm ball} \, {\rm d}_1 & = 3 \, {\rm cm}, \\ {\rm r}_1 & = 1.5 \, {\rm cm} \\ 2^{\rm nd} \, {\rm ball} \, {\rm d}_2 & = 4 \, {\rm cm}, \\ {\rm r}_2 & = 2 \, {\rm cm} \\ 3^{\rm rd} \, {\rm ball} \, {\rm d}_3 & = 5 \, {\rm cm}, \\ {\rm r}_1 & = 2.5 \, {\rm cm} \end{array}$$

Diameter of new ball = ?

Volume of new ball = Volume of 3 spherical balls

$$\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi r_{1}^{3} + \frac{4}{3}\pi r_{2}^{3} + \frac{4}{3}\pi r_{3}^{3}$$

$$\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi r_{1}^{3} + \frac{4}{3}\pi r_{3}^{3}$$

$$r^{3} = 3.375 + 8 + 15.625$$

$$r^{3} = 27$$

$$r = \sqrt[3]{27}$$

$$r = \sqrt[3]{27}$$

$$r = 3\sqrt{27}$$

$$r = 3 \text{ cm}$$
there of the ball = 2 x r
= 2 x 3
= 6 \text{ cm}

Cylinder

Diame

- 1 Find the curved surface area of cylinder whose diameter is 18 cm and height 34 cm?
- 2 Find the total surface area of cylinder whose diameter is 24 cm and height 40 cm?
- 3 Find out the volume of cylinder whose base is 10 cm radius and height is 40 cm?

Sphere

- 1 Find the volume of sphere having diameter 3.5cm?
- 2 Find the total surface area of a sphere having radius 1.75 cm?
- 3 How many spherical balls of 1 cm radius can be made from a sphere of 16 cm diameter.
- 4 Three balls of diameter 2m, 4cm and 6 cm are melted and made into one solid ball. If there is no wastage, find the diameter of solid ball.

Trigonometry - Measurement of angles

Introduction:

Trigonometry is the branch of mathematics which deals with the study of measurement and relationship of the three sides and three angles of a triangle.

Units:

Measurement of Angles

There are three systems of measuring the angle:

(i) Sexagesimal System

This is called British System. In this system, one right angle is divided into 90 equal parts which are called degrees.Each part is divided into 60 parts which are called minutes.Each minute is divided into 60 parts which are called seconds.The parts so divided respectively are called:

One degree (1°) , one minute (1') and one second (1")

It means 1 right angle = 90° (90 degrees)

1 degree $(1^\circ) = 60' (60 \text{ minutes})$

1 minute (1') = 60" (60 seconds)

In Trigonometry, mostly this system is used.

(ii) Centesimal System

This is called French System. In this system, the right angle is divided into 100 equal parts which are called grades. Each grade is divided into 100 minutes and each minute is divided into 100 seconds.

Parts so divided are respectively called:

One grade (1 g), one minute (1'), one second (1").

It means 1 right angle = 100 grades (100g)

This system is easier than Sexagesimal System. But to use this system many other systems will have to be devised that is why this system is not used.

(iii) Circular System

In this system, the unit of measuring angles is radian. It is that angle which is formed at the centre and is formed of an arc of length equal to radius in a circle.

There is one constant ratio between the circumference and dia of a circle. This is represented by $\,\pi$.

$$\frac{\text{Circumference}}{\text{Diameter}} = \text{constant point} = \pi$$
Circumference = π x dia
= $2\pi r$ (where r is radius of the circle)
 $\pi = \frac{22}{7}$

Circumference makes an angle $(2\pi r) = 360^{\circ}$

Radius of the circle makes an angle (r) = 1 Radian

ie :
$$\frac{C}{r} = \frac{360^{\circ}}{1 \text{Radian}}$$

 $\frac{2\pi r}{r} = \frac{360^{\circ}}{1 \text{Radian}}$
 $2\pi = \frac{360^{\circ}}{1 \text{Radian}}$
 $2\pi = \frac{360^{\circ}}{1 \text{Radian}}$
 $2\pi \text{ Radian} = 360^{\circ}$
 $\pi \text{ Radian} = 180^{\circ}$
 $1 \text{ Radian} = \frac{180^{\circ}}{\pi}$
 $1^{\circ} = \frac{\pi}{180^{\circ}} \text{ Radian}$

Examples

1 Convert 45°36'20" into degree and decimal of degree.

$$60 \text{ seconds} = 1 \text{ minute}$$

$$20 \text{ seconds} = \frac{20}{60} = 0.333'$$

$$60 \text{ minutes} = 1 \text{ degree}$$

$$36.333 \text{ minutes} = \frac{36.333}{60} = 0.606'$$

$$45^{\circ}36'20'' = 45.606^{\circ}$$

2 Convert 24.59° into degree, minute and second

1 degree = 60 minutes 0.59 degree = 0.59 x 60 = 35.4' 1 minute = 60 seconds 0.4 minute = 60 sec x 0.4 = 24"

Therefore $24.59^{\circ} = 24^{\circ}35'24''$

3 Change 50º37'30" into degrees

By changing angle degrees into decimals

$$30" = \frac{30}{60} = 0.50'$$
$$37'30" = 37.5'$$

$$37.5' = \frac{37.5}{60} = 0.625^{\circ}$$

50°37'30" = 50.625°

4 Convert 23°25' 32" into radians We know 1° = 60' = 3600" Therefore 23°25'32"

$$= \left(23 + \frac{25}{60} + \frac{32}{3600}\right) \text{ degrees}$$
$$= \frac{82800 + 1500 + 32}{3600}$$
$$= \frac{84332}{3600}$$

But 180° = π radians

Therefore 23.4255 degrees

$$= \frac{23.4255}{180} \pi \text{ radians}$$
$$= \frac{23.4255}{180} \times \frac{22}{7} \text{ radians}$$
$$= 0.4089 \text{ radians}$$

5 Convert 87º19' 57" into Radian.

$$19'57'' = 19' + \frac{57''}{60}$$

= 19' + 0.95'
= 19.95'
$$87^{\circ}19.95' = 87^{\circ} + \frac{19.95'}{60}$$

= 87^{\circ} + 0.332^{\circ} = 87.33^{\circ}
$$1^{\circ} = \frac{\pi}{180} \text{ radian}$$

$$87.33^{\circ} = \frac{\pi}{180} \times 87.33 \text{ radian}$$

= 1.524 radian
$$1524 \text{ radian}$$

$$11'43'' = 11' + \frac{43''}{60}$$

$$= 11' + 0.716'$$

= 11.72'
$$67^{\circ}11.72' = 67^{\circ} + \frac{11.72'}{60}$$

= 67^{\circ} + 0.195^{\circ}
= 67.2°
$$1^{\circ} = \frac{\pi}{180} \text{ radian}$$

$$67.2^{\circ} = \frac{\pi}{180} \times 67.2 \text{ radian}$$

= 1.173 radian

7 Convert $\frac{1}{7}$ π radian into degrees

1 radian =
$$\frac{180}{\pi}$$
 degree

 $\frac{4}{7}\pi$ radian = $\frac{180}{\pi} \times \frac{4}{7}\pi$ degree = 102.9 degree $= 102^{\circ} 0.9 \times 60^{\circ}$ = 102°54' 8 Convert 0.8357 radian into degrees 1 radian = $\frac{180}{\pi}$ degree 0.8357 radian = $\frac{180}{\pi} \times 0.8357$ degree $=47.88^{\circ}$ $= 47^{\circ} 0.88 \times 60'$ $=47^{\circ}52.80'$ = 47° 52'0.8 x 60" $=47^{\circ}52'48"$ 9 Convert 2.752 radian into degrees 1 Radian = $\frac{180}{\pi}$ degree 2.7520 radian = $\frac{180}{\pi}$ x 2.752 degree = 157.7° = 157.7° x 60' = 157°42' 10 Convent $\frac{3}{5}\pi$ radian into degrees 1 Radian = $\frac{180}{\pi}$ degree

1 Radian = $\frac{1}{\pi}$ degree $\frac{3}{5}\pi$ radian = $\frac{180}{\pi} \times \frac{3}{5}\pi$ degree = 108°

Assignment

Convert into Degree

1 12 Radian

Convert into Radians

- 2 78°
- 3 47º20'
- 4 52°36'45"
- 5 25°38"

Convert into degree, minute and seconds

- 6 46.723°
- 7 68.625°
- 8 0.1269 Radian
- 9 2.625 Radians

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WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.8.28

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.8.29 Trigonometry - Trigonometrical ratios

Dependency

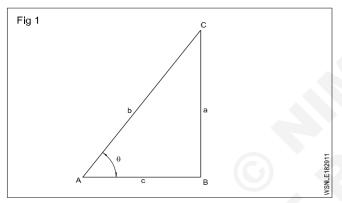
The sides of a triangle bear constant ratios for a given definite value of the angle. That is, increase or decrease in the length of the sides will not affect the ratio between them unless the angle is changed. These ratios are trigonometrical ratios. For the given values of the angle a value of the ratios

 $\frac{BC}{AB}$, $\frac{AC}{AB}$, $\frac{BC}{AC}$, $\frac{AB}{BC}$, $\frac{AB}{AC}$ and $\frac{AC}{BC}$ do not change even when the sides AB, BC, AC are increased to AB', BC' and AC' or decreased to AB", BC" and AC".

For the angle

- AC is the hypotenuse
- AB is the adjacent side
- BC is the opposite side.

The ratios



The six ratios between the sides have precise definitions.

Sine
$$\theta = \frac{BC}{AC} = \frac{Opposite side}{Hypotenuse} = Sin \theta$$

Cosine $\theta = \frac{AB}{AC} = \frac{Adjacent side}{Hypotenuse} = Cos \theta$
Tangent $\theta = \frac{BC}{AB} = \frac{Opposite side}{Adjacent side} = Tan \theta$
Cosecant $\theta = \frac{AC}{BC} = \frac{Hypotenuse}{Opposite side} = Cosec \theta$
Secant $\theta = \frac{AC}{AB} = \frac{Hypotenuse}{Adjacent side} = Sec \theta$
Cotangent $\theta = \frac{AB}{BC} = \frac{Adjacent side}{Opposite side} = Cot \theta$

Relationship between the ratios

$$\operatorname{Cosec} \theta = \frac{\operatorname{AC}}{\operatorname{BC}} = \frac{1}{\frac{\operatorname{BC}}{\operatorname{AC}}} = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{AC}{AB} = \frac{1}{\frac{AB}{AC}} = \frac{1}{\cos \theta}$$

$$\cot \theta = \frac{AB}{BC} = \frac{1}{\frac{BC}{AB}} = \frac{1}{\tan \theta}$$

$$\sin \theta = \frac{\text{sideBC}}{\text{sideAC}} = \frac{a}{b}$$

$$\cos \theta = \frac{\text{side AB}}{\text{sideAC}} = \frac{c}{b}$$

$$\frac{\sin \theta}{\cos \theta} = \frac{\frac{a}{b}}{\frac{c}{b}} = \frac{a}{b} \times \frac{b}{c} = \frac{a}{c}$$

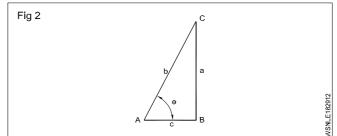
$$= \frac{\text{side BC}}{\text{side AB}} = \tan \theta$$

$$\sin \theta = \frac{1}{\csc \theta} \text{ or cosec } \theta = \frac{1}{\sin \theta} \text{ or sin } \theta.\text{cosec } \theta = 1$$

$$\cos \theta = \frac{1}{\sec \theta} \text{ or sec } \theta = \frac{1}{\cos \theta} \text{ or cos } \theta.\text{sec } \theta = 1$$

$$\tan \theta = \frac{1}{\cot \theta} \text{ or cot } \theta = \frac{1}{\tan \theta} \text{ or cot } \theta.\text{ sec } \theta = 1$$

$$By \text{ pythogoras theorem we have, } \text{ AC}^2 = \text{ AB}^2 + \text{ BC}^2$$



Dividing both sides of the equation by AC², we have

$$\frac{AC^{2}}{AC^{2}} = \frac{AB^{2}}{AC^{2}} + \frac{BC^{2}}{AC^{2}}$$
$$= \left[\frac{AB}{AC}\right]^{2} + \left[\frac{BC}{AC}\right]^{2}$$
$$1 = (\cos \theta)^{2} + (\sin \theta)^{2}$$
$$\sin^{2}\theta + \cos^{2}\theta = 1$$

Sine, Cosine, Tangent, Cosec, Sec and Cotangent are the six trigonometrical ratios $\tan \theta = \frac{\sin \theta}{\cos \theta}$ and $\sin^2 \theta + \cos^2 \theta = 1$ $\sin^2\theta + \cos^2\theta = 1$

It can be transformed as

$$\sin^{2}\theta = 1 - \cos^{2}\theta$$
$$\sin \theta = \sqrt{1 - \cos^{2}\theta}$$
$$\operatorname{or} \cos^{2}\theta = 1 - \sin^{2}\theta$$
$$\cos \theta = \sqrt{1 - \sin^{2}\theta}$$
$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\sqrt{1 - \cos^{2}\theta}}{\cos \theta}$$
$$\tan \theta = \frac{\sin \theta}{\sqrt{1 - \sin^{2}\theta}}$$
We know
$$\sin^{2}\theta + \cos^{2}\theta = 1$$

Dividing both sides by $\cos^2 \theta$.

$$\frac{\sin^2\theta}{\cos^2\theta} + \frac{\cos^2\theta}{\cos^2\theta} = \frac{1}{\cos^2\theta}$$

or 1 + tan² theta = sec² theta

 $\sin^2\theta + \cos^2\theta = 1.$

Dividing both sides by sin²q,

$$\frac{\sin^2 \theta}{\sin^2 \theta} + \frac{\cos^2 \theta}{\sin^2 \theta} = \frac{1}{\sin^2 \theta}$$
$$1 + \frac{\cos^2 \theta}{\sin^2 \theta} = \frac{1}{\sin^2 \theta}$$
$$1 + \cot^2 q = \csc^2 q$$
$$1 + \tan^2 q = \sec^2 q$$

Trigonometrical Tables

Ratio	0 °	30 °	45 °	60°	90 °
sin θ	0	<u>1</u> 2	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
cos θ	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	<u>1</u> 2	0
tan θ	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞

When q increases,

Sine value increases;

Cosine value decreases;

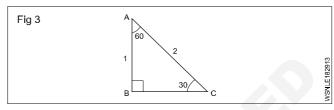
Tangent value increases to more than 1 when the angle is more than 45° (tan 60° = 1.732)

Sine of an angle =	Cosine of its complemen- tary angle
Cosine of an angle =	Sine of its complementary angle

Examples

If sin $30^\circ = \frac{1}{2}$ find the value of sin 60°

By applying pythagores theorem



 $BC^2 = AC^2 - AB^2$

$$BC^2 = 2^2 - 1^2$$

= 3

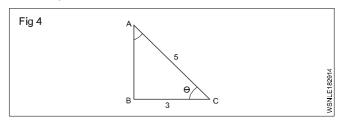
$$\sin 60^{\circ} = \frac{\sqrt{3}}{2}$$

 $\cos\theta = \frac{3}{5}$ Find the other trigonometrical ratios

By applying pythagores theorem

$$AB^2 = AC^2 - BC^2$$

= 5² - 3² = 25 - 9



$$AB = \sqrt{16} = 4$$

Now
$$\sin\theta = \frac{4}{5}$$

 $\tan \theta = \frac{4}{3}$
 $\operatorname{Cosec} \theta = \frac{5}{4}$
 $\sec \theta = \frac{5}{3}$

$$\cot \theta = \frac{3}{4}$$

Ratio	90 - θ	90 + 0	180 - θ	180 + θ	270 - θ	270 + θ	360 - Ө	- θ
sin	COS	cos	sin	- sin	- COS	- COS	- sin	- sin
cos	sin	- sin	- COS	- COS	- sin	sin	cos	COS
tan	cot	- cot	- tan	tan	cot	- cot	- tan	- tan
cosec	sec	sec	cosec	- cosec	- sec	- sec	- cosec	- cosec
sec	cosec	- cosec	- sec	- sec	- cosec	cosec	sec	sec
cot	tan	- tan	- cot	cot	tan	- tan	- cot	- cot

Simplify :

$$\cot \theta + \tan (180+\theta) + \tan(90-\theta) + (\tan 360 - \theta)$$
$$= \cot \theta + \tan \theta - \cot \theta - \tan \theta$$
$$= 0$$

Simplify :

$$\frac{\cos (90+\theta) \sec (-\theta) \tan (180-\theta)}{\sec (360-\theta) \sin (180+\theta) \cos (90-\theta)}$$

$$= \frac{(-\sin\theta)x(\sec\theta)x(-\tan\theta)}{(\sec\theta)x(-\sin\theta)x(-\sin\theta)}$$

$$= \frac{\tan\theta}{\sin\theta} = \frac{1}{\cos\theta} = \sec\theta$$

simplify:

$$\frac{\cos (90^\circ + \theta) \sec (-\theta) \tan (180^\circ - \theta)}{\sec (360^\circ - \theta) \sin (180^\circ + \theta) \cot (90^\circ - \theta)}$$

$$\cos (90^\circ + \theta) = -\sin \theta$$

$$\sec (-\theta) = \sec \theta$$

$$\tan (180^\circ - \theta) = -\tan \theta$$

 $\sec (360^{\circ} - \theta) = \sec \theta$ $\sin (180^{\circ} + \theta) = -\sin \theta$ $\cot (90^{\circ} + \theta) = -\tan \theta$

$$\frac{\cos (90^{\circ} + \theta) \sec (-\theta) \tan (180^{\circ} - \theta)}{\sec (360^{\circ} - \theta) \sin (180^{\circ} + \theta) \cot (90^{\circ} - \theta)}$$

$$=\frac{(-\sin\theta)(\sec\theta)(\tan\theta)}{(\sec\theta)(-\sin\theta)(-\tan\theta)}$$

Simplify:

 $Cot \theta + tan (180^{\circ} + \theta) + tan (90^{\circ} + \theta) + tan (360^{\circ} - \theta)$ $tan (180^{\circ} - \theta) = tan \theta$ $tan (90^{\circ} + \theta) = - cot \theta$ $tan (360^{\circ} - \theta) = - tan \theta$ $cot \theta + tan (180^{\circ} + \theta) + tan (90^{\circ} + \theta) + tan (360^{\circ} - \theta)$ $cot \theta + tan \theta - cot \theta - tan \theta = 0$

Assignment

- 1 Given $\sin 30^\circ = 1/2$, find the value of $\tan 60^\circ$
- 2 If $\cos \theta = 4/5$, find the other radios
- 3 If sin A = 3/5, find cos θ , tan θ & sec θ
- 4 If $\tan \theta = 24/7$, find $\sin \theta$ and $\cos \theta$
- 5 Find the value of $\cos \theta$ and $\tan \theta$, if $\sin \theta = 1/2$
- 6 If $\cos \theta = 5/13$, find the value of $\tan \theta$
- 7 If $\sin \theta = 1/2$, find the value of $\sin^2 \theta \cos^2 \theta$

8 What is the value of

$$\frac{\sin^2 30^{\circ}}{\cos^2 45^{\circ}} + \frac{\tan 45^{\circ}}{\sec 60^{\circ}} - \frac{\sin 60^{\circ}}{\cot 45^{\circ}} - \frac{\cos 30^{\circ}}{\sin 90^{\circ}}$$

Simplify :

1 tan (90 + A) + (tan 180 + A) tan (90 + A)

$$2 \quad \frac{\cos(90+\theta) \cdot \sec(-\theta) \cdot \tan(180-\theta)}{\sec(360+\theta) \cdot \sin(180+\theta) \cdot \cot(90+\theta)}$$

Workshop Calculation & Science - Lift & Escalator Mechanic Exercise 1.8.30 Trigonometry - Trigonometrical tables

Use of trigonometrical tables (Ref: Sin, Cos & Tan Table)

	Mi	inut	es fr	om	0 to	4	Me	ean d	iffe	erei	nce
Deg.	0'	6'	12'	18'	24'	54'	1'	2' 3	3'	4'	5'
0											
1											
2											
3											
26				х				5			
.											
89											

Sine value for 26°-20'

Refer to Natural sine table.

Degrees column go up to 26° down

Minutes column 18' horizontal and under this note the value which is given as 0.4431.

Under mean difference for 2' in the same horizontal line 5 is given. Add this to the extreme right number noted for $26^{\circ}-18'$.

Sine 26° - 20' = 0.4431 + .0005 = 0.4436

Cosine value for 43°-41'

Referring to the Natural cosines table for 43° –36' it is given as 0.7242 and the mean difference for 5' minutes is given as 10.

SINE TABLE

- 1 Sin 25° = 0.4226
- 2 Sin 17° 5'

$$\frac{\text{Difference 5'} = 0.2924}{\sin 17^{\circ} 5' = 0.2938}$$
 Ans

_ 0 2024

cip 17º

 $\cos 43^\circ - 41'$ = value for $\cos 43^\circ.36'$ - the value given for mean difference of 5' = 0.7242 - 0.0010 = 0.7232

When reading sine value add the mean difference value. When reading cosine value subtract the mean difference value.

Arrangement

Values of trigonometrical ratios can be taken from mathematical tables.

The left hand vertical column consists of degrees.

The top horizontal column is arranged in minutes in steps of 6' from 0' to 54'. In the extreme right horizontal columns the mean differences are written in minutes from 1' to 5' in steps of 1' to account for angles with minutes between the interval of 6'.

- The values of cosine, cosecant and cotangent decrease when the value of the angle increases.
- For sine, secant and tangent, the value increases when the angle increases.
- The value of sine and cosine will never be more than 1.
- The value of secant and cosecant will never be less than 1.
- The value of Tan and Cot ranges from 0 to ∞.

EXAMPLE

From the tables obtain the cosine of 45°20 '.

cos 45°18 ' = 0.7108 mean difference for 2 ' = 0.0004 cos 45° 20 ' = 0.7104

3 sin 17° 45' 13"

 $\frac{\sin 17^{\circ} \ 46' = 0.3051}{\sin 17^{\circ} \ 45' = 0.3048}$ Difference 1' = 0.0003

$$1'(or) 60" = 0.0003$$

$$13" = \frac{0.0003}{60} \times 13$$

$$= \frac{0.0039}{60}$$

$$= \frac{0.00039}{6}$$

$$= 0.000065$$

$$\sin 17^{0} 45' = 0.3048$$

$$13" = 0.000065$$

$$\sin 17^{0} 45'13" = 0.304865$$
Ans.

4 sin82° 14'18"

 $\sin 82^{\circ} 15' = 0.9908$ $\sin 82^{\circ} 14' = 0.9908$ Difference 1' = 0

1'(or) 60'' = 0sin18" = 0 $sin82^{\circ}14' = 0.9908$ 18" = 0.0000 $sin82^{\circ}41'18'' = 0.9908$ Ans.

Finding the corresponding angles when sine values are given:

1. Sin θ = 0.9925

 $\theta = 83^{\circ}$

2. Sin θ = 0.8791

0.8788	=	Sin 61º 30'
0.0003	=	2'
0.8791	=	Sin 61º 32'

3. $\sin \theta = 0.68015$

 $0.6794 = \sin 42^{\circ}48'$

$$0.0006 = 3'$$

 $0.6800 = \sin 42^{\circ} 51'$
 $0.6803 = \sin 42^{\circ} 52'$

Difference 0.0003 = 1' (or) 60"

$$\begin{array}{rcl} 0.00015 & = & \frac{60}{0.0003} & X & 0.00015 \\ & = & \frac{60 \times 15}{30} \\ & = & 30" \end{array}$$

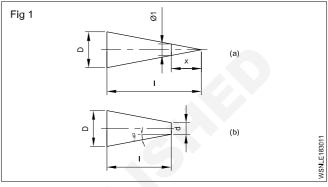
 $0.6800 = \sin 42^{\circ} 51'$ 0.00015 =30"

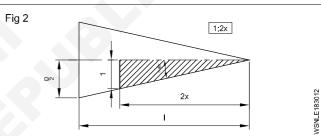
 $0.68015 = \sin 42^{\circ} 51'30"$

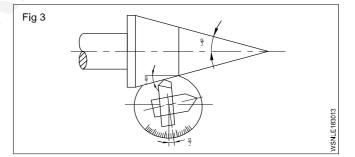
$\theta = 42^{\circ} 51'30''$

Calculations involving tapers

- **D** Big diameter of the taper
- d small diameter of the taper
- C Taper Ratio 1:x







C Ratio of inclination - 1:2 x 2

I - length of taper

a - included angle of taper

α setting angle

Taper ratio = Ratio of inclination (for wedges).

Taper ratio

The ratio between the difference in diameter to the length of the taper is known as taper ratio. D is the difference in larger diameter shown in the sketch as the small diameter of taper is 0. Taper ratio is D:1. In the sectioned portion the difference in diameter is 1 and the length of taper is shown as x.

C = D: d = 1 : x as per Fig 1 (a), C = $\frac{D-d}{I}$ as per Fig 1 (b)

Ratio of inclination

Taking half of the taper, $\frac{D}{2}$ is the difference in diameter for a taper length of I, if d = 0.

 $\therefore \frac{C}{2} = \frac{D}{2I} \text{ if the small diameter is 0}$ or $\frac{C}{2} = \frac{D - d}{2I}$

1 Ratio of inclination = $\frac{1}{2}$ of the taper ratio.

Setting angle

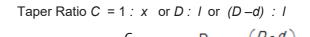
One of the methods of turning taper is by swivelling the compound slide to an angle known as setting angle and feeding the tool at an angle to the axis of work.

 $\tan \frac{\alpha}{2} = \frac{C}{2} = \frac{D-d}{2l}$ $\tan \frac{\alpha}{2} = \frac{\text{taper ratio}}{2}$

difference in diameter

2 x taper length

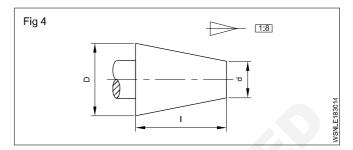
NOTE: $\frac{\alpha}{2}$ is the setting angle which is equal to half of the included angle of the taper.



Ratio of inclination $\frac{C}{2} = 1:2x = \frac{D}{2}: I \text{ or } \left(\frac{D-d}{2}\right):I$

Setting angle determination is by the formula

$$\tan \frac{\alpha}{2} = \frac{D-d}{2l} = \frac{C}{2}$$



EXAMPLE

A pivot in the form of a frustum of a cone has a taper ratio 1:8. If the small diameter is 30 mm and length of taper is 80 mm, find its large diameter.

$$C = 1:8 = \frac{1}{8}$$

$$\therefore \frac{D-d}{7} = \frac{1}{8}$$

$$\therefore D - d = \frac{1}{8} = \frac{80}{8} = 10 \text{ mm.}$$

$$D - 30 \text{ mm} = 10 \text{ mm}$$

$$D = 10 \text{ mm} + 30 \text{ mm} = 40 \text{ mm}$$

Large diameter $D = 40 \text{ mm}$

Find the corresponding angles when cos values are given:

Ŭ			
1	Cos θ	=	0.5150
	θ	=	59°
2	Cosθ	=	0.0192
	θ	=	88°54'
3	Cosθ	=	0.9682
	0.9686	=	cos 14º24'
(-)	4	=	5'
	0.9682	=	cos 14º29'
	θ	=	14º 29'

Cos Table

 Cos 38° Cos 38° = 0.7880
 Cos 83°12' Cos 83°12' = 0.1184

3 Cos 26°40' Cos 26°36' = 0.8942 4' = 5(-)

 $\cos 26^{\circ}40' = 0.8937$

4 Cos 31°20'

Cos 31°18' = 0.8545 2' = 3 (-)

Cos 31°20' = 0.8542

$4 \cos \theta = 0.8476$	
$0.8480 = \cos 32^{\circ} 0'$	$=\frac{5 \text{ cm}}{250}$
(-) 0.0003 = 2'	250 mm
$0.8477 = \cos 32^{\circ} 2'$	= <u>50 mm</u>
$0.8475 = \cos 32^{\circ} 3'$	250 mm
0.0002 = 1'(or) 60"	= 0.2000
0.0002 = 1'(or) 60'' 60	$\theta = 11^{\circ} 32'$
$\begin{array}{rcl} 0.0001 & = &x \ 0.0001 \\ & & 0.0002 \\ & & 60 \end{array}$	2 Find the height of the slip gauge if a Sine bar with plugs of 10" centre is set up to inspect a taper having an included angle of 9° 56".
= x 1 = 30" 0.8477 = Cos 32° 2'	$Sin \theta = \frac{Opp.side}{Hyp.} = \frac{h}{l}$
(-) 0.0001 = 30" (+)	$\sin 9^{\circ}56'' = \frac{h}{10}$
0.8476 = Cos 32° 2' 30"	∴h = 10 x sin 9°56"
tan Table	Fig 5
1 tan 35° 37'	10" h 👳
tan 35° 36' = 0.7159	9° 56" 56" ₹
1' = 0.0004	
tan 35° 37' = 0.7163	$\sin 9^{\circ}0'' = 0.1564$
tan 35° 37' = 0.7163	Sin 9° 1" = 0.1567
2 tan 50° 5'	1' (or) 60" = 0.0003
$Tan 50^{\circ}0' = 1.1918$	$56'' = \frac{0.0003}{60} \times 56$
5' = 0.0036	
 Tan 50° 5' = 1.1954	$=\frac{0.0168}{20}$
	60 0.00168
Find the corresponding angles when tan values are given	$=\frac{6000000}{6}$
1 tan θ = 0.3972	= 0.00028
0.3959 = tan 21° 36'	sin9° 0' 00" = 0.1564
0.0013 = 4'	56" = 0.00028
$0.3972 = \tan 21^{\circ} 40'$	sin9° 0' 56" = 0.15668
$2 \tan \theta = 1.0065$	h = 10 x sin9° 56"
$1.0035 = \tan 45^{\circ} 6'$	= 10 x 0.15668
0.0030 = 5'	= 1.5668 cm
1.0065 = tan 45° 11'	Height of slip gauge = 1.5668"
Problems Related with Trigonometrical tables	3 Find the angle which the ladder makes with the ground if the foot of a 4.5 m long ladder is placed

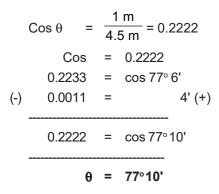
1 A 250 mm Sine bar is used to measure an angle. If the difference in height is 5 cm, find the angle.

$$Sin\theta = \frac{Opp.side}{Hyp.} = \frac{h}{l}$$

In Right angled D

$$\cos C = \frac{BC}{AC}$$

at 1 m away from the wall.

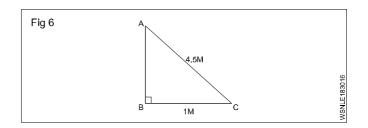


Assignment

- I Find the values of the given angles
 - 1 Sin 65°
 - 2 Sin 42°23'
 - 3 Sin 66° 35' 32"
 - 4 Sin 7° 15' 41"
 - 5 Sin 27°27"
 - 6 Cos 26°40'
 - 7 Cos 47°39'
 - 8 Cos 79°31'53"
 - 9 Tan 28°45'
 - 10 Tan 67°27'36"

II Find corresponding angles for given values

- 1 Sin θ = 0.3062
- 2 Sin θ = 0.6002
- 3 Sin θ = 0.22453
- 4 Sin θ = 0.04802
- 5 $\cos \theta = 0.6446$



- 6 $\cos \theta = 0.8926$
- 7 $\cos \theta = 0.11773$
- 8 $\cos \theta = 0.21646$
- 9 Tan θ = 0.3411
- 10 Tan θ = 2.3868

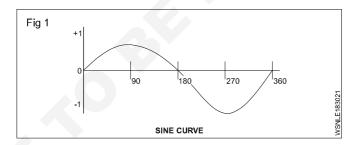
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- 1 Calculate its base. if the slant height of a cone is 12.25 cm and the vertex angle is 110° .
- 2 A ladder 2.5 m long makes an angle of 60° with the ground. Find the height of the wall where the ladder touches the wall.
- 3 A sine bar of 200 mm is to be set at an angle of 15°15'3". Select the slip gauge block to built up the required height.
- 4 In a right angled triangle ABC, $\angle C = 90^{\circ}$, If AB = 50 mm and $\angle B = 75^{\circ}$, Find the remaining sides.
- 5 Calculate the required length of the bar for this point if a centre point having an included angle of 60° is to be turned at the end of a 50 mm dia bar.

Natural Sines

0	0' 0.0 ⁰	6' 0.1 ⁰	12' 0.2 ⁰	18' 0.3 ⁰	24' 0.4°	30' 0.5 ⁰	36' 0.6 ⁰	42' 0.7°	48' 0.8 ⁰	54' 0.9 ⁰	1'	2'	3'	4'	5'
0 1 2 3 4	0.0000 0.0175 0.0349 0.0523 0.0698	0.0017 0.0192 0.0366 0.0541 0.0715	0.0035 0.0209 0.0384 0.0558 0.0732	0.0052 0.0227 0.0401 0.0576 0.0750	0.0070 0.0244 0.0419 0.0593 0.0767	0.0087 0.0262 0.0436 0.0610 0.0785	0.0105 0.0279 0.0454 0.0628 0.0802	0.0122 0.0297 0.0471 0.0645 0.0819	0.0140 0.0314 0.0488 0.0663 0.0837	0.0157 0.0332 0.0506 0.0680 0.0854	3 3 3 3 3 3	6 6 6 6	9 9 9 9 9	12 12 12 12 12	15 15 15 15 14
5 6 7 8 9	0.0872 0.1045 0.1219 0.1392 0.1564	0.0899 0.1063 0.1236 0.1409 0.1582	0.0906 0.1080 0.1253 0.1426 0.1599	0.0924 0.1097 0.1271 0.1444 0.1616	0.0941 0.1115 0.1288 0.1461 0.1633	0.0958 0.1132 0.1305 0.1478 0.1650	0.0976 0.1149 0.1323 0.1495 0.1668	0.0993 0.1167 0.1340 0.1513 0.1685	0.1011 0.1184 0.1357 0.1530 0.1702	0.1028 0.1201 0.1374 0.1547 0.1719	3 3 3 3 3 3	6 6 6 6	9 9 9 9	12 12 12 11 11	14 14 14 14 14
10 11 12 13 14	0.1736 0.1908 0.2079 0.2250 0.2419	0.1754 0.1925 0.2096 0.2267 0.2436	0.1771 0.1942 0.2113 0.2284 0.2453	0.1788 0.1959 0.2130 0.2300 0.2470	0.1805 0.1977 0.2147 0.2317 0.2487	0.1822 0.1994 0.2164 0.2334 0.2504	0.1840 0.2011 0.2181 0.2351 0.2521	0.1857 0.2028 0.2198 0.2368 0.2538	0.1874 0.2045 0.2215 0.2385 0.2554	0.1891 0.2062 0.2232 0.2402 0.2571	3 3 3 3 3 3	6 6 6 6	9 9 9 8 8	11 12 11 11 11	14 14 14 14 14
15 16 17 18 19	0.2558 0.2756 0.2924 0.3090 0.3256	0.2605 0.2773 0.2940 0.3107 0.3272	0.2622 0.2790 0.2957 0.3123 0.3289	0.2639 0.2807 0.2974 0.3140 0.3305	0.2656 0.2823 0.2990 0.3156 0.3322	0.2672 0.2840 0.3007 0.3173 0.3338	0.2689 0.2857 0.3024 0.3190 0.3355	0.2706 0.2874 0.3040 0.3206 0.3371	0.2723 0.2890 0.3057 0.3223 0.3387	0.2740 0.2907 0.3074 0.3239 0.3404	3 3 3 3 3	6 6 6 5	8 8 8 8	11 11 11 11 11	14 14 14 14 14
20 21 22 23 24	0.3420 0.3584 0.3746 0.3907 0.4067	0.3437 0.3600 0.3762 0.3923 0.4083	0.3453 0.3616 0.3778 0.3939 0.4099	0.3469 0.3633 0.3795 0.3955 0.4115	0.3486 0.3649 0.3811 0.3971 0.4131	0.3502 0.3665 0.3827 0.3987 0.4147	0.3518 0.3681 0.3843 0.4003 0.4163	0.3535 0.3697 0.3859 0.4019 0.4179	0.3551 0.3714 0.3875 0.4035 0.4195	0.3567 0.3730 0.3891 0.4051 0.4210	3 3 3 3 3 3	5 5 5 5 5	8 8 8 8	11 11 11 11 11	14 14 13 13 13
25 26 27 28 29	0.4226 0.4384 0.4540 0.4695 0.4848	0.4242 0.4399 0.4555 0.4710 0.4863	0.4258 0.4415 0.4571 0.4726 0.4879	0.4274 0.4431 0.4586 0.4741 0.4894	0.4289 0.4446 0.4602 0.4756 0.4909	0.4305 0.4462 0.4617 0.4772 0.4924	0.4321 0.4478 0.4633 0.4787 0.4939	0.4337 0.4493 0.4648 0.4802 0.4955	0.4352 0.4509 0.4664 0.4818 0.4970	0.4368 0.4524 0.4679 0.4833 0.4985	3 3 3 3 3	5 5 5 5 5	8 8 8 8	11 10 10 10 10	13 13 13 13 13
30 31 32 33 34	0.500 0.5150 0.5299 0.5446 0.5592	0.5015 0.5165 0.5314 0.5461 0.5606	0.5030 0.5180 0.5329 0.5476 0.5621	0.5045 0.5195 0.5344 0.5490 0.5635	0.5060 0.5210 0.5358 0.5505 0.5650	0.5075 0.5225 0.5373 0.5519 0.5664	0.5090 0.5240 0.5388 0.5534 0.5678	0.5105 0.5255 0.5402 0.5548 0.5693	0.5120 0.5270 0.5417 0.5563 0.5707	0.5135 0.5284 0.5432 0.5577 0.5721	3 2 2 2 2	5 5 5 5 5 5	8 7 7 7 7	10 10 10 10 10	13 12 12 12 12
35 36 37 38 39	0.5736 0.5878 0.6018 0.6157 0.6293	0.5750 0.5892 0.6032 0.6170 0.6307	0.5764 0.5906 0.6046 0.6184 0.6320	0.5779 0.5920 0.6060 0.6198 0.6334	0.5793 0.5934 0.6074 0.6211 0.6347	0.5807 0.5948 0.6088 0.6225 0.6361	0.5821 0.5962 0.6101 0.6239 0.6374	0.5835 0.5976 0.6115 0.6252 0.6388	0.5850 0.5990 0.6129 0.6266 0.6401	0.5864 0.6004 0.6143 0.6280 0.6414	2 2 2 2 2	5 5 5 5 4	7 7 7 7 7	9 9 9 9	12 12 12 11 11
40 41 42 43 44	0.6428 0.6561 0.6691 0.6820 0.6947	0.6441 0.6574 0.6704 0.6833 0.6959	0.6455 0.6587 0.6717 0.6845 0.6972	0.6468 0.6600 0.6730 0.6858 0.6984	0.6481 0.6613 0.6743 0.6871 0.6997	0.6494 0.6626 0.6756 0.6884 0.7009	0.6508 0.6639 0.6769 0.6896 0.7022	0.6521 0.6652 0.6782 0.6909 0.7034	0.6534 0.6665 0.6794 0,6921 0.7046	0.6547 0.6678 0.6807 0.6934 0.7059	2 2 2 2 2 2	4 4 4 4	7 7 6 6 6	9 9 9 8 8	11 11 11 11 10
45 46 47 48 49	0.7071 0.7193 0.7314 0.7431 0.7547	0.7083 0.7206 0.7325 0.7443 0.7558	0.7096 0.7218 0.7337 0.7455 0.7570	0.7108 0.7230 0.7349 0.7466 0.7581	0.7120 0.7242 0.7361 0.7478 0.7593	0.7133 0.7254 0.7373 0.7490 0.7604	0.7145 0.7266 0.7385 0.7501 0.7615	0.7157 0.7278 0.7396 0.7513 0.7627	0.7169 0.7290 0.7408 0.7524 0.7638	0.7181 0.7302 0.7420 0.7536 0.7649	2 2 2 2 2 2	4 4 4 4	6 6 6 6	8 8 8 8	10 10 10 10 9
50 51 52 53 54	0.7660 0.7771 0.7880 0.7986 0.8090	0.7672 0.7782 0.7891 0.7997 0.8100	0.7683 0.7793 0.7902 0.8007 0.8111	0.7694 0.7804 0.7912 0.8018 0.8121	0.7705 0.7815 0.7923 0.8028 0.8131	0.7716 0.7826 0.7934 0.8039 0.8141	0.7727 0.7837 0.7944 0.8049 0.8151	0.7738 0.7848 0.7955 0.8059 0.8161	0.7749 0.7859 0.7965 0.8070 0.8171	0.7760 0.7869 0.7976 0.8080 0.8181	2 2 2 2 2	4 4 3 3	6 5 5 5 5	7 7 7 7 7	9 9 9 9
55 56 57 58 59	0.8192 0.8290 0.8387 0.8480 0.8572	0.8202 0.8300 0.8396 0.8490 0.8581	0.8211 0.8310 0.8406 0.8499 0.8590	0.8221 0.8320 0.8415 0.8508 0.8599	0.8231 0.8329 0.8425 0.8517 0.8607	0.8241 0.8339 0.8434 0.8526 0.8616	0.8251 0.8348 0.8443 0.8536 0.8625	0.8261 0.8358 0.8453 0.8545 0.8634	0.8271 0.8368 0.8462 0.8554 0.8643	0.8281 0.8377 0.8471 0.8563 0.8652	2 2 2 2 1	3 3 3 3 3	5 5 5 5 4	7 6 6 6	8 8 8 7

Natura	al Sines	;													
0	0' 0.0 ⁰	6' 0.1°	12' 0.2 ⁰	18' 0.3 ⁰	24' 0.4 ^o	30' 0.5 ⁰	36' 0.6°	42' 0.7°	48' 0.8 ⁰	54' 0.9 ⁰	1'	2'	3'	4'	5'
		_													
60 61	0.8660 0.8746	0.8669 0.8755	0.8678	0.8686 0.8771	0.8695 0.8780	0.8704 0.8788	0.8712 0.8796	0.8721 0.8805	0.8729 0.8813	0.8738 0.8821	1	3	4 4	6	7 7
62	0.8829	0.8838	0.8846	0.8854	0.8862	0.8870	0.8878	0.8886	0.8894	0.8902	1	3 3	4	6 5	7
63	0.8910	0.8918	0.8926	0.8934	0.8942	0.8949	0.8957	0.8965	0.8973	0.8980		3	4	5	6
64	0.8988	0.8996	0.9003	0.9011	0.9018	0.9026	0.9033	0.9041	0.9048	0.9056	1	3	4	5	6
65	0.9063	0.9070	0.9078	0.9085	0.9092	0.9100	0.9107	0.9114	0.9121	0.9128	1	2	4	5	6
66	0.9135	0.9143	0.9150	0.9157	0.9164	0.9171	0.9178	0.9184	0.9191	0.9198	1	2	3	5	6
67	0.9205	0.9212	0.9219	0.9225	0.9232	0.9239	0.9245	0.9252	0.9259	0.9265	1	2	3	4	6
68	0.9272	0.9278	0.9285	0.9291	0.9298	0.9304	0.9311	0.9317	0.9323	0.9330		2	3	4	5
69	0.9336	0.9342	0.9348	0.9354	0.9361	0.9367	0.9373	0.9379	0.9385	0.9391	1	2	3	4	5
70	0.9397	0.9403	0.9409	0.9415	0.9421	0.9426	0.9432	0.9438	0.9444	0.9449	1	2	3	4	5
71	0.9455	0.9461	0.9466	0.9472	0.9478	0.9483	0.9489	0.9494	0.9500	0.9505	1	2	3	4	5
72	0.9511	0.9516	0.9521	0.9527	0.9532	0.9537	0.9542	0.9548	0.9553	0.9558	1	2	3	3	4
73	0.9563	0.9568	0.9573	0.9578	0.9583	0.9588	0.9593	0.9598	0.9603	0.9608	1	2	2	3	4
74	0.9613	0.9617	0.9622	0.9627	0.9632	0.9636	0.9641	0.9646	0.9650	0.9655	1	2	2	3	4
75	0.9659	0.9664	0.9668	0.9673	0.9677	0.9681	0.9686	0.9690	0.9694	0.9699	1	1	2	3	4
76	0.9703	0.9707	0.9711	0.9715	0.9720	0.9724	0.9728	0.9732	0.9736	0.9740	1	1	2	3	3
77	0.9744	0.9748	0.9751	0.9755	0.9759	0.9763	0.9767	0.9770	0.9774	0.9778		1	2	2	3
78 79	0.9781	0.9785 0.9820	0.9789	0.9792	0.9796 0.9829	0.9799	0.9803	0.9806	0.9810	0.9813 0.9845	1	1	2 2	2 2	3 3
/9	0.9816	0.9620	0.9823	0.9826	0.9629	0.9833	0.9836	0.9839	0.9842	0.9645			2	Z	3
80	0.9848	0.9851	0.9854	0.9857	0.9860	0.9863	0.9866	0.9869	0.9871	0.9874	0	1	1	2	2
81	0.9877	0.9880	0.9882	0.9885	0.9888	0.9890	0.9893	0.9895	0.9898	0.9900	0	1	1	2	2
82	0.9903	0.9905	0.9907	0.9910	0.9912	0.9914	0.9917	0.9919	0.9921	0.9923	0	1	1	1	2
83	0.9925	0.9928	0.9930	0.9932	0.9934	0.9936	0.9938	0.9940	0.9942	0.9943	0	1	1	1	2
84 85	0.9945 0.9962	0.9947 0.9963	0.9949 0.9965	0.9951 0.9966	0.9952 0.9968	0.9954 0.9969	0.9956 0.9971	0.9957	0.9959	0.9960 0.9974	0	1 0	1 1	1 1	1 1
86	0.9962	0.9963	0.9965	0.9966	0.9966	0.9969	0.9971	0.9972	0.9973	0.9974	0	0	1	1	1
87	0.9986	0.9987	0.9988	0.9989	0.9990	0.9990	0.9991	0.9992	0.9993	0.9993	0	0	0	1	1
88	0.9994	0.9995	0.9995	0.9996	0.9996	0.9997	0.9997	0.9997	0.9998	0.9998	0	0	Ő	0	0
89	0.9998	0.9999	0.9999	0.9999	0.9999	1.0000	1.0000	1.0000	1.0000	1.0000	0	0	0	0	0
90	1.0000														
							, The second sec								



Angle	sinA =	Examples
0 to 90°	sin A	sin 34°38' = 0.5683
90° to 180°	sin(180°-A)	sin 145°22' = sin(180° – 145° 22')
		= sin 34°38' = 0.5683
180° to 270°	–sin(A – 180°)	sin 214°38' = -sin(214°38' - 180°)
		=-sin34°38' =-0.5683
270° to 360°	sin(360° A)	$\sin 325^{\circ}22' = -\sin(360^{\circ} - 325^{\circ}22')$
		= - sin 34°38' = -0.5683
	0 to 90° 90° to 180° 180° to 270°	0 to 90° sin A 90° to 180° sin(180° – A) 180° to 270° –sin(A – 180°)

Numbers in different columns to be subtracted, not added

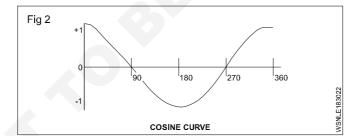
" " 0" 6" 11" 2" 3" 4" 5" 0 0.000 1.00000 1.00000 1.000		0' 6' 12' 18' 24' 30' 36' 42' 48' 54' 1' 2' 3' 4' 5'														
0 10000 10000 10000 10000 10000 00000 0.9998 0.9997	0	-		12'								1'	2'	3'	4'	5'
1 0.9998 0.9998 0.9998 0.9997 0.9996 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9977 0.9977 0.9973 0.9977 0.9973 0.9977 0.9973 0.9977 0.9974 0.9973 0.9974 0.9976 0.9975 0.9975 0.9976 0.9974 1 1 2 2 3 1 1 2 2 3 4 10 0.9974 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.9774 0.97		0.00	0.10	0.20	0.30	0.40	0.50	0.60	0.70	0.80	0.90					
1 0.9988 0.9988 0.9986 0.9986 0.9986 0.9986 0.9987 0.9977 0.9977 0.9977 0.9977 0.9977 0.9977 0.9977 0.9977 0.9977 0.9978 0.9978 0.9978 0.9978 0.9978 0.9978 0.9977 0.9977 0.9977 0.9977 0.9971 1.1 1.1 1.1 1 1.1 1.1 1.1 1.1 1.1 1.2 2.2 3.3 3.0 0.9978 0.9770 0.9770 0.9770 0.9770 0.9775 0.9776 0.9776 0.9776 0.9776 0.9776 0.9776 0.9776 0.9776 0.9776 0.9776 <t< td=""><td>0</td><td>1.0000</td><td>1.0000</td><td>1.0000</td><td>1.0000</td><td>1.0000</td><td>1.0000</td><td>0.9999</td><td>0.9999</td><td>0.9999</td><td>0.9999</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></t<>	0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9999	0	0	0	0	0
3 0 0 0 0 0 0 0 1 1 1 5 0 0 0 0 0 0 1 1 1 5 0 0 0 0 0 1 1 1 1 7 0 0 0 0 0 0 1	1	0.9998		0.9998						0.9995	0.9995	0	0	0	0	0
4 0.9976 0.9973 0.9973 0.9971 0.9972 0.9971 0.9972 0.9972 0.9973 0.9773											0.9987	0	0	0	1	1
5 0.9962 0.9965 0.9957 0.9951 0.9947 0.9947 0 1 2 2 3 </td <td></td>																
6 0.9945 0.9945 0.9946 0.9947 0.9928 0.9930 0.9928 0.9911 2 2 0 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9170 0.776 </td <td>4</td> <td>0.9976</td> <td>0.9974</td> <td>0.9973</td> <td>0.9972</td> <td>0.9971</td> <td>0.9969</td> <td>0.9968</td> <td>0.9966</td> <td>0.9965</td> <td>0.9963</td> <td>0</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td>	4	0.9976	0.9974	0.9973	0.9972	0.9971	0.9969	0.9968	0.9966	0.9965	0.9963	0	0	1	1	1
6 0.9945 0.9945 0.9946 0.9947 0.9928 0.9930 0.9928 0.9911 2 2 0 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9930 0.9170 0.776 </td <td>5</td> <td>0.0062</td> <td>0.0060</td> <td>0.0050</td> <td>0.0057</td> <td>0.0056</td> <td>0.0054</td> <td>0.0052</td> <td>0.0051</td> <td>0.0040</td> <td>0.0047</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td>	5	0.0062	0.0060	0.0050	0.0057	0.0056	0.0054	0.0052	0.0051	0.0040	0.0047	0	1	1	1	1
7 0 0 0 0 0 0 0 0 0 0 1 1 1 2 2 0 0 0 0 0 0 0 0 1 1 2 2 10 0 0 0 0 0 0 0 1 1 2 2 10 1 1 1 1 2 2 3 3 11 0 0 0 0 0 0 0 0 0 0 0 1 1 2 2 3 4 11 0 0 0 0 0 0 0 0 0 0 0 <td></td> <td>1</td> <td></td>		1														
B 0.9903 0.9903 0.9986 0.9868 0.9862 0.9867 0.9867 0.987 11 0.9844 0.9844 0.9844 0.9845 0.9865 0.9862 0.9862 0.9865 0.9865 0.9865 0.9875 0.9756 1 1 2 2 3 10 0.9844 0.9844 0.9845 0.9865 0.9865 0.9865 0.9865 0.9865 1 1 2 2 3 4 15 0.9855 0.9656 0.9666 0.9666 0.9666 0.9667 0.9673 0.9675 0.9674 1 2 2 3 4 16 0.9655 0.9666 0.9664 0.9663 0.9664 0.9663 0.9664 0.9663 0.9664 1 2 3 4 5 10 0.9455 0.9456 0.9464 0.9430 0.9421 0.9472 0.9472 0.9472 0.9472 0.9472 0.9473 0.848 0.8430																
9 0.9877 0.9871 0.9871 0.9871 0.9871 0.9871 0.9871 0.9871 1 1 2 2 10 0.9848 0.9843 0.9836 0.9836 0.9836 0.9820 0.9820 0.9820 0.9781 0.9774 0.9744 0.9744 0.9744 0.9974 0.9974																
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13 0.9744 0.9736 0.9736 0.9736 0.9745 0.9715 0.9715 0.9714 1 1 2 3 4 15 0.9658 0.9665 0.9664 0.9664 0.9664 0.9664 0.9664 0.9664 1 1 2 3 4 16 0.9658 0.9650 0.9664 0.9664 0.9664 0.9664 0.9664 0.9664 1 2 3 4 17 0.9656 0.9650 0.9654 0.9652 0.9572 0.9574 0.9547 0.9547 0.9474		1														
14 0.9703 0.9669 0.9694 0.9690 0.9697 0.9673 0.9663 0.9664 1 1 2 3 4 15 0.9650 0.9664 0.9600 0.9600 0.9600 0.9601 0.9617 1 2 2 3 4 16 0.9615 0.9600 0.9600 0.9600 0.9600 0.9616 1 2 3 4 19 0.9455 0.9460 0.9444 0.9433 0.9422 0.9421 0.9446 0.9441 1 2 3 4 5 10 0.9365 0.9369 0.9373 0.9367 0.9341 0.9440 0.9433 0.9422 0.9421 0.9460 0.9441 1 2 3 4 5 10 0.9330 0.9325 0.9324 0.9324 0.9324 0.9324 0.9421 1 2 3 4 5 5 10 0.9305 0.9324 0.9324 <td< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>																
15 0.9655 0.9655 0.9656 0.9643 0.9632 0.9622 0.9627 0.9673 0.9678 0.9573 0.9668 1 2 2 3 4 16 0.9613 0.9568 0.6533 0.9588 0.6532 0.9571 0.9571 1 2 3 4 18 0.9571 0.9563 0.9583 0.9472 0.9466 0.9461 1 2 3 4 5 19 0.9455 0.9449 0.9171 0.9320 0.9221 0.9221 0.9221 0.9221 0.9221 0.9221 0.9221 0.9221 0.9221 0.9221 0.9212 0.921 0.921 0.941 0.9031 0.9021 0.9914 0.913 0.9017 0.9216		1														
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16 0.9613 0.9693 0.9580 0.9580 0.9573 0.9572 0.9571 1 2 2 3 3 18 0.9511 0.9556 0.9530 0.9442 0.9440 0.9449 0.9449 0.9442 0.9442 0.9440 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9449 0.9440 0.9449 0.9449 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9441 0.9444 0.9441 0.944	15	0.9659	0.9655	0.9650	0.9646	0.9641	0.9636	0.9632	0.9627	0.9622	0.9617	1	2	2	3	4
18 0.9511 0.9456 0.94440 0.94840 0.94840 0.94420 0.94472 0.9466 0.9461 1 2 3 4 5 0 0.9337 0.9337 0.9337 0.9337 0.9337 0.9367 0.9364 0.9340 1 2 3 4 5 21 0.9336 0.9330 0.9332 0.9377 0.9371 0.9367 0.9364 0.9324 0.9221 1 2 3 4 6 21 0.9272 0.9262 0.9221 0.9212 1 2 3 4 6 24 0.9136 0.9128 0.9124 0.9114 0.9107 0.9144 0.9137 0.9166 0.9176 0.9170 0.9144 0.9137 0.9361 1 3 4 5 6 25 0.9056 0.9048 0.8906 0.8874 0.8870 0.8870 0.8870 0.8871 0.8763 0.8763 0.8763 0.8763 0.8763 <td></td> <td></td> <td></td> <td></td> <td></td> <td>0.9593</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>1</td> <td>2</td> <td></td> <td>3</td> <td>4</td>						0.9593						1	2		3	4
19 0.9455 0.9444 0.9438 0.9432 0.9421 0.9415 0.9409 0.9403 1 2 3 4 5 20 0.9337 0.9336 0.9373 0.9377 0.9376 0.9346 0.9344 0.9342 1 2 3 4 5 21 0.9326 0.9327 0.9325 0.9226 0.9219 0.9212 1 2 3 4 6 21 0.9335 0.9128 0.9111 0.9117 0.9117 0.9117 0.9117 0.9113 1 2 3 4 5 6 24 0.9128 0.9111 0.9103 0.9026 0.9018 0.9114 0.9143 1 3 4 5 6 25 0.9033 0.9056 0.9044 0.9034 0.8926 0.8918 1 3 4 5 7 26 0.8804 0.8891 0.8847 0.8840 0.8842 0.8843 0.88																
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46 0.6947 0.6934 0.6921 0.6909 0.6896 0.6884 0.6871 0.6858 0.6833 2 4 6 8 11 47 0.6820 0.6807 0.6794 0.6782 0.6769 0.6756 0.6743 0.6730 0.6717 0.6704 2 4 6 9 11 48 0.6691 0.6678 0.6665 0.6622 0.6639 0.6266 0.6613 0.6600 0.6587 0.6574 2 4 7 9 11 49 0.6561 0.6547 0.6534 0.6521 0.6508 0.6494 0.6481 0.6488 0.6411 2 4 7 9 11 50 0.6428 0.6414 0.6401 0.6388 0.6374 0.6361 0.6347 0.6334 0.6320 0.6307 2 4 7 9 11 51 0.6280 0.6280 0.6225 0.6239 0.6255 0.6211 0.6184 0.6170 2 5 7 9 12 53 0.6115 0.611	45	0 7071	0 7050	0 7046	0 7034	0 7022	0 7000	0 6007	0 6084	0 6072	0 6050	2	А	6	R	10
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48 0.6691 0.6678 0.66658 0.6652 0.6639 0.6626 0.6613 0.6600 0.6587 0.6574 2 4 7 9 11 50 0.6541 0.6547 0.6504 0.6521 0.6508 0.6494 0.6481 0.6488 0.6455 0.6441 2 4 7 9 11 50 0.6428 0.6414 0.6401 0.6388 0.6374 0.6361 0.6347 0.6334 0.6320 0.6307 2 4 7 9 11 51 0.6293 0.6280 0.6266 0.6252 0.6239 0.6255 0.6211 0.6198 0.6184 0.6170 2 5 7 9 12 52 0.6157 0.6143 0.6129 0.6115 0.6101 0.6088 0.6404 0.6000 0.6046 0.6032 2 5 7 9 12 53 0.6018 0.6004 0.5990 0.5976 0.5962 0.5973 0.5779 0.5764 0.5750 2 5 7 9 12 <td></td>																
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WCS - Lift & Ecalator Mechanic : (NSOF - Revised 2022) - 1st Vear : Exercise 1.8.30 87	59	0.5150	0.5135	0.5120	0.5105	0.5090	0.5075	0.5060	0.5045	0.5030	0.5015	3	5	б	10	13
			WCe	ift 2 E	calator	Machar				2022)	1st Voor	· Evor		0 20		87

WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.8.30

Natural Cosines

Numbers in different columns to be subtracted, not added

0	01		4.01	4.01	0.41	0.01	0.01	401	4.01	541		0	01	41	C 1
	0'	6'	12'	18'	24'	30'	36'	42' 0.7°	48'	54'	1'	2'	3'	4'	5'
	0.0°	0.1°	0.2°	0.3 ^o	0.4°	0.5 ⁰	0.6 ^o	0.70	0.8 ^o	0.9 ^o					
60	0.5000	0.4985	0.4970	0.4955	0.4939	0.4924	0.4909	0.4894	0.4879	0.4863	3	5	8	10	13
61	0.4848	0.4833	0.4818	0.4802	0.4787	0.4772	0.4756	0.4741	0.4726	0.4710	3	5	8	10	13
62	0.4695	0.4679	0.4664	0.4648	0.4633	0.4617	0.4602	0.4586	0.4571	0.4555	3	5	8	10	13
63	0.4540	0.4524	0.4509	0.4493	0.4478	0.4462	0.4446	0.4431	0.4415	0.4399	3	5	8	10	13
64	0.4384	0.4368	0.4352	0.4337	0.4321	0.4305	0.4289	0.4274	0.4258	0.4242	3	5	8	11	13
0.5	0.4000	0.4040	0.4405	0 4470	0.4400	0 44 47	0.4404	0 4445	0.4000	0.4000		-	0		10
65	0.4226	0.4210	0.4195	0.4179	0.4163	0.4147	0.4131	0.4115	0.4099	0.4083	3	5	8	11	13
66	0.4067	0.4051	0.4035	0.4019	0.4003	0.3987	0.3971	0.3955	0.3939	0.3923 0.3762	3	5	8	11	13
67 68	0.3907	0.3891 0.3730	0.3875 0.3714	0.3859 0.3697	0.3843 0.3681	0.3827 0.3665	0.3811 0.3649	0.3795	0.3778	0.3762	3	5	8 8	11 11	13 14
69	0.3740	0.3730	0.3714	0.3535	0.3518	0.3503	0.3486	0.3033	0.3453	0.3600	3	5 5	о 8	11	14
09	0.5564	0.3307	0.3551	0.3535	0.3310	0.3302	0.3400	0.3409	0.3455	0.3437	3	5	0	11	14
70	0.3420	0.3404	0.3387	0.3371	0.3355	0.3338	0.3322	0.3305	0.3289	0.3272	3	5	8	11	14
71	0.3256	0.3239	0.3223	0.3206	0.3190	0.3173	0.3156	0.3140	0.3123	0.3107	3	6	8	11	14
72	0.3090	0.3074	0.3057	0.3040	0.3024	0.3007	0.2990	0.2974	0.2957	0.2940	3	6	8	11	14
73	0.2924	0.2907	0.2890	0.2874	0.2857	0.2840	0.2823	0.2807	0.2790	0.2773	3	6	8	11	14
74	0.2756	0.2740	0.2723	0.2706	0.2689	0.2672	0.2656	0.2639	0.2622	0.2605	3	6	8	11	14
75	0.2588	0.2571	0.2554	0.2538	0.2521	0.2504	0.2487	0.2470	0.2453	0.2436	3	6	8	11	14
76	0.2419	0.2402	0.2385	0.2368	0.2351	0.2334	0.2317	0.2300	0.2284	0.2267	3	6	8	11	14
77	0.2250	0.2233	0.2215	0.2198	0.2181	0.2164	0.2147	0.2130	0.2113	0.2096	3	6	9	11	14
78	0.2079	0.2062	0.2045	0.2028	0.2011	0.1994	0.1977	0.1959	0.1942	0.1925	3	6	9	11	14
79	0.1908	0.1891	0.1874	0.1857	0.1840	0.1822	0.1805	0.1788	0.1771	0.1754	3	6	9	11	14
	0.4700	0.4740	0.4700	0.4005	0.4000	0.4050	0.4000	0.4040	0.4500	0.4500		~	0		
80	0.1736	0.1719	0.1702	0.1685	0.1668	0.1650	0.1633	0.1616	0.1599	0.1582	3	6	9	11	14
81 82	0.1564 0.1392	0.1547	0.1530	0.1513 0.1340	0.1495 0.1323	0.1478 0.1305	0.1461 0.1288	0.1444 0.1271	0.1426 0.1253	0.1409 0.1236	3	6	9 9	11 12	14 14
83	0.1392	0.1374	0.1357	0.1340	0.1323	0.1305	0.1200	0.1271	0.1253	0.1236	3	6 6	9	12	14
84	0.1219	0.1201	0.1104	0.0993	0.0976	0.0958	0.0941	0.1097	0.0906	0.1003	3	6	9	12	14
04	0.1045	0.1020		0.0993	0.0970	0.0950	0.0941	0.0924	0.0906	0.0009		U	9	12	14
85	0.0872	0.0854	0.0837	0.0819	0.0802	0.0785	0.0767	0.0750	0.0732	0.0715	3	6	9	12	14
86	0.0698	0.0680	0.0663	0.0645	0.0628	0.0610	0.0593	0.0576	0.0558	0.0541	3	6	9	12	15
87	0.0523	0.0506	0.0488	0.0471	0.0454	0.0436	0.0419	0.0401	0.0384	0.0366	3	6	9	12	15
88	0.0349	0.0332	0.0314	0.0297	0.0279	0.0262	0.0244	0.0227	0.0209	0.0192	3	6	9	12	15
89	0.0175	0.0157	0.0140	0.0122	0.0105	0.0087	0.0070	0.0052	0.0035	0.0017	3	6	9	12	15
90	0.0000														



Quadrant	Angle	cos A =	Examples
First	0 to 90°	cos A	cos 33°26' = 0.8345
Second	90° to 180°	-cos(180°-A)	sin 146°34' = -cos(180° - 146o 34')
			= -cos 33o26' = -0.8345
Third	180° to 270°	cos(A – 180°)	$\cos 213^{\circ}26' = -\cos(213^{\circ}26' - 180^{\circ})$
			= -cos 33°26' = -0.8345
Fourth	270° to 360°	cos(360°-A)	$\cos 326^{\circ}34' = \cos(360^{\circ} - 326^{\circ}34')$
			= cos 33°26' = 0.8345

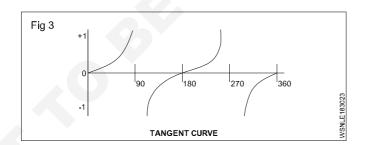
Natural Tangents

• · · · · · · · · · · ·<	utur															
1 0.0175 0.0175 0.0279 0.0244 0.0242 0.0244 0.0140 0.122 0.125 0.1264 0.1260 0.1264 0.1260 0.1264 0.1264 0.1264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264	0								1			1'	2'	3'	4'	5'
1 0.0175 0.0175 0.0279 0.0244 0.0242 0.0244 0.0140 0.122 0.125 0.1264 0.1260 0.1264 0.1260 0.1264 0.1264 0.1264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264 0.2264	0											3	6	9	12	15
2 0.0349 0.0354 0.0384 0.0438 0.0414 0.0412 0.0524 0.0584 0.1104 0.122 0.128 0.1384 0.665 0.1174 0.1384 0.665 0.1174 0.1384 0.665 0.1174 0.1384 0.665 0.1572 0.1584 0.1656 0.1174 0.1384 0.665 0.1174 0.1174 0.1172 0.1284 0.1684 0.1657 0.1572 0.1584 0.1584 0.1572 0.1574 0.1584 0.1584 0.1572 0.1574 0.1572 0.1284 0.2667 0.2753 0.2754 0.2741 0.2717 0.2753 0.2754 0.2741 0.2717 0.2783 0.2854 0.2261 0.2441												1				
4 0.0899 0.0714 0.0734 0.0752 0.0769 0.0805 0.0867 3 6 9 12 15 5 0.0677 0.0892 0.0910 0.0924 0.0946 0.0981 0.0985 0.1175 0.1125 0.1216 <												1				
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38 0.7813 0.7841 0.7869 0.7898 0.7926 0.7954 0.7983 0.8012 0.8040 0.8069 5 9 14 19 24 39 0.8098 0.8127 0.8185 0.8185 0.8243 0.8243 0.8302 0.8332 0.8361 5 9 14 19 24 40 0.8391 0.8421 0.8451 0.8481 0.8211 0.8541 0.8571 0.8601 0.8622 5 10 15 20 25 41 0.8693 0.8724 0.8754 0.8785 0.8847 0.8847 0.8841 0.8910 0.8941 0.8972 5 10 16 21 26 42 0.9004 0.9035 0.9077 0.9099 0.9131 0.9163 0.9195 0.9228 0.9260 0.9293 5 11 16 21 22 28 44 0.9657 0.9691 0.9725 0.9759 0.9775 0.9827 <td< td=""><td>36</td><td>0.7265</td><td>0.7292</td><td>0.7319</td><td>0.7346</td><td>0.7373</td><td>0.7400</td><td>0.7427</td><td>0.7454</td><td>0.7481</td><td>0.7508</td><td>5</td><td>9</td><td>14</td><td>18</td><td>23</td></td<>	36	0.7265	0.7292	0.7319	0.7346	0.7373	0.7400	0.7427	0.7454	0.7481	0.7508	5	9	14	18	23
39 0.8098 0.8127 0.8156 0.8185 0.8214 0.8273 0.8322 0.8332 0.8331 5 10 15 20 24 40 0.8391 0.8421 0.8451 0.8481 0.8511 0.8571 0.8601 0.8632 0.8662 5 10 15 20 24 40 0.8693 0.8724 0.8754 0.8755 0.8816 0.8874 0.8878 0.8910 0.8941 0.8972 5 10 16 21 26 42 0.9004 0.9036 0.9067 0.9099 0.9131 0.9163 0.9195 0.9226 0.9260 0.9233 6 11 17 22 28 44 0.9657 0.9691 0.9725 0.9739 0.9827 0.9861 0.9930 0.9965 6 11 17 22 28 45 1.0000 1.0035 1.0070 1.0165 1.0141 1.0176 1.0247 1.0283 1.0319									1							
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42 0.9004 0.9036 0.9067 0.9099 0.9131 0.9163 0.9195 0.9228 0.9260 0.9293 5 11 16 21 27 43 0.9325 0.9358 0.9391 0.9424 0.9457 0.9490 0.9523 0.9556 0.9590 0.9623 6 11 17 22 28 44 0.9657 0.9991 0.9725 0.9759 0.9793 0.9827 0.9861 0.9896 0.9930 0.9965 6 11 17 22 28 45 1.0000 1.0035 1.0070 1.0105 1.0141 1.0176 1.0212 1.0247 1.0283 1.0319 6 12 18 24 30 46 1.0355 1.0392 1.0428 1.0464 1.0501 1.0538 1.0575 1.0612 1.0649 1.0686 6 12 18 25 31 47 1.0761 1.0799 1.0837 1.0875 1.0913 1.01951 1.1760 1.1762 1.1833 1.1463 7 14 21		1							1							
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WCS - Lift & Ecalator Mechanic : (NSQF - Revised 2022) - 1st Year : Exercise 1.8.30

Natural Tangents

		1					1	1							
0	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	0.0°	0.1°	0.2°	0.3 ^o	0.4 ^o	0.5°	0.6°	0.7°	0.8 ⁰	0.9 ^o					
			-												
60	1.7321	1.7391	1.7461	1.7532	1.7603	1.7675	1.7747	1.7820	1.7893	1.7966	12	24	36	48	60
61	1.8040	1.8115	1.8190	1.8265	1.8341	1.8418	1.8495	1.8572	1.8650	1.8728	13	26	38	51	64
62	1.8807	1.8887	1.8967	1.9047	1.9128	1.9210	1.9292	1.9375	1.9458	1.9542	14	27	41	55	68
63	1.9626	1.9711	1.9797	1.9883	1.9970	2.0057	2.0145	2.0233	2.0323	2.0413	15	29	44	58	73
64	2.0503	2.0594	2.0686	2.0778	2.0872	2.0965	2.1060	2.1155	2.1251	2.1348	16	31	47	63	78
65	2.1445	2.1543	2.1642	2.1742	2.1842	2.1943	2.2045	2.2148	2.2251	2.2355	17	34	51	68	85
66	2.2460	2.2566	2.2673	2.2781	2.2889	2.2998	2.3109	2.3220	2.3332	2.3445	18	37	55	73	92
67	2.3559	2.3673	2.3789	2.3906	2.4023	2.4142	2.4262	2.4383	2.4504	2.4627	20	40	60	79	99
68	2.4751	2.4876	2.5002	2.5129	2.5257	2.5386	2.5517	2.5649	2.5782	2.5916	22	43	65	87	108
69	2.6051	2.6187	2.6325	2.6464	2.6605	2.6746	2.6889	2.7034	2.7179	2.7326	24	47	71	95	119
	0 7475	0 7005	0 7770	0 7000	0.0000	0.0000	0.0007	0.0550	0.0740	0.0070		50	70	404	404
70	2.7475	2.7625	2.7776	2.7929	2.8083	2.8239	2.8397	2.8556	2.8716	2.8878	26	52	78	104	131
71	2.9042	2.9208	2.9375	2.9544	2.9714	2.9887	3.0061	3.0237	3.0415	3.0595	29	58	87 96	116	145
72 73	3.0777 3.2709	3.0961 3.2914	3.1146 3.3122	3.1334	3.1524 3.3544	3.1716 3.3759	3.1910 3.3977	3.2106 3.4197	3.2305	3.2506 3.4646	32	64	96 108	129 144	161
73	3.2709	3.2914	3.5339	3.3332 3.5576	3.3544	3.3759	3.6305	3.4197	3.4420	3.4646	36 41	72 81	108	144	180 204
14	3.4074	3.5105	3.0009	3.5570	3.3010	3.0059	3.0305	3.0334	3.0000	3.7002	41	01	122	103	204
75	3.7321	3.7583	3.7848	3.8118	3.8391	3.8667	3.8947	3.9232	3.9520	3.9812	46	93	139	186	232
76	4.0108	4.0408	4.0713	4.1022	4.1335	4.1653	4.1976	4.2303	4.2635	4.2972	53	107	160	213	267
77	4.3315	4.3662	4.4015	4.4374	4.4737	4.5107	4.5483	4.5864	4.6252	4.6646		101	100	210	207
78	4.7046	4.7453	4.7867	4.8288	4.8716	4.9152	4.9594	5.0045	5.0504	5.0970					
79	5.1446	5.1929	5.2422	5.2924	5.3435	5.3955	5.4486	5.5026	5.5578	5.6140					
			-												
80	5.6713	5.7297	5.7894	5.8502	5.9124	5.9758	6.0405	6.1066	6.1742	6.2432		DIF	FERENC	ΈS	
81	6.3138	6.3859	6.4596	6.5350	6.6122	6.6912	6.7720	6.8548	6.9395	7.0264		UNT	RUSTW	ORTHY	
82	7.1154	7.2066	7.3002	6.3962	7.4947	7.5958	7.6996	7.8062	7.9158	8.0285			HERE		
83	8.1443	8.2636	8.3863	8.5126	8.6427	8.7769	8.9152	9.0579	9.2052	9.3572					
84	9.5144	9.677	9.845	10.02	10.20	10.39	10.58	10.78	10.99	11.20					
85	11.43	11.66	11.91	12.16	12.43	12.71	13.00	13.30	13.62	13.95					
	11.00	44.07	45.00	45.40	45.00	40.05	10.00	47.04	47.00	10.10					
86	14.30	14.67	15.06	15.46	15.89	16.35	16.83	17.34	17.89	18.46					
87	19.08	19.74	20.45 31.82	21.20	22.02	22.90	23.86	24.90	26.03	27.27					
88 89	28.64 57.29	30.14 63.66	71.62	33.69 81.85	35.80 95.49	38.19 114.6	40.92 143.2	44.07 191.0	47.74 286.5	52.08 573.0					
90	57.29 ×	03.00	/ 1.02	01.05	93.49	114.0	143.2	191.0	200.5	515.0					
90	^														



Quadrant	Angle	tan A =	Examples					
First	0 to 90°	tan A	tan 56°17' = 1.4986					
Second	90° to 180°	–tan(180° – A)	tan 123°43' = –tan(180° – 123° 43')					
			=tan 56°17' =1.4986					
Third	180° to 270°	tan(A – 180°)	tan 236°17' = tan(236°17' – 180°)					
			= tan 56°17' = 1.4986					
Fourth	270° to 360°	-tan(360° - A)	tan 303°43' = -tan(360° - 303°43')					
			= – tan 56°17' = –1.4986					
			= - tan 56°17' = -1.4986					